



Pathways for X-ray Nanometer Focusing

What are the Scientific Opportunities

Anatoly SNIGIREV

ERL :

Beam energy

$$E = 5.3 \text{ GeV}$$

"high coherence" mode

current

$$I = 10 \text{ mA}$$

betafunctor

$$\beta = 1 \text{ m}$$

(2.5 m; 12.5 m)

emittance

$$\varepsilon = 0.015 \text{ nm rad}$$

Source size:

(FWHM)

$$\sigma = 4 \text{ } \mu\text{m}$$

$$S = 10 \text{ } \mu\text{m}$$

(esrf 25 x 900 μm^2)

Beam divergence

(FWHM)

$$\sigma' = 4 \text{ } \mu\text{rad}$$

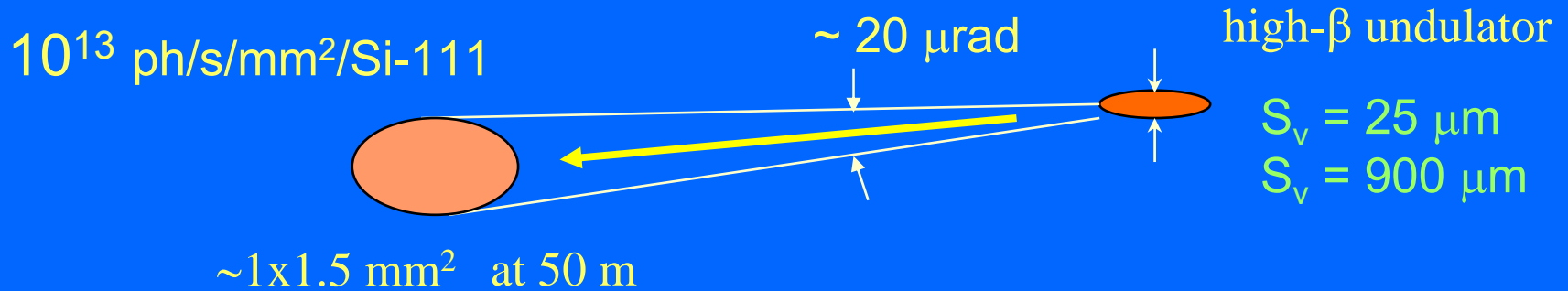
$$S' = 10 \text{ } \mu\text{rad}$$

(esrf 20 x 30 μrad^2)

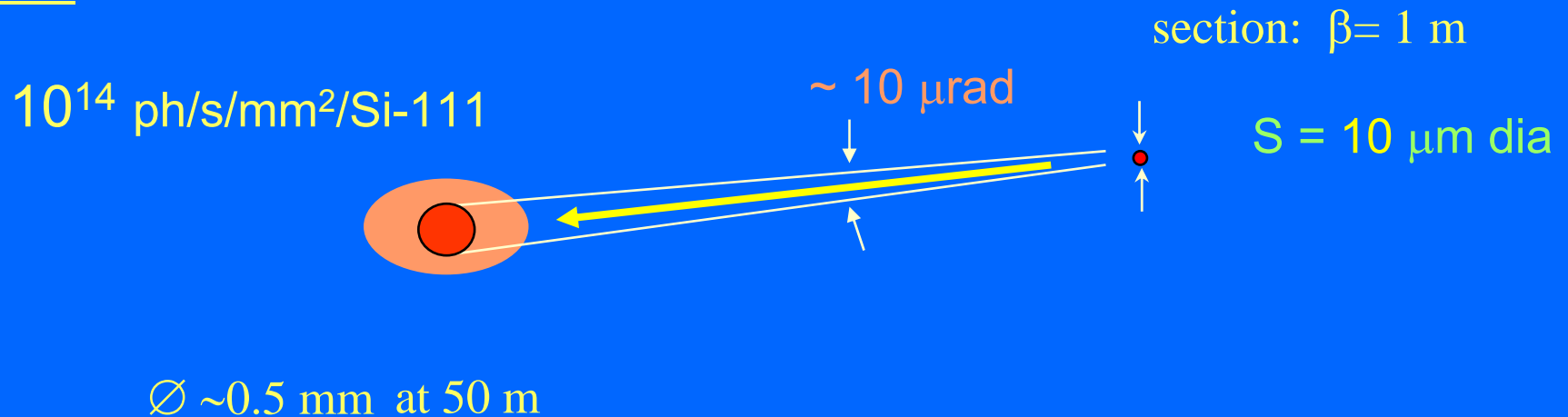
Av. brilliance: $3 \times 10^{22} \text{ ph / (s } 0.1\% \text{ mm}^2 \text{ mrad}^2)$

