

Mechanical Properties of Spoke Cavities

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July 12, 2005*

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*A U.S. Department of Energy Office of Science Laboratory
Managed by The University of Chicago*

Collaborators

- **ANL**
 - Ken Shepard, Mike Kelly, Joel Fuerst, Mark Kedzie, Gary Zinkann

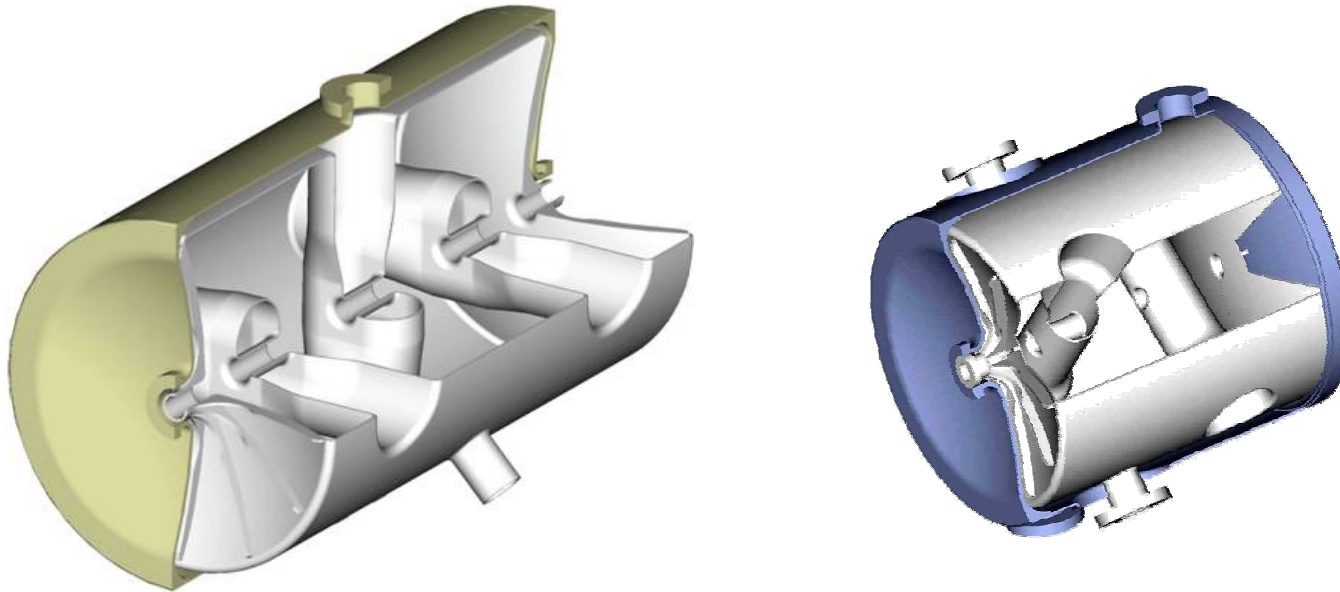
- **AES**
 - John Rathke, Tom Schultheiss

- **Energen**
 - Chad Joshi, Chiu-Ying Tai

Spoke Cavity Mechanical Properties

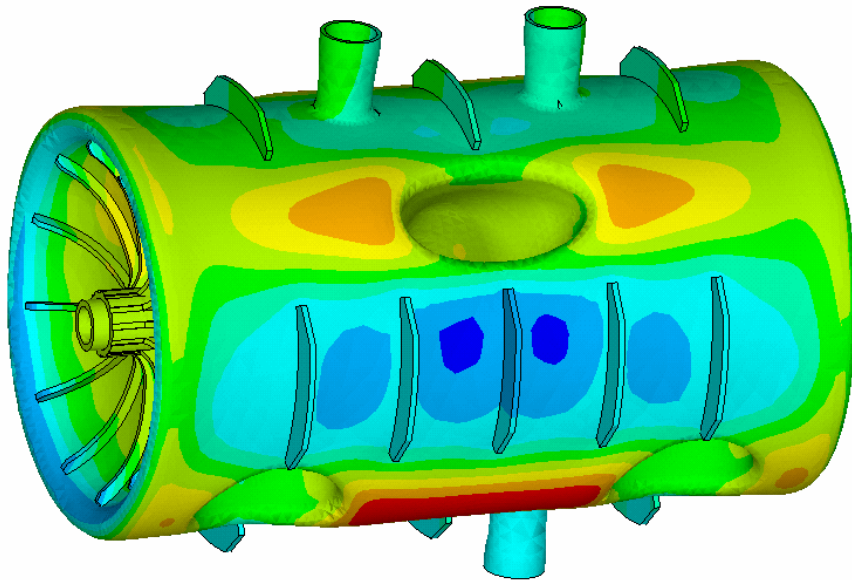
- **SC cavities typically have both a small loaded and a small intrinsic bandwidth. This makes them very sensitive to mechanical deformations which result in frequency variations.**
- **Mechanical Properties:**
 - cw operation => microphonic induced noise.
 - pulsed operation => Lorentz Detuning.

