

# Phenomenology at neutrino oscillation experiments

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- Neutrino oscillations
- Neutrino oscillation experiments
- Future long-baseline experiments
- Phenomenology at a neutrino factory:
  - standard oscillations
  - non-standard interactions
- Near detectors - MINSIS
- Summary.

# Neutrino basics

- A **neutrino** is an **electrically neutral**, **weakly-interacting fermion**.
- They are the **SU(2) partners of the charged leptons**.
- Experimental evidence (LEP  $Z^0$  decays) shows that there are **3 species of light  $\nu$** .
- Major discovery announced in 1998 by Super-Kamiokande: **neutrino oscillations**.



Super-Kamiokande detector

# Why do $\nu$ 's oscillate?

- Oscillations occur if the interaction (flavour) states of a particle do not coincide with the mass eigenstates.
- The  $\nu$  flavour states are related to the  $\nu$  mass states via a mixing matrix,  $U_{PMNS}$ :

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

# The PMNS matrix

- The **PMNS matrix** is a unitary  $3 \times 3$  matrix <sup>1</sup>.  
⇒ Parameterised by **3 angles and 3 phases**.
- For Dirac particles,  $\psi \neq \bar{\psi}$ , we can absorb 2 phases by making field redefinitions

$$\Rightarrow U_{PMNS} = U(\theta_{12}, \theta_{13}, \theta_{23}, \delta).$$

- But  $\nu$ 's may be **Majorana particles**, so we must retain the additional **2 Majorana phases**:

$$U_{PMNS} = U(\theta_{12}, \theta_{13}, \theta_{23}, \delta) \times \text{Diag}(e^{i\alpha_1}, e^{i\alpha_2}, 1).$$

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<sup>1</sup>We assume... see later!

# Majorana phases

The **Majorana phases never appear in  $\nu$  oscillations...** why not?

- Mathematically:  $\nu_\alpha \rightarrow \nu_\beta \sim U_{\alpha i}^* U_{i\beta}$  so the Majorana phases do not appear in the oscillation probabilities.
- Physically: Majorana particles appear in **lepton-number violating** processes. But  **$\nu$  oscillations** only **violate lepton flavour**.
- So we shouldn't expect to see Majorana phases in  $\nu$  oscillations.
- To measure them, we need experiments which see **LN**V processes, such as **neutrinoless double- $\beta$  decay**.

# Oscillation probabilities

Oscillations probabilities, in vacuum, are straightforward to calculate. The probability for  $\nu_\alpha \rightarrow \nu_\beta$  takes the form:

$$P_{\alpha\beta} \sim X_{\alpha\beta}(\theta_{12}, \theta_{23}, \theta_{13}, \delta) \sin^2 \left( \frac{\Delta m_{ij}^2 L}{2E} \right).$$

- $X_{\alpha\beta}$  is a function of the elements of  $U_{PMNS}$ .  
For example,  $X_{\mu\tau} = \sin^2 2\theta_{23}$ .
- $L$  is the distance travelled by the  $\nu$  - the 'baseline'.
- $E$  is the  $\nu$  energy.
- $\Delta m_{ij}^2 = m_i^2 - m_j^2$  ( $i, j = 1, 2, 3$ ).

# Oscillation parameters

So  $\nu$  oscillations depend upon:

- 3 mixing angles -  $\theta_{12}$ ,  $\theta_{23}$ , and  $\theta_{13}$ .
- 1 CP violating phase -  $\delta$ .
- 3 mass-squared differences -

$$\Delta m_{21}^2 = \Delta m_S^2,$$

$$\Delta m_{31}^2 \simeq \Delta m_{32}^2 = \Delta m_A^2.$$

There can be **CP violation in the leptonic sector** if all 3 mixing angles are non-zero.

We know that all  $\Delta m^2$ 's  $\neq 0 \Rightarrow$  At least two  $\nu$  masses  $\neq 0$ .

# $\nu$ oscillation experiments

These parameters are measured by  $\nu$  oscillation experiments.

$\nu$  oscillation experiments have three components:

$\nu$  beam  $\rightarrow$  Baseline (L)  $\rightarrow$  Detector



The NuMI beam.  
[lbne.fnal.gov/](http://lbne.fnal.gov/)



The MINOS far detector.  
MINOS

# Designing a $\nu$ oscillation experiment

Different channels give us sensitivity to different parameters, as do different values of  $L$  and  $E$ :

- Because  $\Delta m_S^2 \ll \Delta m_A^2$ , there are 2 distinct oscillation frequencies.
- You can tune your experiment so that either

$$\frac{\Delta m_A^2 L}{2E} \sim 1 \quad \text{or} \quad \frac{\Delta m_S^2 L}{2E} \sim 1.$$

- Hence we can choose different values of  $L/E$  and have both short-baseline and long-baseline experiments.

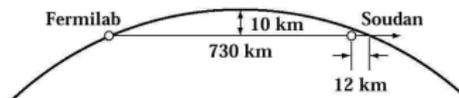
# Short and long-baseline experiments

- **Short-baseline** experiments refer to those with a baseline of  $\sim 1$  km.

Example: CHOOZ.

- **Long-baseline** experiments are those with baselines  $\gtrsim 100$  km.

Example: MINOS.



The 735 km MINOS  
baseline.