Undulator X-ray beam (ESRF/ERL)

ESRF 200 mA



ERL 10 mA



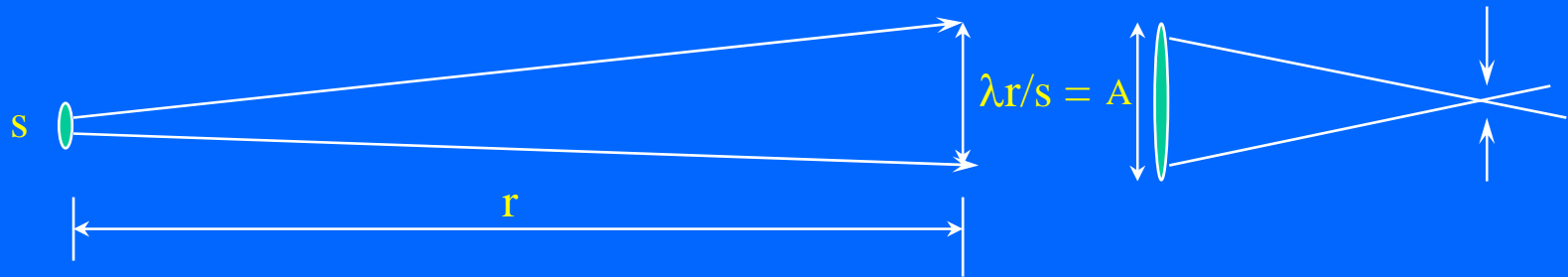
Why do we need a coherent beam for Microoptics?

Transverse coherence \sim Aperture of the optics

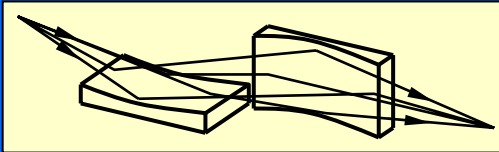
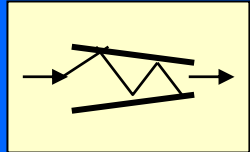
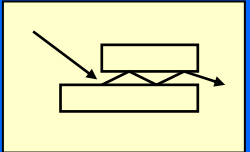
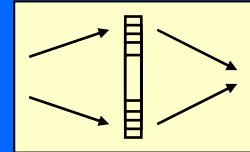
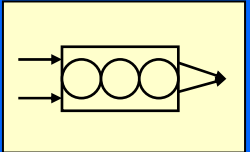
- Diffraction limited focusing at nm level
- Coherent secondary source - coherence enhancement

Aperture (acceptance) of nanooptics is about 50 -500 μm
resolution \sim 10 – 100 nm