Spoke Cavity Mechanical Properties

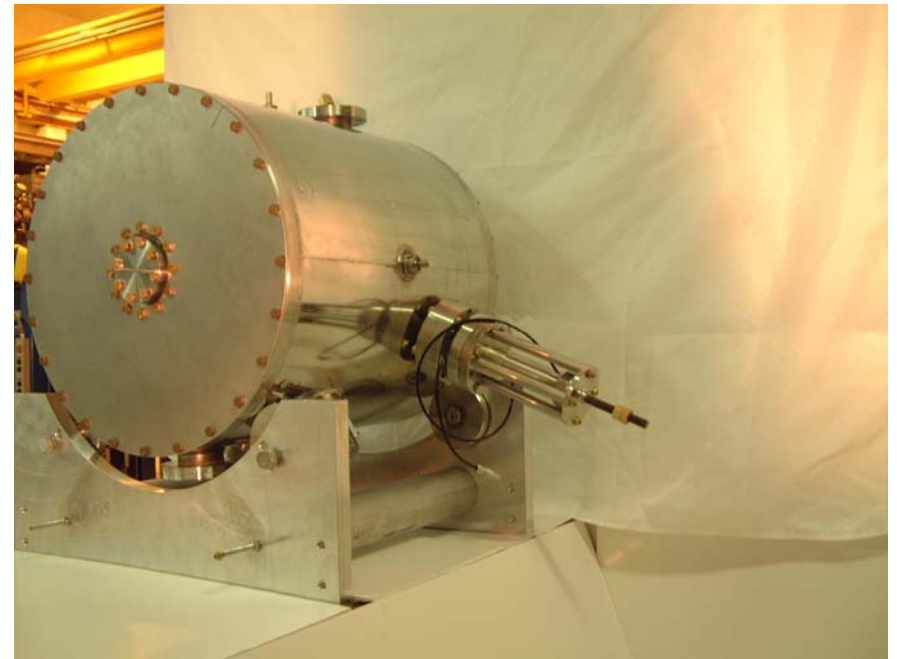


- **Methods of controlling amplitude and phase errors:**
 - Overcoupling
 - Reactive Tuners
 - Fast Mechanical Tuners
 - *Piezoelectric actuated*
 - *Magnetostrictive actuated*

Outline

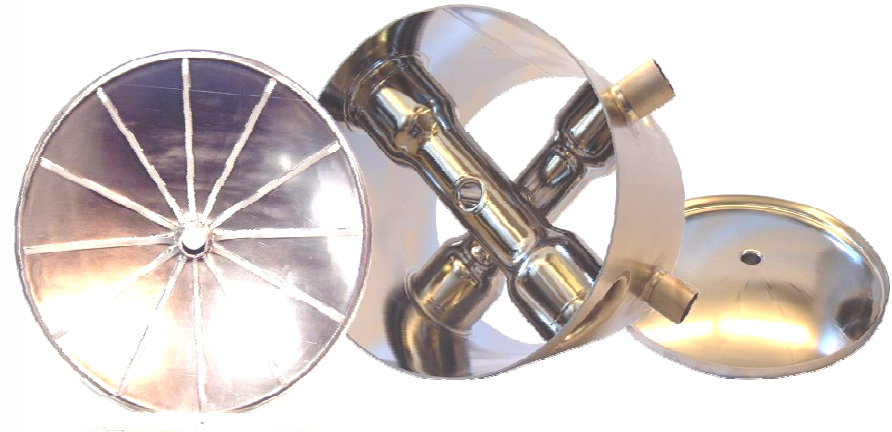
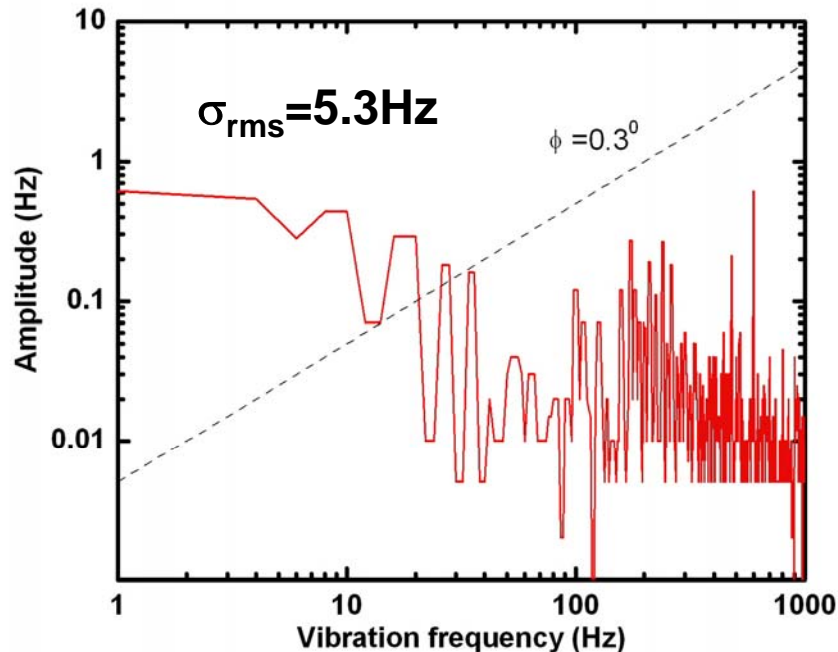


- **Cavity mechanical properties.**



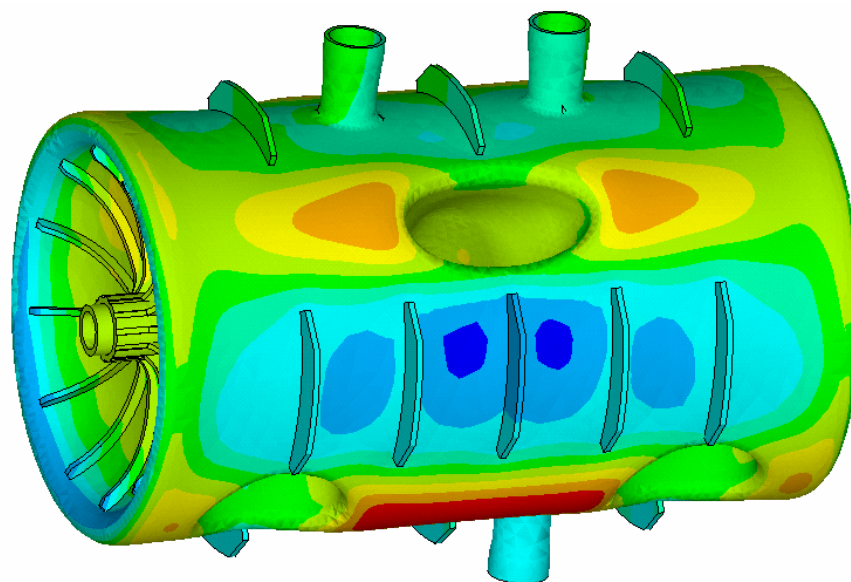
- **Fast mechanical tuners.**

$\beta = 0.4$ Double Spoke Microphonics



- Results of first cold test of a production model double spoke cavity with an integral stainless steel housing holding the liquid helium bath.
- $\Delta f / \Delta P = -76 \text{ Hz/torr}$