[www.hep.ucl.ac.uk/minos/](http://www.hep.ucl.ac.uk/minos/)

# An example of a SBL experiment: CHOOZ



<http://phototheque.in2p3.fr>

- The **CHOOZ** experiment looked for  $\bar{\nu}_e \rightarrow \bar{\nu}_e$ .
- Nuclear reactors provided  $\bar{\nu}_e$  with  $E \sim 3$  MeV.
- A detector was built at  $L \sim 1$  km.

$$\Rightarrow \frac{\Delta m_{A}^2 L}{4E} \sim 1 \quad \frac{\Delta m_{S}^2 L}{2E} \sim 0.03.$$

$$\Rightarrow P_{\bar{\nu}_e \rightarrow \bar{\nu}_e} \simeq 1 - \sin^2(2\theta_{13}) \sin^2\left(\frac{\Delta m_{A}^2 L}{4E}\right).$$

# Current knowledge of mixing parameters

The most recent limits obtained by both short and long-baseline experiments can be found in

M. C. Gonzalez-Garcia, M. Maltoni and J. Salvado, arXiv:1001.4524.

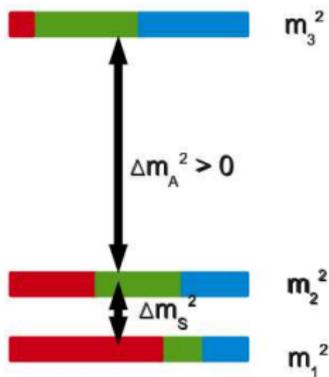
Basically, this is what we know:

- $\theta_{13} \approx 0$        $\theta_{12} \approx 35^\circ$        $\theta_{23} \approx 45^\circ$
- $|\Delta m_{31}^2| \sim |\Delta m_{32}^2| = |\Delta m_A^2| \approx 2.4 \times 10^{-3} \text{ eV}^2$
- $\Delta m_{21}^2 = \Delta m_S^2 \approx 7.6 \times 10^{-5} \text{ eV}^2 \Rightarrow \Delta m_S^2 \ll |\Delta m_A^2|$ .
- $\delta$  unknown.

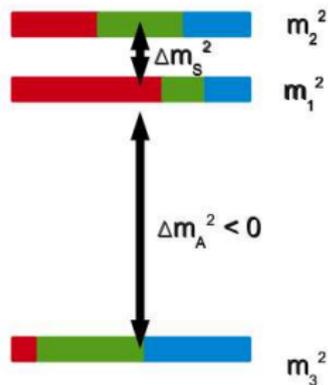
# Current knowledge summarised



Normal  
ordering



Inverted  
ordering

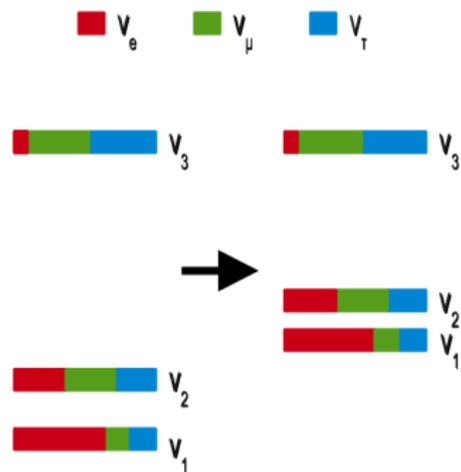


The MSW (Mikheyev-Smirnov-Wolfenstein) effect is also known as the **matter effect**.

L. Wolfenstein, 'Neutrino oscillations in matter', Phys. Rev. D **17**, 2369-2374 (1978).

- $\nu$ 's interact with matter via neutral-current scattering.
- But  $\nu_e$ 's also interact via charged-current scattering  
 $\Rightarrow \nu_e$ 's get 'heavier' in matter.
- There isn't much  $\nu_e$  in  $\nu_3$  so  $\nu_3$  isn't affected.
- But  $\nu_1$  and  $\nu_2$  get heavier.
- See picture on next slide...

# $\nu$ mixing in matter



- For **normal ordering** (pictured):  
 $\Delta m_A^2$  gets smaller  $\Rightarrow$   
**oscillations enhanced.**
- For **inverted ordering**:  
 $\Delta m_A^2$  gets larger  $\Rightarrow$   
**oscillations suppressed.**
- Vice versa for  $\bar{\nu}$ .

Thus, **matter effects** enable us to determine the  $\nu$  **mass ordering**.

- The matter effect is a **cumulative effect**.
- So the more matter there is, the larger the effect.
- Future long-baseline experiment will exploit this:

Current baselines are  $\sim 100$ 's of km. Future baselines may be  $\sim 1000$ 's of km, when matter effects become significant.

## Aside: mass ordering vs mass hierarchy

The **mass hierarchy** refers to the **hierarchy of the  $\nu$  masses**:

- **Normal hierarchy NH** -  $m_1 \simeq m_2 \ll m_3$
- **Inverted hierarchy IH** -  $m_3 \ll m_1 \simeq m_2$
- **Quasi-degenerate QD** -  $m_1 \simeq m_2 \simeq m_3$ .

The **mass ordering** refers to the **ordering of the  $\nu$  masses**:

- **Normal ordering NO** -  $m_1 < m_2 < m_3$
- **Inverted ordering IO** -  $m_3 < m_1 < m_2$ .

**Oscillation experiments** can tell us about the **mass ordering** but not about the mass hierarchy (no information about the **absolute scale of  $\nu$  masses**).

# Aims of future oscillation experiments

The goals of future  $\nu$  oscillation experiments are to measure the unknown oscillation parameters:

- $\theta_{13}$ 
  - symmetries
  - possibility for CPV if  $\theta_{13} \neq 0$
  - value dictates how to optimise experiment (see later).
- the CP violating phase,  $\delta$ 
  - BAU, baryogenesis via leptogenesis?
- determine the  $\nu$  mass ordering (normal or inverted)
  - need long-baseline experiments.

We would also like to look for **non-standard physics**.

# Future long-baseline $\nu$ experiments

Future experiments will have to study **appearance channels** ( $\nu_\alpha \rightarrow \nu_{\alpha \neq \beta}$ ).