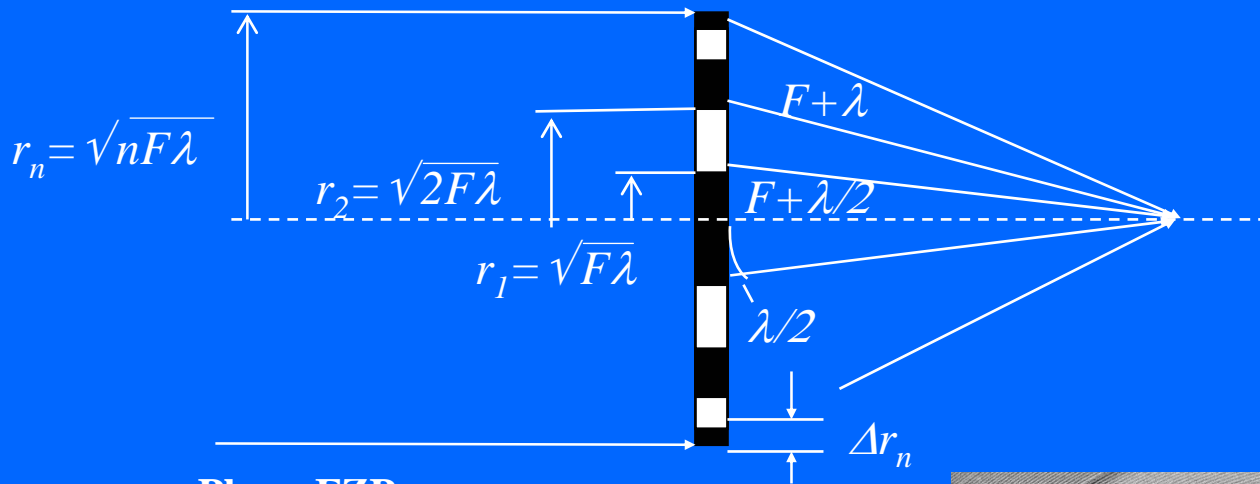
for ERL : beamsize 500 μm dia at 50 m



Focusing Optics for Hard X-rays: 6 - 60 (200) keV

	<i>reflective</i>			<i>diffractive</i>	<i>refractive</i>	
	Kirkpatrick Baez systems		Capillaries	Waveguides	Fresnel Zone plates	Refractive lenses
	mirrors Kirkpatrick Baez, 1948	multilayers Underwood Barbee, 1986	Kreger 1948	Feng et al 1993	Baez 1952	Snigirev et al, 1996
						
Energy	< 30 keV	< 80keV	< 20keV	< 20keV	< 30 keV (80)	<1 MeV
Bandwidth DE/E	w. b.	10 ⁻²	w.b.	10 ⁻³	10 ⁻³	10 ⁻³
resolution	25 nm Spring 8 2006	40 nm Hignette 2005	50 nm Bilderback 1994	40x25 nm² Salditt 2004	20 nm @ 20keV APS, 2006 ~15nm<1keV	50 nm Schroer 2004

Fresnel Zone Plate (FZP)

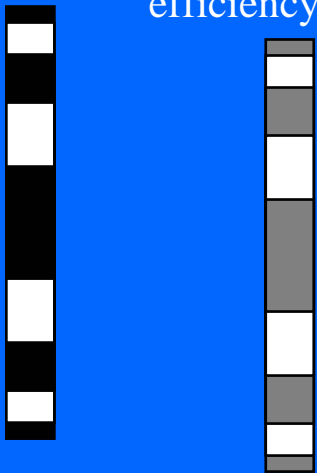


FZP parameters

$A = 100 - 1000 \mu\text{m}$
 $\Delta r_n = 0.05 - 0.3 \mu\text{m}$
 $t_{\text{Si}} = 1 - 10 \mu\text{m}$
 $F = 60 \text{ cm at } 4 - 12 \text{ keV}$
 $\text{flux } 10^{10} \text{ photons/sec}$