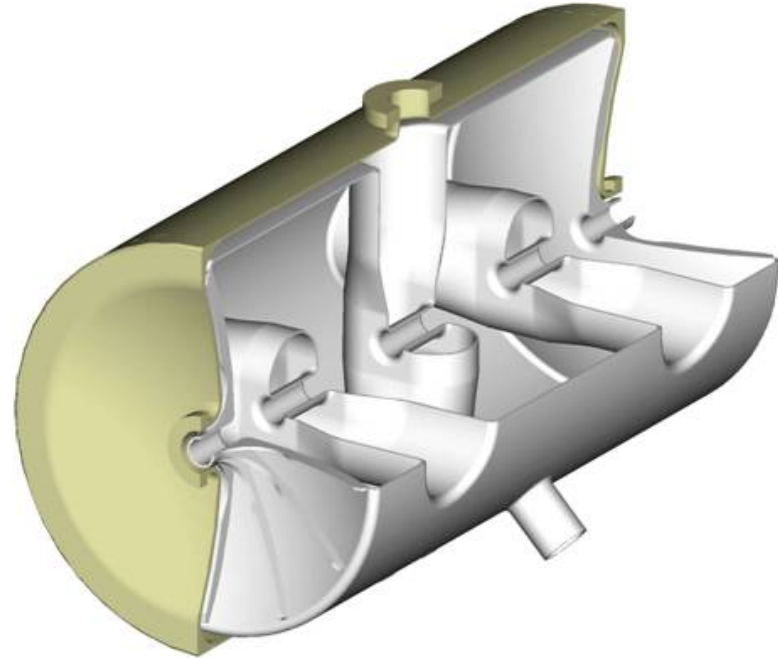
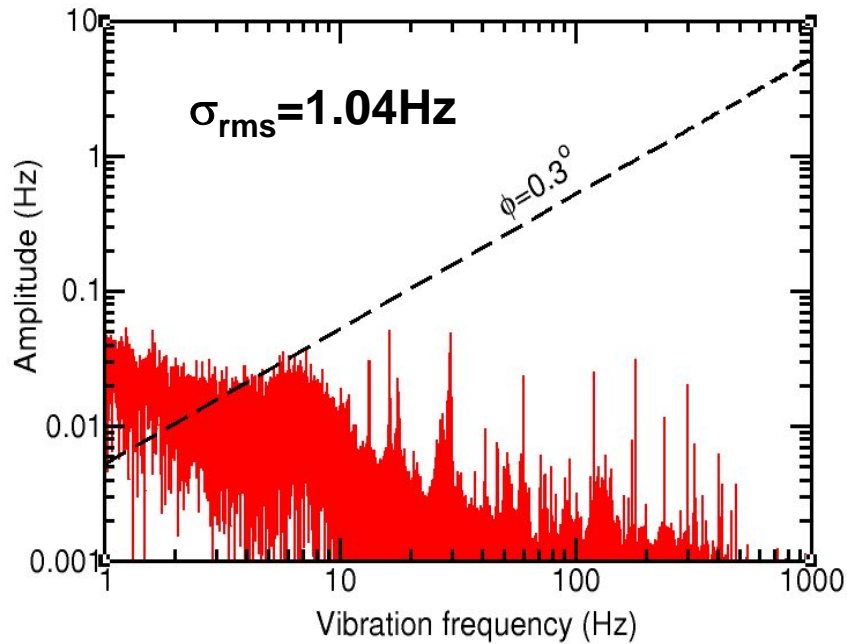
$\beta = 0.5$ Triple Spoke Cavity



- $\beta=0.5$ triple spoke cavity designed* to minimize $\Delta f/\Delta P$.
- Designed to balance the electric and magnetic field contributions to frequency shifts due to uniform external pressure.

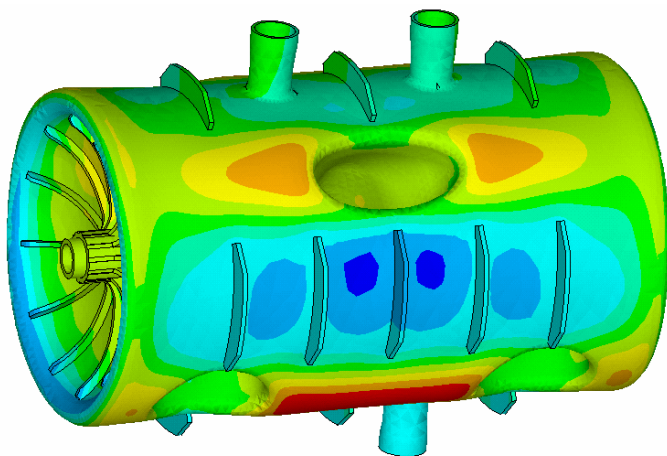
* Modeling performed by AES.

$\beta = 0.5$ Triple Spoke Microphonics

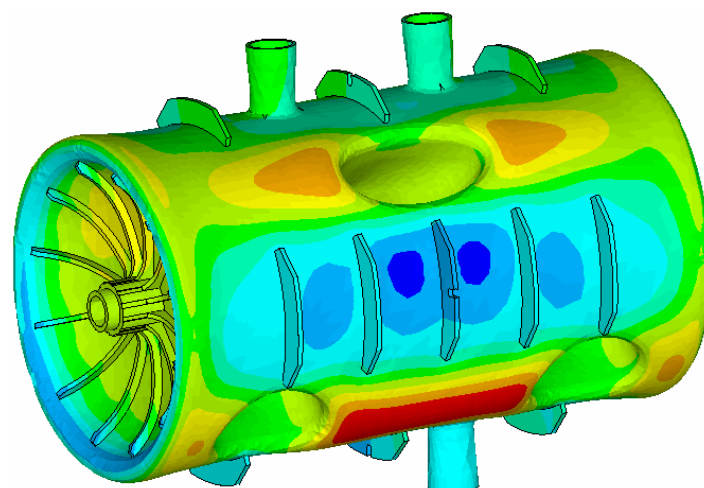


- **Cavity tested in a realistic accelerator environment.**
 $\Delta f / \Delta P = -12.4 \text{ Hz/torr}$