Experiments which will be able to do this are **superbeams**,  **$\beta$ -beams** and **neutrino factories**.

- **Superbeams** e.g. T2K are more powerful versions of conventional  $\nu$  beams:

Beam produced from  $\pi^\pm$  decay  $\Rightarrow$  contains  $\nu_\mu$  with some  $\nu_e$  contamination.

- **$\beta$ -beams**:

Beam produced from decay of radioactive ions  $\Rightarrow$  a pure  $\nu_e$  or  $\bar{\nu}_e$  beam.

# A neutrino factory

A **neutrino factory** is considered to be the **ultimate  $\nu$  experiment!**

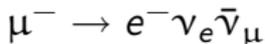
- 7500 km baseline  $\Rightarrow$  guaranteed sensitivity to the mass ordering.
- The **magic baseline** has 'magic' properties (more later...).
- Access to **multiple oscillation channels**.



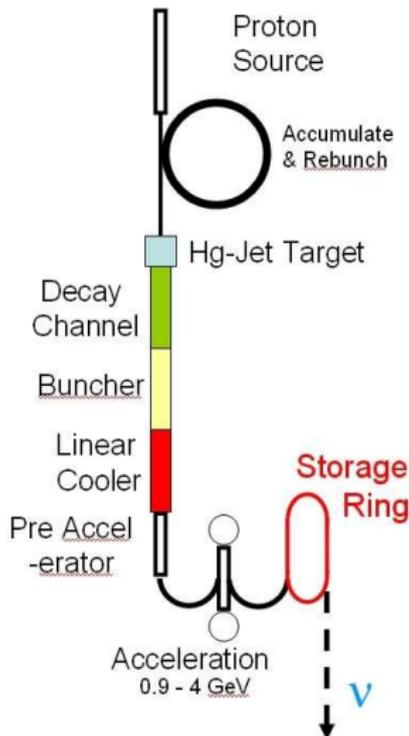
# Brief overview of a neutrino factory

A **neutrino factory** produces a very **pure beam of  $\nu_\mu$  and  $\bar{\nu}_e$**  with a **precisely known flux**.

- Create an intense source of muons.
- Accelerate the muons.
- Inject into a storage ring where they decay:



- Place a detector far away.
- Look at the **disappearance** ( $\bar{\nu}_\mu \rightarrow \bar{\nu}_\mu$ ) and **appearance** ( $\nu_e \rightarrow \nu_\mu$ ) channels.



# $\nu$ oscillations at a $\nu$ factory

- A  $\nu$  factory will see the 'golden channel' ( $\nu_e \rightarrow \nu_\mu$ ):

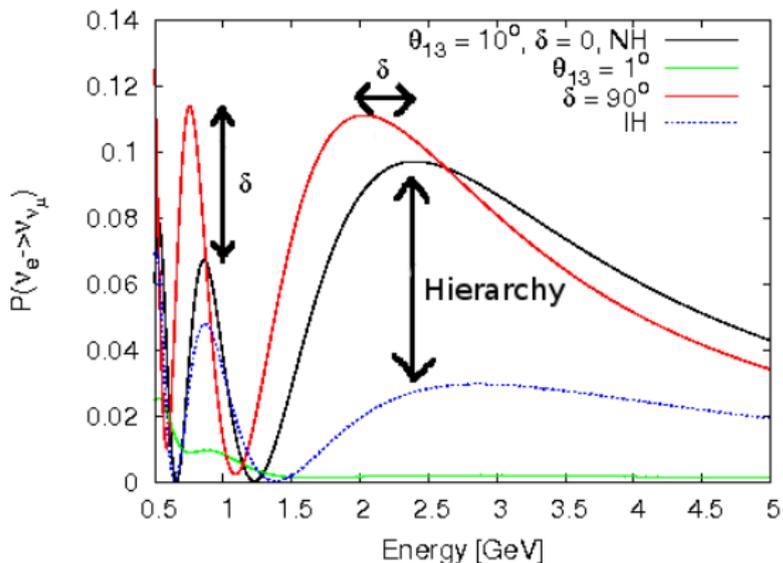
A. Cervera, A. Donini, M. B. Gavela, J. J. Gomez Cadenas, P. Hernandez, O. Mena and S. Rigolin, Nucl. Phys. B **579**, 17 (2000).

$$\begin{aligned} P_{\nu_e \rightarrow \nu_\mu} &= s_{213}^2 s_{23}^2 \sin^2 \left( \frac{\Delta m_{31}^2 L}{4E} - \frac{AL}{2} \right) \\ &+ s_{213} \alpha s_{212} s_{223} \frac{\Delta m_{31}^2 L}{2EA} \sin \left( \frac{AL}{2} \right) \sin \left( \frac{\Delta m_{31}^2 L}{4E} - \frac{AL}{2} \right) \times \\ &\quad \cos \left( \delta - \frac{\Delta m_{31}^2 L}{4E} \right) \\ &+ \alpha^2 c_{23}^2 s_{212}^2 \left( \frac{\Delta m_{31}^2 L}{2EA} \right)^2 \sin^2 \left( \frac{AL}{2} \right). \end{aligned}$$

where  $A$  is the matter potential.

- Information on all the parameters we want to measure.
- Extract parameters by looking at the oscillation spectrum.

# Optimising an experiment for standard oscillations



- $\theta_{13}$  controls the amplitude of the oscillation  $\Rightarrow$  high statistics.
- CP violation is a low energy effect  $\Rightarrow$  detector with low energy threshold.
- Hierarchy determined at high energy  $\Rightarrow$  long baseline.

# The degeneracy problem

The spectrum is very complicated!