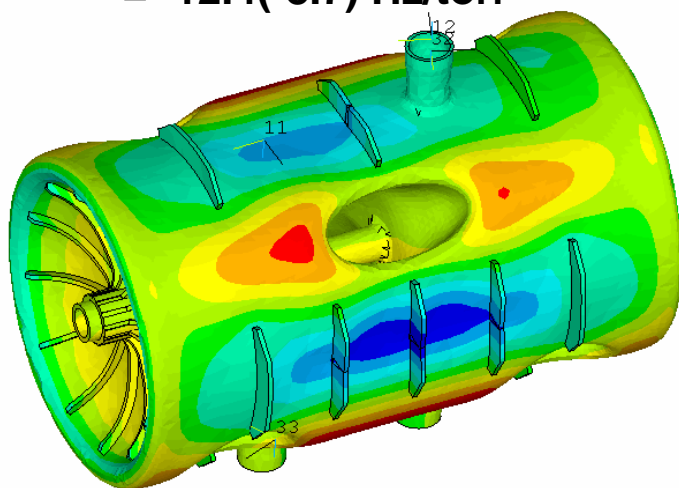
$\beta = 0.5$ Triple Spoke Cavity



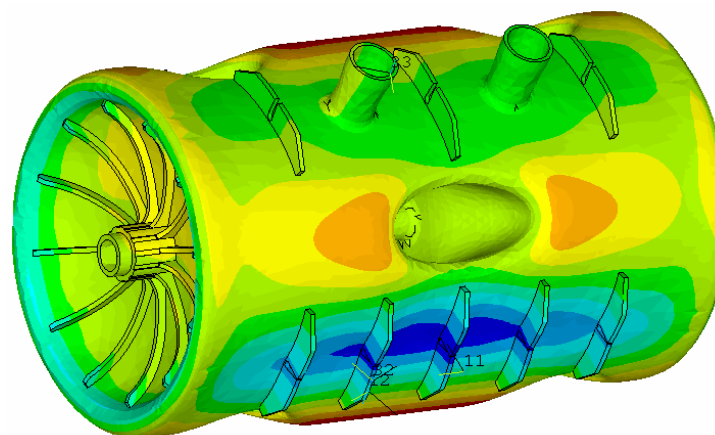
measured $\Delta f/\Delta P$ (predicted)
= -12.4(-8.7) Hz/torr



$\Delta f/\Delta P = -6.3(-4.7)$ Hz/torr



$\Delta f/\Delta P = -2.5(-0.3)$ Hz/torr

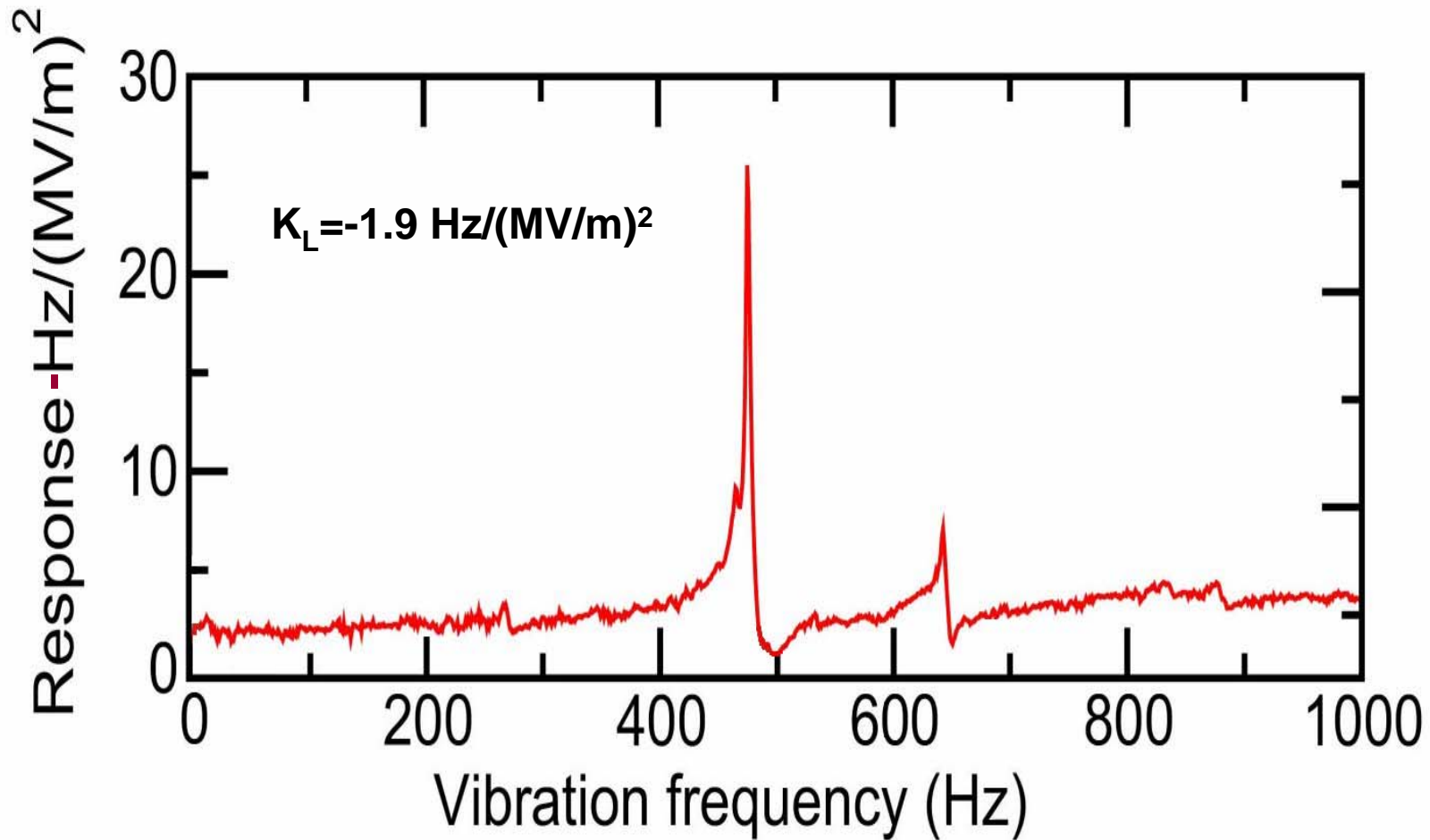


$\Delta f/\Delta P = -0.5(+5.4)$ Hz/torr

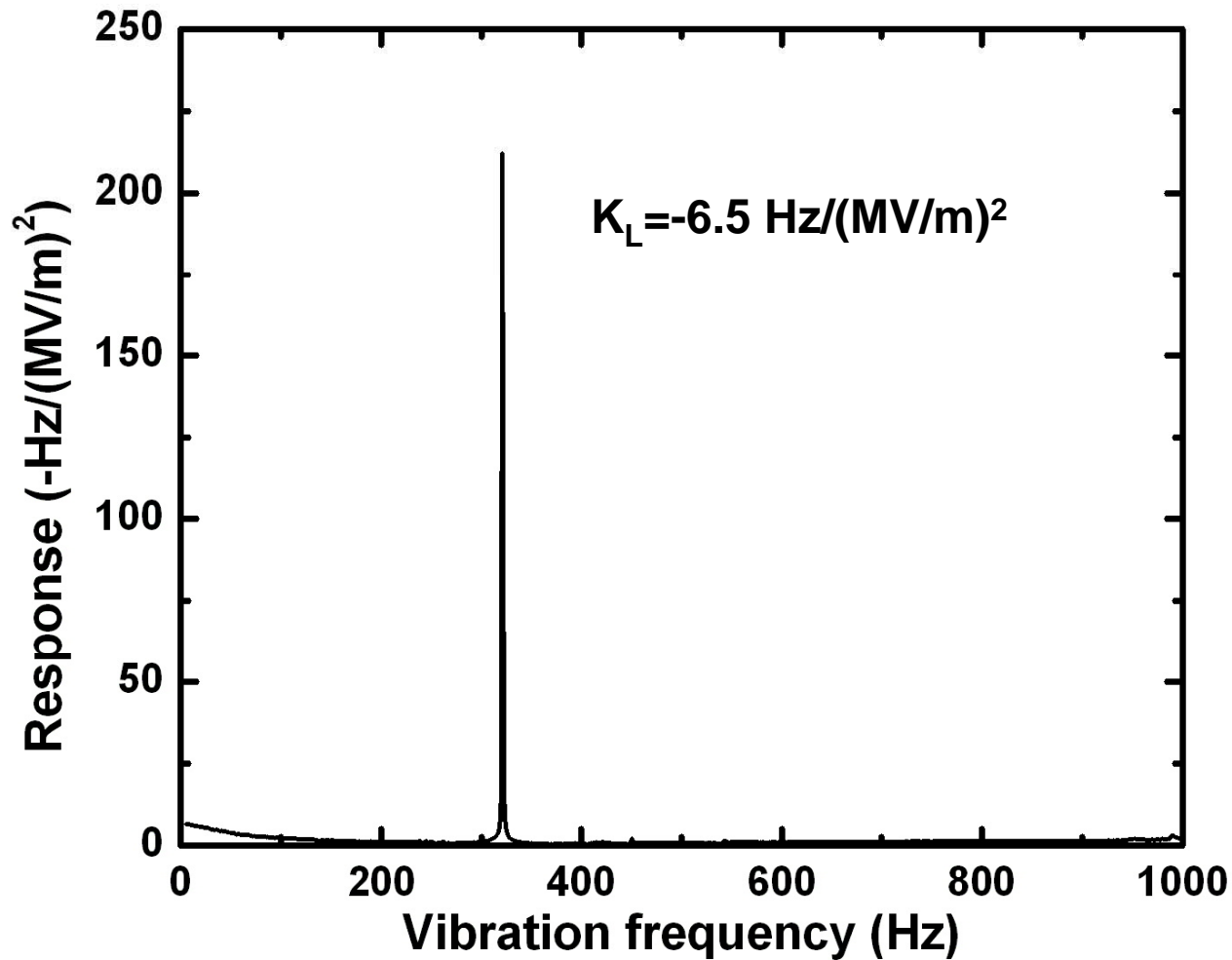
Changing Gears

- **Finished talking about microphonics.**
- **I am now going to talk about Lorentz detuning.**