⇒ We have a problem with **degeneracies**:

- Data can be fitted to different combinations of  $(\theta_{13}, \delta, \text{sign}(\Delta m_A^2))$ .
- From a single measurement, we cannot tell which is the true solution (see next slide)

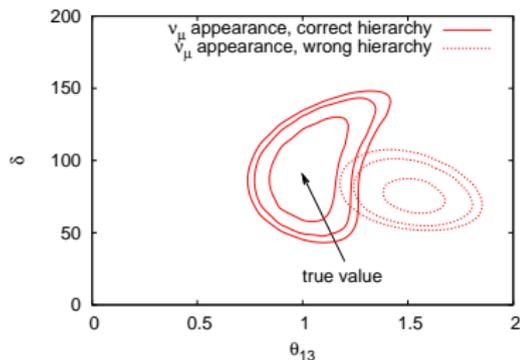
. ⇒ This severely weakens the precision of measurements.

**Possible solutions:**

- Combine information from **complementary channels**.
- Use a **magic baseline**.

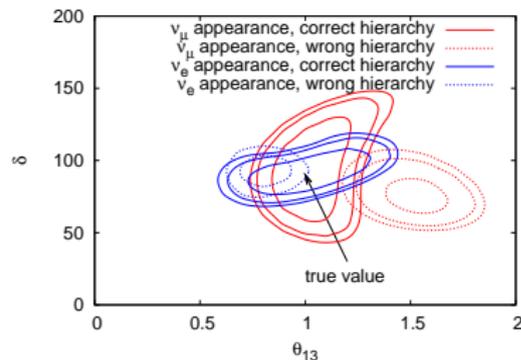
# Using complementary channels to resolve degeneracies

Only  $\nu_{\mu}$  appearance channel:



GLoBES

$\nu_{\mu}$  and  $\nu_e$  appearance channels:



The degenerate solutions appear in different regions of parameter space for each channel.

Thus we can eliminate the fake solutions by combining appropriate channels.

# Using the magic baseline to resolve degeneracies

- Recalling our oscillation probability, we find that if we set:

$$\sin\left(\frac{AL}{2}\right) = 0 \Rightarrow \frac{AL}{2} = \pi \Rightarrow L \sim 7500\text{km}$$

then our probability reduces simply to

$$P_{\nu_e \rightarrow \nu_\mu} = s_{213}^2 s_{23}^2 \sin^2\left(\frac{\Delta m_{31}^2 L}{4E} - \pi\right).$$

- Hence we get rid of the CP and solar terms, and only have to deal with  $\theta_{13}$  and  $\text{sign}(\Delta m_{31}^2)$ .
- We then use a second detector at  $\sim 4000$  km to measure the full oscillation probability, including CPV effects.

# Neutrino factory: one size fits all...?

- A **high energy** ( $\sim 25$  GeV) and a **long baseline** ( $\sim 7500$  km) guarantees sensitivity to **the mass ordering**.
- But is a high energy and long-baseline appropriate for **all** scenarios?
- We know that the **phenomenology at these experiments** will depend strongly on the value of  $\theta_{13}$ .

But so far we have only a weak bound:  $\theta_{13} < 13^\circ$  ( $3\sigma$ ).

- **Why is this a problem?**

# $\theta_{13}$ dependence of oscillation probability

Let's go back to our oscillation probability:

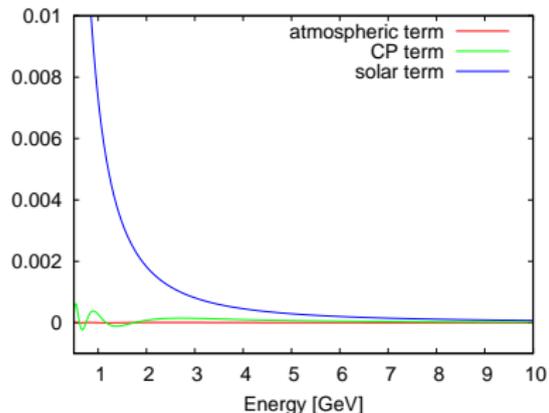
$$\begin{aligned} P_{\nu_e \nu_\mu} &= s_{213}^2 s_{23}^2 \sin^2\left(\frac{\Delta m_{31}^2 L}{4E} - \frac{AL}{2}\right) \\ &+ s_{213} \alpha s_{212} s_{223} \frac{\Delta m_{31}^2 L}{2EA} \sin\left(\frac{AL}{2}\right) \sin\left(\frac{\Delta m_{31}^2 L}{4E} - \frac{AL}{2}\right) \times \cos\left(\delta - \frac{\Delta m_{31}^2 L}{4E}\right) \\ &+ \alpha^2 c_{23}^2 s_{212}^2 \left(\frac{\Delta m_{31}^2 L}{2EA}\right)^2 \sin^2\left(\frac{AL}{2}\right). \end{aligned}$$

- The **atmospheric term** contains information on  $\theta_{13}$  and the mass ordering.
- The **CP term** contains information on  $\theta_{13}$ ,  $\delta$  and the mass ordering.
- The **solar term** doesn't tell us anything interesting.

# $\theta_{13}$ dependence of oscillation spectrum

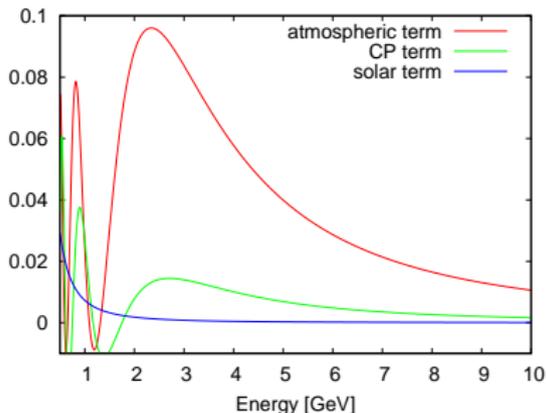
This is how each of the terms vary with the value of  $\theta_{13}$ :

$\theta_{13} = 0.1^\circ$



GLoBES 3.0

$\theta_{13} = 10^\circ$



GLoBES 3.0

# Solar and atmospheric regimes

- For  $\theta_{13} \lesssim 1^\circ$  - **solar regime** - the **solar term** is dominant.