$\beta = 0.4$ Double Spoke Lorentz Transfer Function

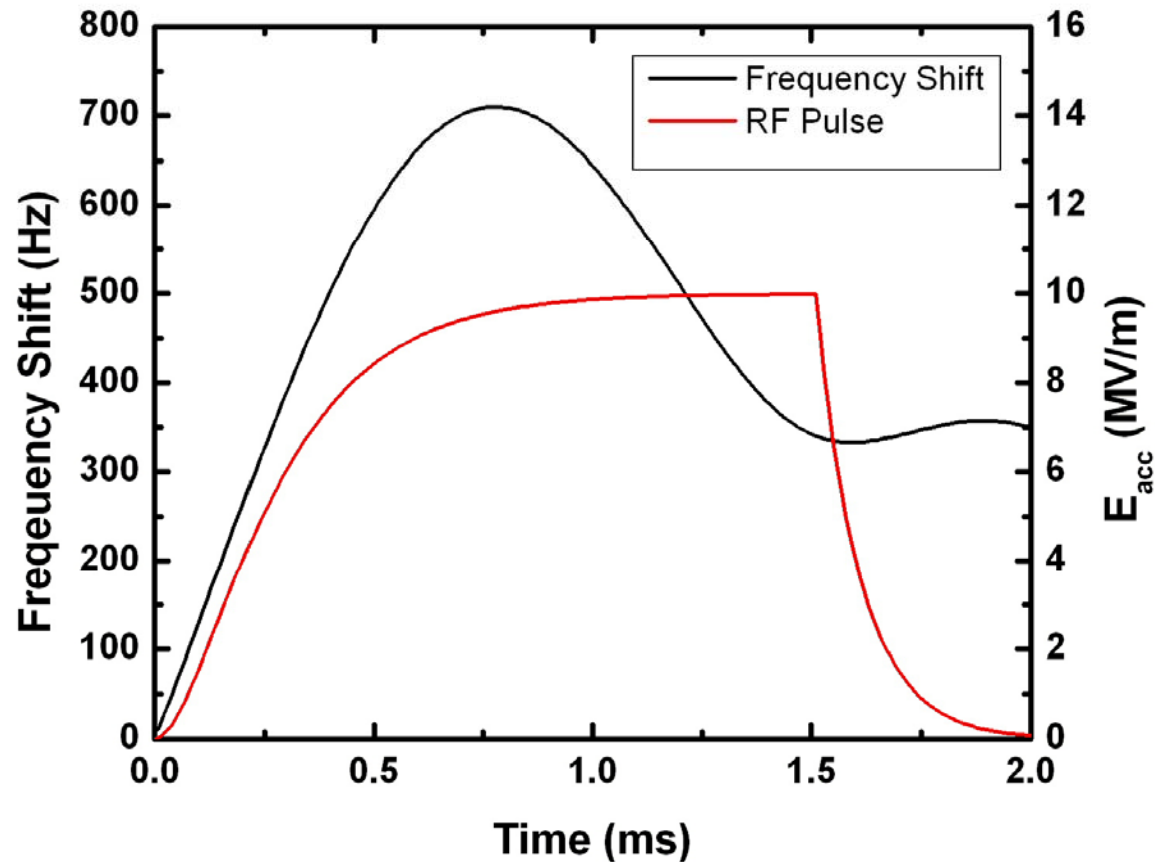


$\beta = 0.5$ Triple Spoke Lorentz Transfer Function

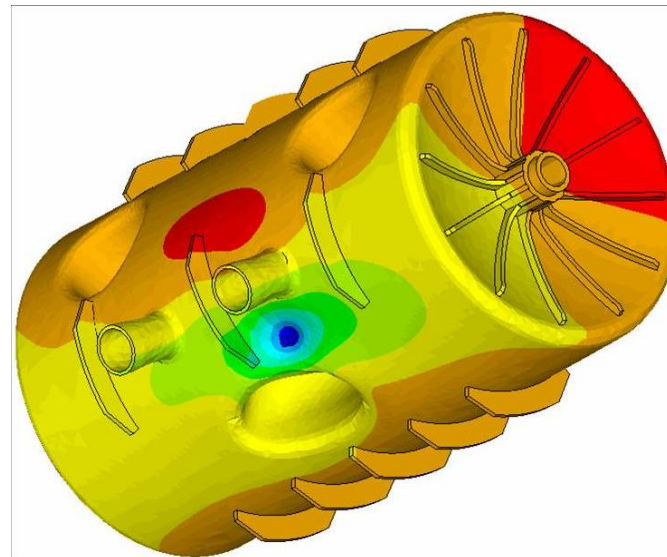
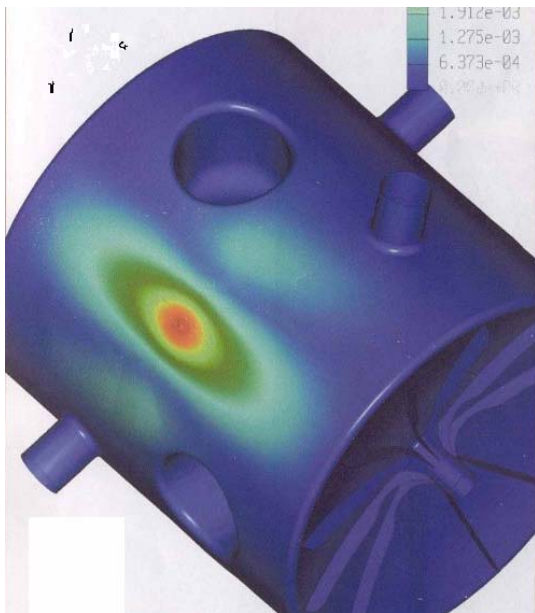
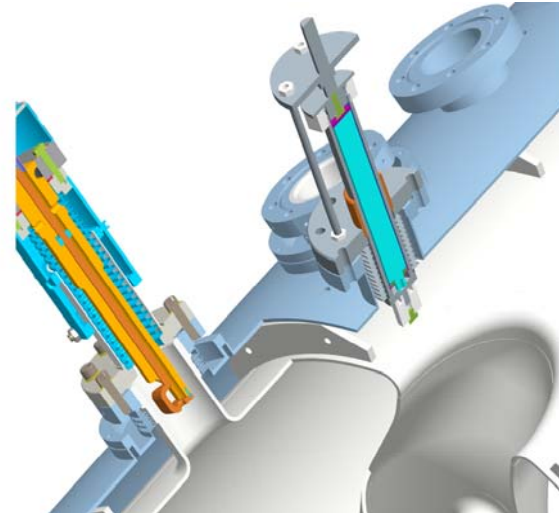
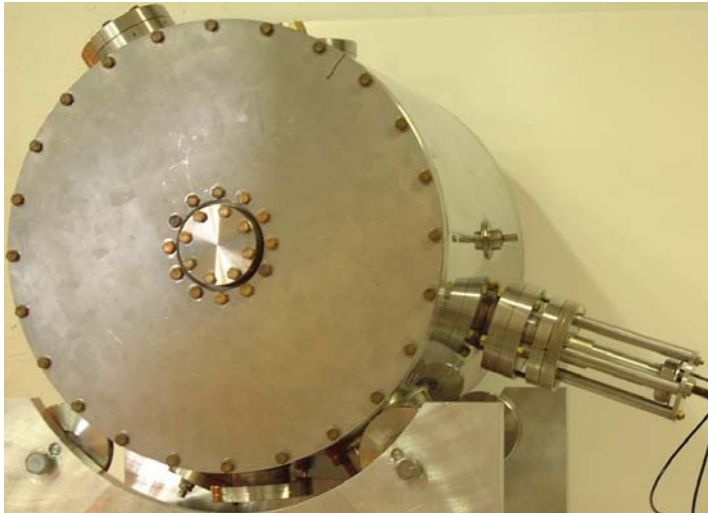


Frequency Variation Due to Pulsed Fields Prediction

$$\text{Response}(t) = \int_{-\infty}^{\infty} (\text{Transfer Function}(\omega) * \text{Input}(\omega)) e^{-i\omega t} d\omega$$



Spoke Cavity Fast Mechanical Tuning

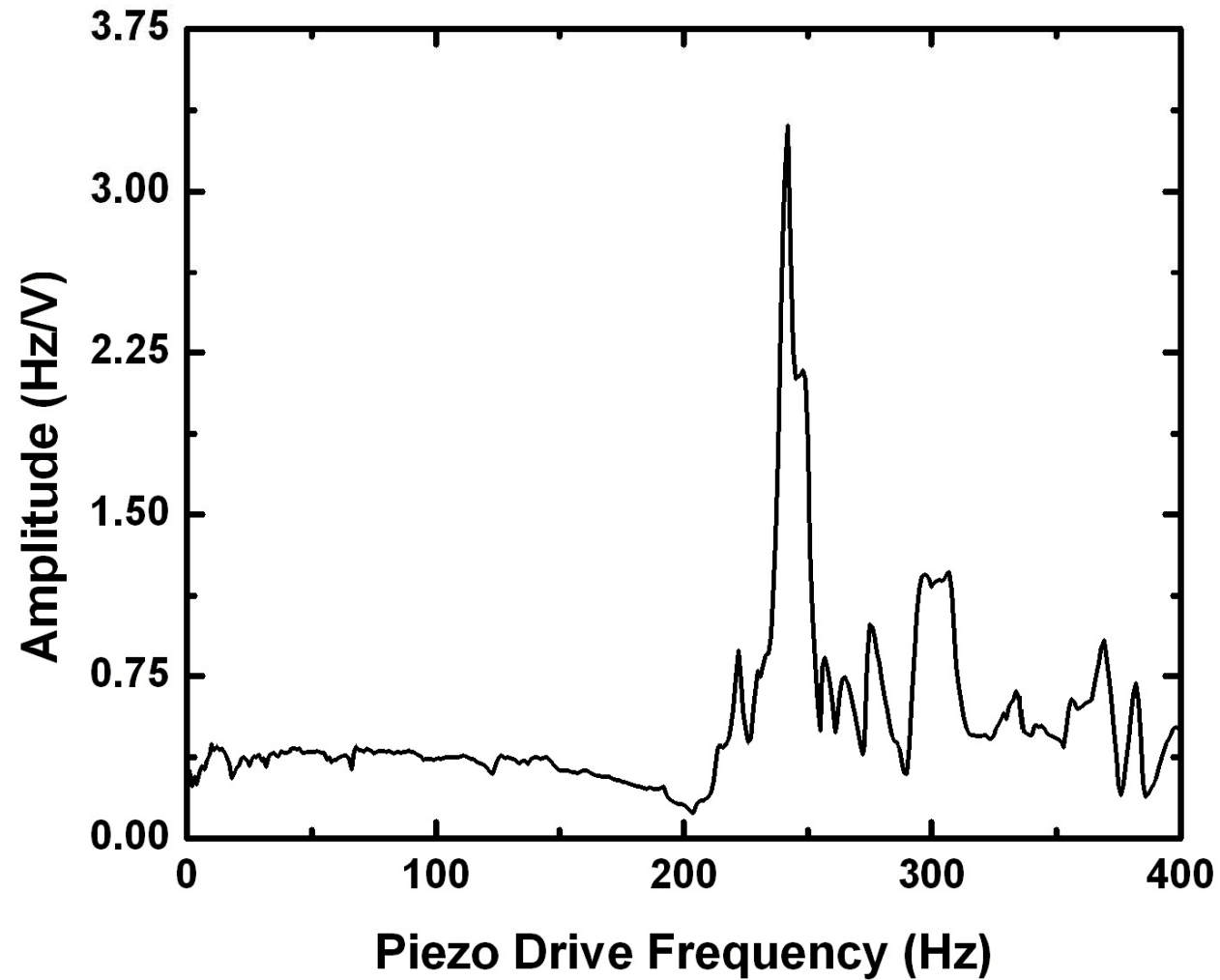


Piezoelectric Actuated Fast Tuner

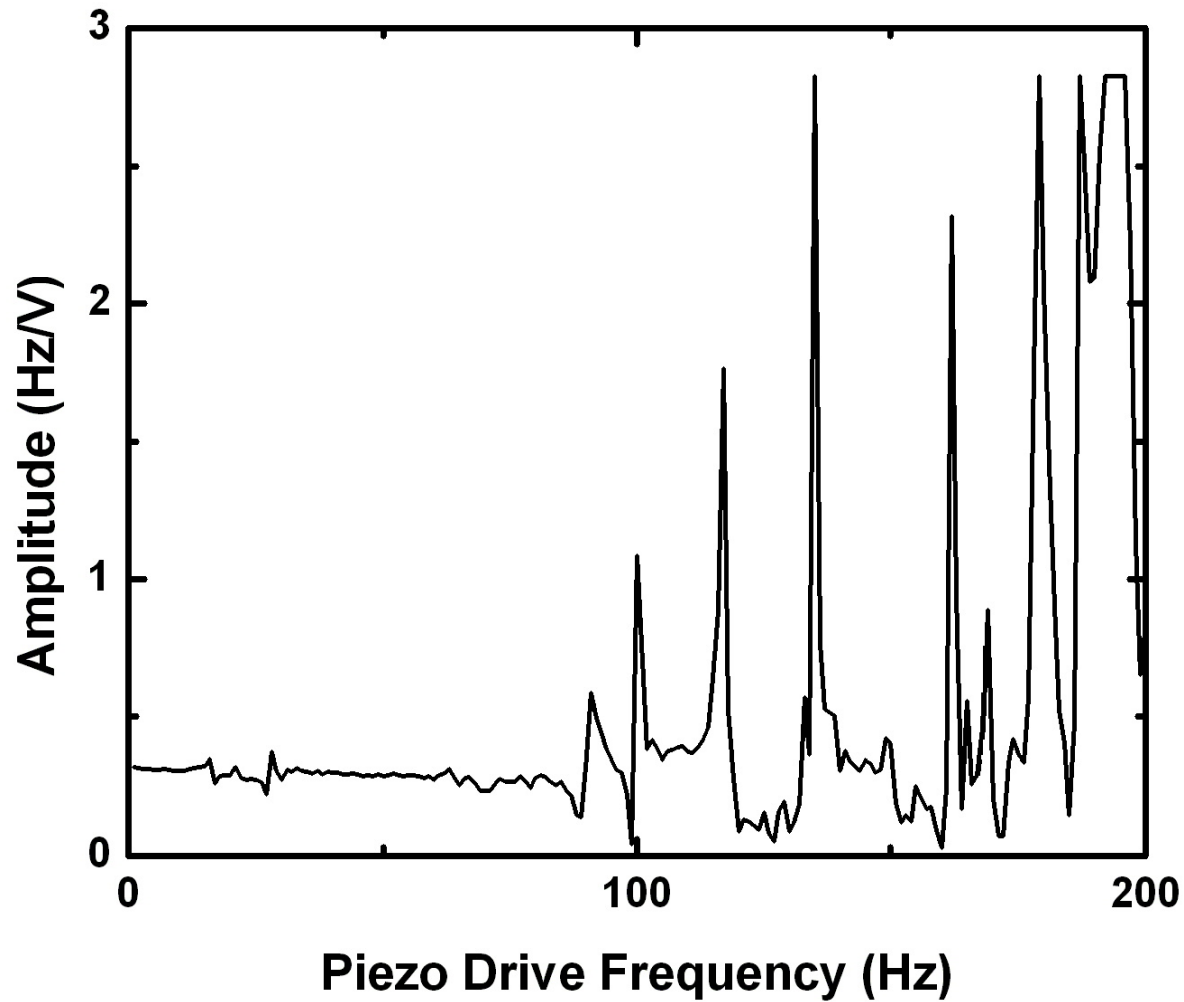


- Response time <math><1\text{ms}</math>.
- Layered piezo-ceramic material electrically connected in parallel operating at $\sim 20\text{K}$ with a resolution of 2nm purchased from Physik Instrumente.
- Not designed for high frequency operation.

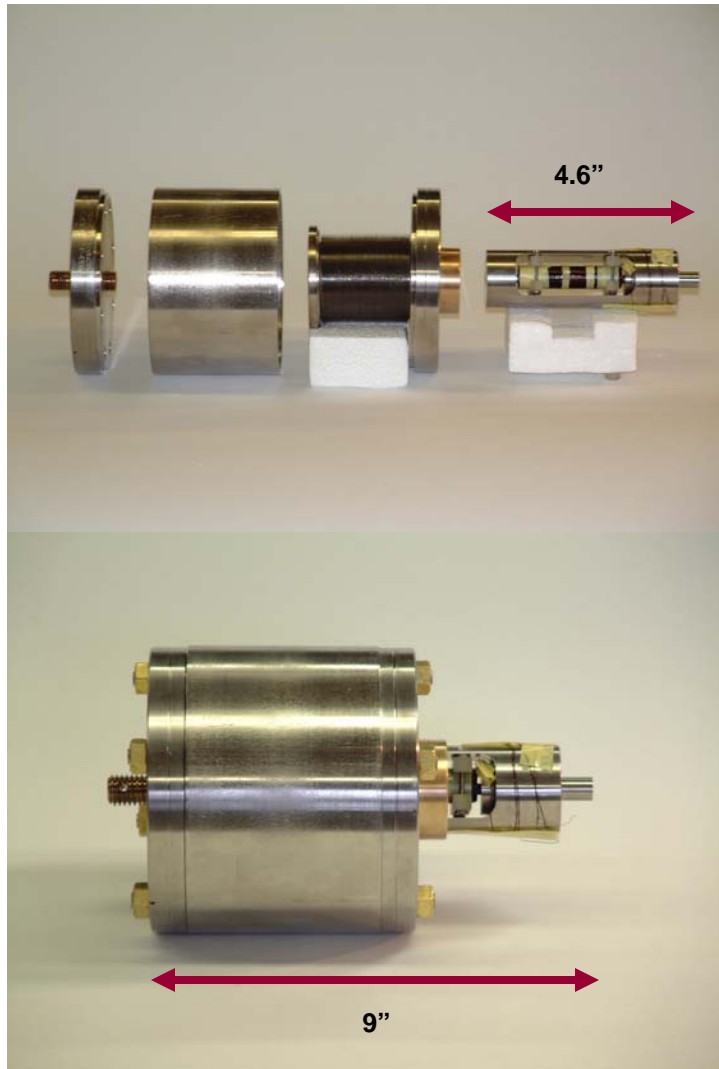
$\beta = 0.4$ Double Spoke Piezo Transfer Function



$\beta = 0.5$ Triple Spoke Piezo Transfer Function



Magnetostrictive Actuated Fast Tuner



- Magnetostrictive actuator designed and built by Energen, Inc and slated to be tested at ANL.
- Response time <6ms.
- Magnetostrictive rod coaxial with an external solenoid operating at 4K.

Future Work

- **Measure microphonic induced noise spectrum of $\beta = 0.5$ triple spoke cavity to measure the effect of modifying the support ribs.**