⇒ A long baseline is the only way to determine the mass ordering.

- For  $\theta_{13} \gtrsim 1^\circ$  - **atmospheric regime** - the **atmospheric** and **CP** terms are dominant, so measurements are easier.

But we can still use a  $\nu$  factory, can't we?

# Matter effects fake CP violation

Long-baseline = strong matter effects.

## What's the problem?

- The earth is not CP symmetric i.e. there's only matter and no anti-matter.
- So our beam  $\nu$ 's only interact with matter.
- Then how do we know if CP violation occurs because  $\delta \neq 0$ ,  $\pi$ , or just because the earth is CP-asymmetric?

For large  $\theta_{13}$ , matter effects and CPV at a  $\nu$  factory become difficult to distinguish.

# Neutrino factory: high energy vs low energy

- But if  $\theta_{13}$  is large, we can determine the mass ordering using a shorter baseline to minimise matter effects.

⇒ Consider a **low energy neutrino factory** (LENF).

S. Geer, O. Mena and S. Pascoli, Phys. Rev. D **75**, 093001 (2007); A. D. Bross, M. Ellis, S. Geer, O.

Mena and S. Pascoli, Phys. Rev. D **77**, 093012 (2008).

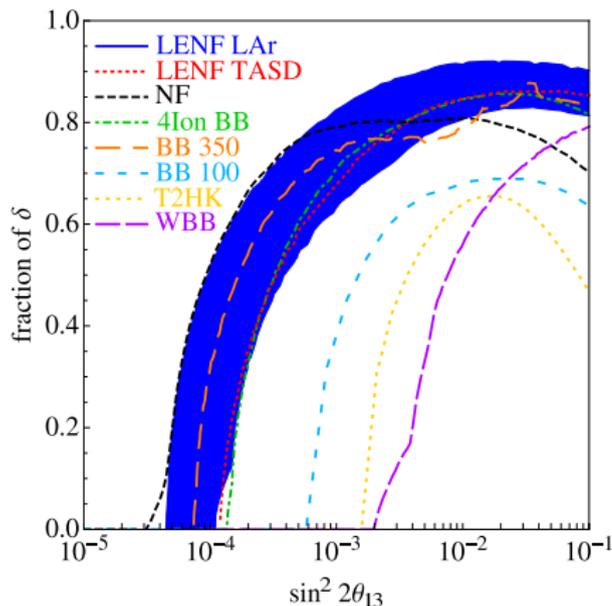
- If appropriately optimised, the low energy neutrino factory outperforms the other options...

A. Bross, M. Ellis, E. Fernández-Martínez, S. Geer, TL, O. Mena and S. Pascoli, arXiv: 0911.3776.

... and lower energy = lower cost ;-)

# LENF sensitivity to CPV

CP violation discovery potential:



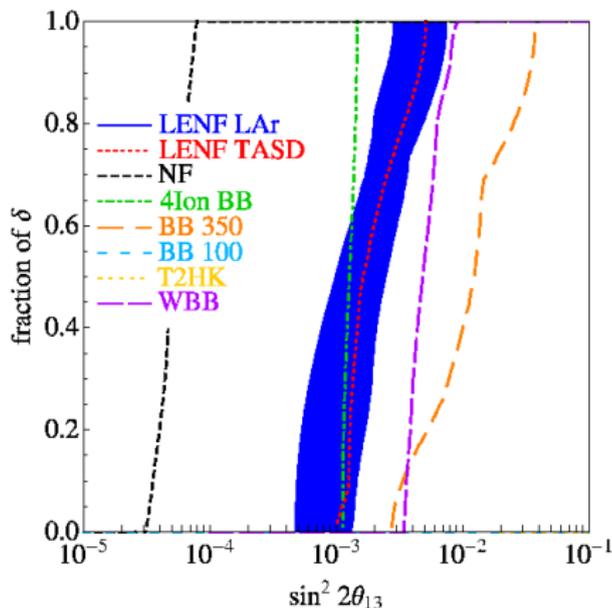
arXiv: 0911.3776

GLoBES 3.0

- The **high energy neutrino factory (NF)** was designed for the scenario that  $\theta_{13}$  is **very small**.
- But the **low energy neutrino factory (LENF)** performs better if  $\theta_{13}$  is **large**.

# LENF sensitivity to the mass ordering

Sensitivity to the mass ordering:



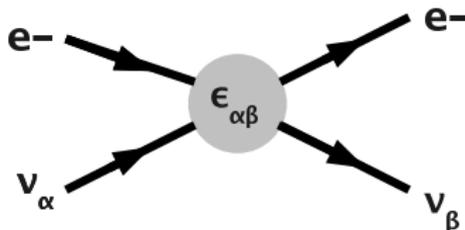
However, the **low energy neutrino factory (LENF)** is only sensitive to the mass ordering for large  $\theta_{13}$ .

# New physics at a $\nu$ factory

We would also like to search for new physics with a  $\nu$  factory, for example **non-standard interactions** (NSI's).

- NSI's are effective 4-point flavour-changing interactions.
- NSI's can be parameterized as  $\epsilon_{\alpha\beta}$  (model-independent) which describe the rate of the transition  $\nu_{\alpha} \rightarrow \nu_{\beta}$ .