- **Pulse a spoke cavity and measure the frequency variation.**
- **Use fast mechanical tuners to reduce frequency variations due to microphonics and the Lorentz force.**

Lorentz Transfer Function

- Amplitude modulated RF fields are expressed as:

$$\vec{E}_i(\vec{x}, t) = A(t) \vec{E}_i(\vec{x}) e^{2\pi i f_i t}$$

$$\vec{H}_i(\vec{x}, t) = A(t) \vec{H}_i(\vec{x}) e^{2\pi i f_i t}$$

- The local displacement of a cavity surface can be expressed as:

$$\vec{u}(\vec{x}, t) = \sum_i \eta_i(t) \vec{\xi}_i(\vec{x})$$

Frequency Shift

$$\Delta f(t) = f_0 \sum_i \frac{A^2(t)}{\sqrt{2\pi M_{ii}}} \frac{\int_{-\infty}^{\infty} \frac{e^{i\omega t}}{\left(\Omega_i^2 - \omega^2 - \frac{i\Omega_i \omega}{Q_i^{MECH}} \right)} d\omega}{\int_V \left[\frac{1}{\mu_0 c} |\vec{E}_0(\vec{x})|^2 + \epsilon_0 |\vec{H}_0(\vec{x})|^2 \right] d^3x}$$

$$\times \left(\int_{\Delta V} \left[\mu_0 |\vec{H}_0(\vec{x})|^2 - \epsilon_0 |\vec{E}_0(\vec{x})|^2 \right] \vec{\xi}_i(\vec{x}) \cdot d\vec{a} \right)^2$$