T. Ota, J. Sato and N. Yamashita, Phys. Rev. D **65**, 093015 (2002).



# NSI's at long-baseline experiments

- $\nu$  oscillation experiments are particularly powerful tools for detecting NSI's because a  $\nu$  transition can occur via oscillation, or NSI:

$$\text{Rate} = \left| \nu_{\alpha} \xrightarrow{\text{OSC}} \nu_{\beta} + \nu_{\alpha} \xrightarrow{\frac{\text{NSI}}{\epsilon_{\alpha\beta}}} \nu_{\beta} \right|^2.$$

- Hence there is an **interference term** which is **linear**, rather than quadratic, in  $\epsilon_{\alpha\beta}$ .

T. Ota, J. Sato and N. Yamashita, Phys. Rev. D **65**, 093015 (2002).

# NSI's from a specific model

Here's an example of a specific model which predicts NSI's:

There is a class of phenomenologically interesting models which explain light  $\nu$  masses **and** predict the existence of low energy observables -

'Minimal flavour seesaw models'.

B. Gavela, T. Hambye, D. Hernández and P. Hernández, JHEP **0909**, 038 (2009).

# Minimal flavour seesaw models: brief overview

In order that the model **does not prevent the existence of observable FC interactions**, there are **2 scales** built in:

- A lepton-number violating scale,  $\Lambda_{LN}$ , which sets the mass scale for the SM neutrinos (seesaw scale).
- A lepton-flavour violating scale,  $\Lambda_{FL}$ , which sets the mass scale for the additional heavy neutrinos.

with  $\Lambda_{FL} \ll \Lambda_{LN}$ .

This model makes predictions for flavour changing interactions  $\ell_\alpha \rightarrow \ell_\beta$  and  $\nu_\alpha \rightarrow \nu_\beta$ .

# Basic mechanism of the model

$$\begin{aligned} L &= L_{SM} + i\bar{N}\gamma_\mu\partial^\mu N + i\bar{N}'\gamma_\mu\partial^\mu N' \\ &- [Y_N^b\bar{N}\tilde{\phi}^\dagger\ell_L^b + \frac{\Lambda}{2}(\bar{N}'N^c + \bar{N}N'^c) + h.c.] \end{aligned}$$

- Start with a pair of Weyl fields,  $N$  (lepton no. = +1) and  $N'$  (lepton no. = -1).
- Species with opposite LN pair up  $\Rightarrow$  Dirac field.
- LFV interactions  $\Rightarrow$  Dirac masses for heavy  $\nu$ 's.
- LNV interactions  $\Rightarrow$  Masses for SM  $\nu$ 's.

# The PMNS matrix revisited

- The inclusion of NSI's means that we should consider a **non-unitary mixing matrix**.
- Obviously the full, high-energy matrix,  $U_{PMNS}$ , is unitary, but at our low-energy experiments we see an approximation,  $N$ :

$$(NN^\dagger)_{\alpha\beta} = \delta_{\alpha\beta} - \varepsilon_{\alpha\beta}.$$

S. Antusch, C. Biggio, E. Fernández-Martínez, M. B. Gavela and J. López-Pavón, JHEP 10, 084 (2006).

- In our model:

$$\varepsilon_{\alpha\beta} = \frac{v^2 y^2}{\Lambda_{FL}^2} Y_\alpha^* Y_\beta$$

where  $y$  and  $\Lambda_{FL}$  are the parameters we want to constrain.

- Which  $\varepsilon_{\alpha\beta}$ 's can we measure?

# NSI's at a low energy neutrino factory

Well, for example, the LENF has leading order sensitivity to the NSI parameters  $\epsilon_{e\mu} e^i \phi_{e\mu}$  and  $\epsilon_{e\tau} e^i \phi_{e\tau}$ :

$$\begin{aligned} P_{\nu_e \rightarrow \nu_\mu} &= s_{213}^2 s_{23}^2 \sin^2 \left( \frac{\Delta m_{31}^2 L}{4E} - \frac{AL}{2} \right) \\ &+ s_{213} \alpha s_{212} s_{223} \frac{\Delta m_{31}^2 L}{2EA} \sin \left( \frac{AL}{2} \right) \sin \left( \frac{\Delta m_{31}^2 L}{4E} - \frac{AL}{2} \right) \cos \left( \delta - \frac{\Delta m_{31}^2 L}{4E} \right) \\ &+ \alpha^2 c_{23}^2 s_{212}^2 \left( \frac{\Delta m_{31}^2 L}{2EA} \right)^2 \sin^2 \left( \frac{AL}{2} \right) \\ &- 4 \epsilon_{e\tau} s_{213} c_{23} s_{23}^2 \sin \left( \frac{AL}{2} \right) \sin \left( \frac{\Delta m_{31}^2 L}{4E} - \frac{AL}{2} \right) \cos \left( \delta + \phi_{e\tau} - \frac{\Delta m_{31}^2 L}{4E} \right) \\ &+ 4 \epsilon_{e\tau} \alpha s_{212} c_{23}^2 s_{23} \sin \left( \frac{AL}{2} \right) \sin \left( \frac{\Delta m_{31}^2 L}{4E} - \frac{AL}{2} \right) \cos \left( \phi_{e\tau} + \frac{\Delta m_{31}^2 L}{4E} \right) \\ &+ 4 \epsilon_{e\tau}^2 c_{23}^2 s_{23}^2 \sin^2 \left( \frac{AL}{2} \right) \\ &- 4 \epsilon_{e\mu} s_{213} c_{23}^2 s_{23} \sin \left( \frac{AL}{2} \right) \sin \left( \frac{\Delta m_{31}^2 L}{4E} - \frac{AL}{2} \right) \cos \left( \delta + \phi_{e\mu} - \frac{\Delta m_{31}^2 L}{4E} \right) \\ &- 4 \epsilon_{e\mu} \alpha s_{212} c_{23}^2 s_{23} \sin \left( \frac{AL}{2} \right) \sin \left( \frac{\Delta m_{31}^2 L}{4E} - \frac{AL}{2} \right) \cos \left( \phi_{e\mu} + \frac{\Delta m_{31}^2 L}{4E} \right) \\ &+ 4 \epsilon_{e\mu}^2 c_{23}^2 s_{23}^2 \sin^2 \left( \frac{AL}{2} \right). \end{aligned}$$

# Degeneracies with NSI's

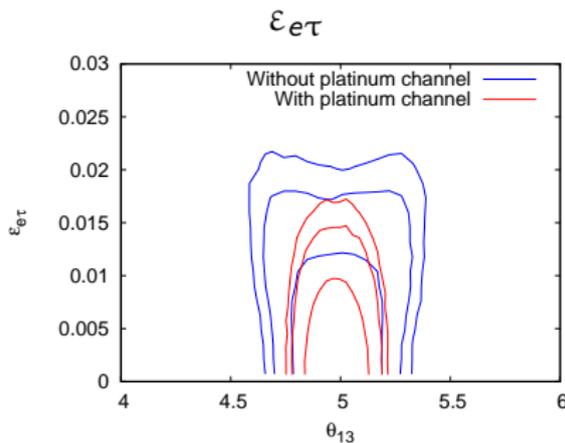
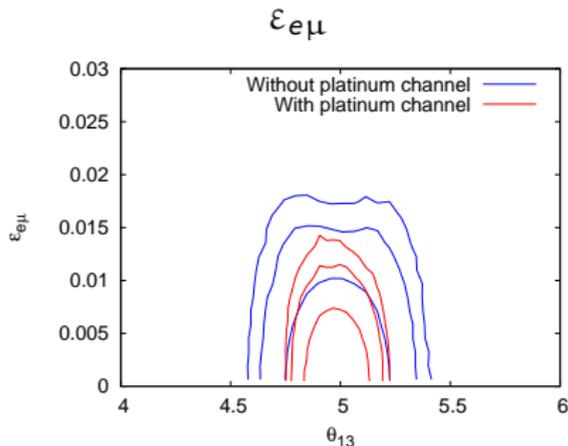
The spectrum just got even more complicated...

- When we include NSI's, the parameter space is vastly increased and so the **degeneracy problem** is magnified.
- Crucially, we must ensure that **NSI's do not degrade our sensitivity to the oscillation parameters**.
- The high-energy  $\nu$  factory is already immune to this problem because of the 'magic baseline'.
- But for the LBNF, we have to find a solution: the addition of the 'platinum channel' ( $\nu_\mu \rightarrow \nu_e$ ) is essential in **maximising the experimental sensitivity to all parameters**.

E. Fernández-Martínez, TL, O. Mena and S. Pascoli.

# Maximising the LENF sensitivity to NSI's

- Simulate  $\varepsilon_{e\mu} = \varepsilon_{e\tau} = 0$  and look at the 68%, 90% and 95% confidence level contours in the  $\theta_{13} - \varepsilon$  plane:



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MonteCUBES

- The sensitivity to both oscillation parameters and NSI's is increased by including the  $\nu_{\mu} \rightarrow \nu_e$  channel.
- We can obtain an upper bound of  $\sim 10^{-2}$ ... Can we do better?

# Near detectors

- So far I've talked about the physics at the **far detector of a neutrino factory**.
- But we can also use a **near detector** ( $L \sim 1$  km)  
  
⇒ no oscillations, only 'zero-distance' effects.
- But why wait for a  $\nu$  factory? We already have existing  $\nu$  beams, so let's build a detector now for one of these beams...

## MINSIS

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The idea: place a  $\nu_\tau$  detector very close (**1 km**) to the  $\nu_\mu$  beam source at Fermilab and look for  $\nu_\mu \rightarrow \nu_\tau$  transitions.

# Discovery potential of near detectors

- A near detector at a  $\nu$  experiment has the advantage of having a very **high event rate**  $\Rightarrow$  high statistics.
- In addition, the  $\nu_{\mu} \rightarrow \nu_{\tau}$  **channel** turns out to have a very **rich sensitivity to NSI's**, and hence is dubbed the



Let's see how a near detector can constrain our MFV model.

# Current bounds on the MFV model

The best bound on this model so far comes from the MEGA experiment, which measured

The MEGA Collaboration, Phys. Rev. Lett. 83, 1521 (1999).

$$Br(\mu^+ \rightarrow e^+ \gamma) \leq 1.2 \times 10^{-11} \quad (90\% \text{ CL})$$

where

$$B(\ell_\alpha \rightarrow \ell_\beta) = \frac{\Gamma(\ell_\alpha \rightarrow \ell_\beta \gamma)}{\Gamma(\ell_\alpha \rightarrow \ell_\beta \nu_\alpha \bar{\nu}_\beta)}.$$

How do we relate this branching ratio to our predictions?

# Bounds from charged lepton experiments

- The NSI's depend on the Yukawa couplings  $Y_\alpha$ ,  $Y_\beta$ , which are functions of the neutrino mixing parameters.
- We need to relate these couplings to the observed branching ratios.
- First we can relate  $NN^\dagger$  to these branching ratios:

S. Antusch, C. Biggio, E. Fernández-Martínez, M. B. Gavela and J. López-Pavón, JHEP 10, 084.

$$\frac{|(NN^\dagger)_{\alpha\beta}|^2}{(NN^\dagger)_{\alpha\alpha}(NN^\dagger)_{\beta\beta}} = \frac{\Gamma(\ell_\alpha \rightarrow \ell_\beta \gamma)}{\Gamma(\ell_\alpha \rightarrow \ell_\alpha \nu_\beta \bar{\nu}_\beta)} \frac{96\pi}{100\alpha}$$

and thus obtain an upper bound on  $|(NN^\dagger)_{\alpha\beta}|^2$ .

# Any holes anywhere?

- So we can deduce that:

$$\frac{y^2 v^2}{\Lambda_{FL}^2} < \frac{\text{Bound on } (NN^\dagger)_{\alpha\beta}}{|Y_\alpha^* Y_\beta|}$$

where  $|Y_\alpha^* Y_\beta|$  is predicted theoretically by the model.

- However the Yukawa couplings depend strongly upon the CP violating Dirac phase,  $\delta$ , and the Majorana phase,  $\alpha$ .
- Neither of these phases is known at present!
- Therefore we can only obtain predictions as a function of  $\delta$  and  $\alpha$ .

- The model predicts that

$$Y_e = e^{i\delta} s_{13} + e^{-i(\alpha-\pi/2)} s_{12} \left( \frac{|\Delta m_{21}^2|}{|\Delta m_{31}^2|} \right)^{1/4} .$$

- Hence for some values of  $\delta$  and  $\alpha$ ,  $Y_e \ll 1$

$\Rightarrow$  The interaction rates for transitions involving electrons become very small and we lose sensitivity in this region.

**Solution:** look at a different channel without electrons e.g.  $\mu \rightarrow \tau$ .

- Neutrino transitions are related to NSI's via:

S. Antusch, C. Biggio, E. Fernández-Martínez, M. B. Gavela and J. López-Pavón, JHEP 10, 084.

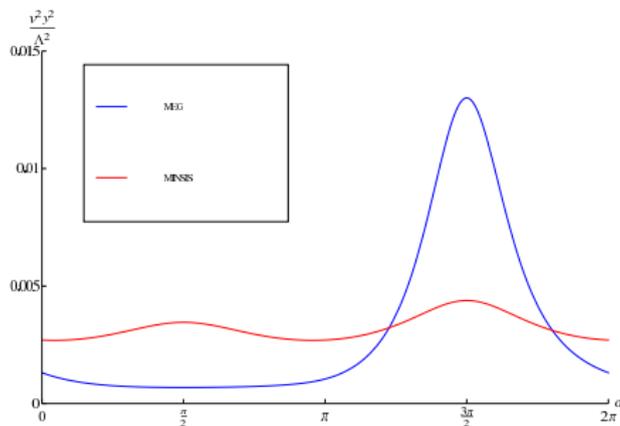
$$P(\nu_\alpha \rightarrow \nu_\beta) = |(NN^\dagger)_{\alpha\beta}|^2$$

- Hence with a (realistic!)  $10^{-6}$  sensitivity to  $P_{\nu_\mu \rightarrow \nu_\tau}$ , we obtain a bound of  $(NN^\dagger)_{\mu\tau} < 1 \times 10^{-3}$ .
- For comparison, the current bound from a lepton experiment comes from the limit:

$$Br(\tau \rightarrow \mu\gamma) < 4.4 \times 10^{-8} \Rightarrow (NN^\dagger)_{\tau\mu} < 4.3 \times 10^{-3}.$$

The BABAR collaboration, Phys. Rev. Lett. 104 021802 (2010).

So **MINSIS** could obtain better sensitivity than **MEGA** in some regions of parameter space:



R. Alonso de Pablo, B. Gavela, TL

MINSIS can be complementary to charged lepton experiments.

# Summary

- Future long-baseline experiments such as **neutrino factories** are being optimised to measure  $\theta_{13}$ ,  $\delta$  and the **mass hierarchy**.
- **Complementary channels** and/ or a **magic baseline** can be used to **resolve degeneracies** and enhance experimental sensitivity.
- In some scenarios, a **low energy neutrino factory** will out-perform a high energy neutrino factory.
- Long-baseline experiments are powerful tools for **detecting non-standard interactions**.
- **Near detectors** are also good probes of **non-standard interactions**.
- **Neutrino experiments** can be **complementary to charged lepton experiments**.

# Suggested references (1/2)

- **Oscillation parameter update:**

- M. C. Gonzalez-Garcia, M. Maltoni and J. Salvado, arXiv:1001.4524.

- **The MSW effect:**

- L. Wolfenstein, Phys. Rev. D **17**, 2369-2374 (1978).

- **Overview of past, current and future neutrino facilities**  
(and a lot of theory too!):

- [The ISS Physics Working Group], Rept. Prog. Phys. **72**, 106201 (2009), arXiv: 0710.4947 (hep-ph).

- **The low energy neutrino factory:**

- A. Bross, M. Ellis, E. Fernández-Martínez, S. Geer, T. Li, O. Mena and S. Pascoli, arXiv: 0911.3776.

## Suggested references (2/2)

- **NSI's** (theory):

- T. Ota, J. Sato and N. Yamashita, Phys. Rev. D **65**, 093015 (2002), arXiv:hep-ph/0112392;

- S. Antusch, C. Biggio, E. Fernández-Martínez, M. B. Gavela and J. López-Pavón, JHEP **10**, 084 (2006), arXiv:hep-ph/060702;

- S. Antusch, J. P. Baumann and E. Fernández-Martínez, Nucl. Phys. B **810**, 369-388 (2009), arXiv:0807.1003 (hep-ph).

- **MFV model:**

- B. Gavela, T. Hambye, D. Hernández and P. Hernández, JHEP **0909**, 038 (2009), arXiv:0906.1461 (hep-ph).

- **MINSIS:**

- [www-off-axis.fnal.gov/MINSIS/](http://www-off-axis.fnal.gov/MINSIS/).