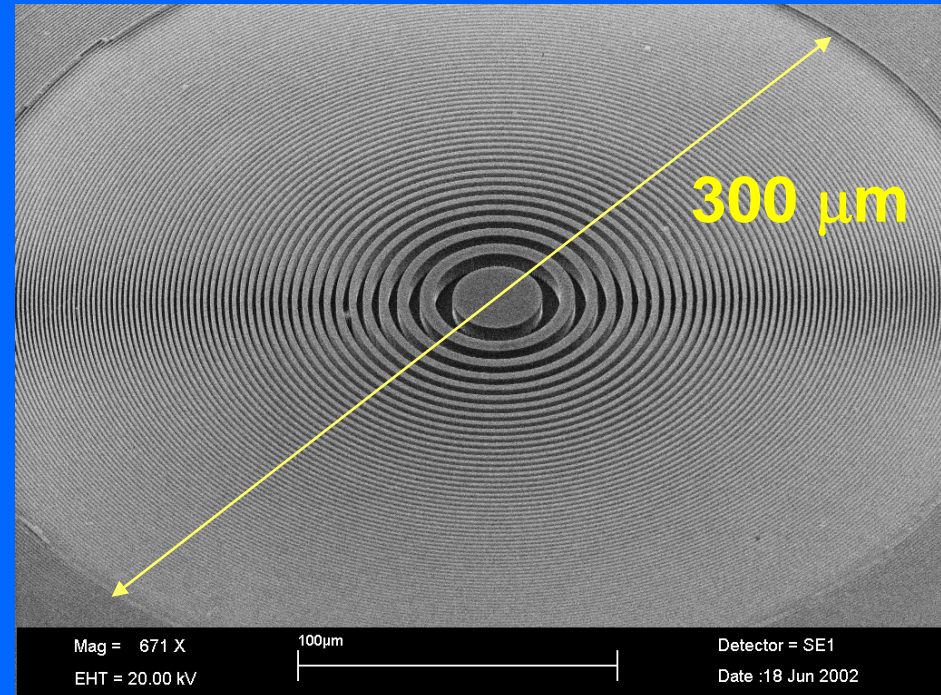
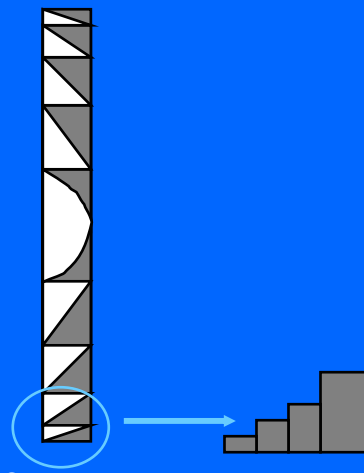
Phase FZP

alternate zones -
 phase shifting
 efficiency $\sim 40\%$



Kinoform FZP

(sawtooth profile)
 efficiency $\sim 70 - 100\%$

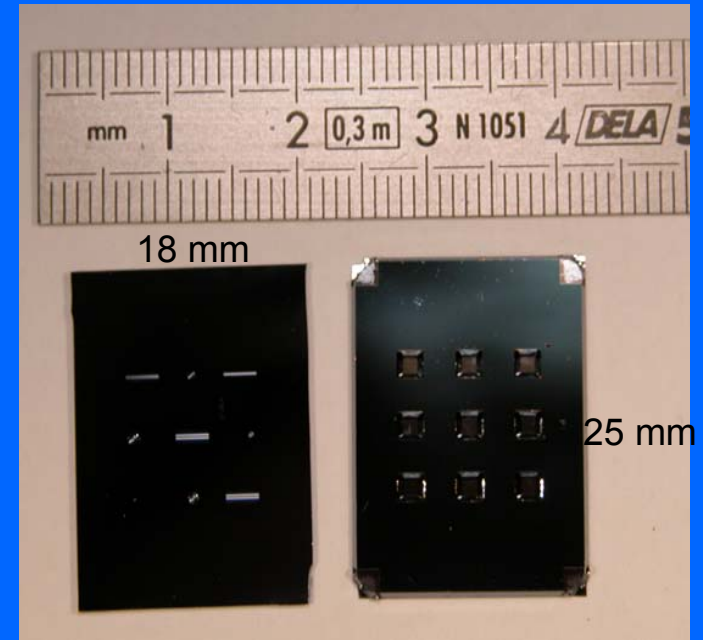
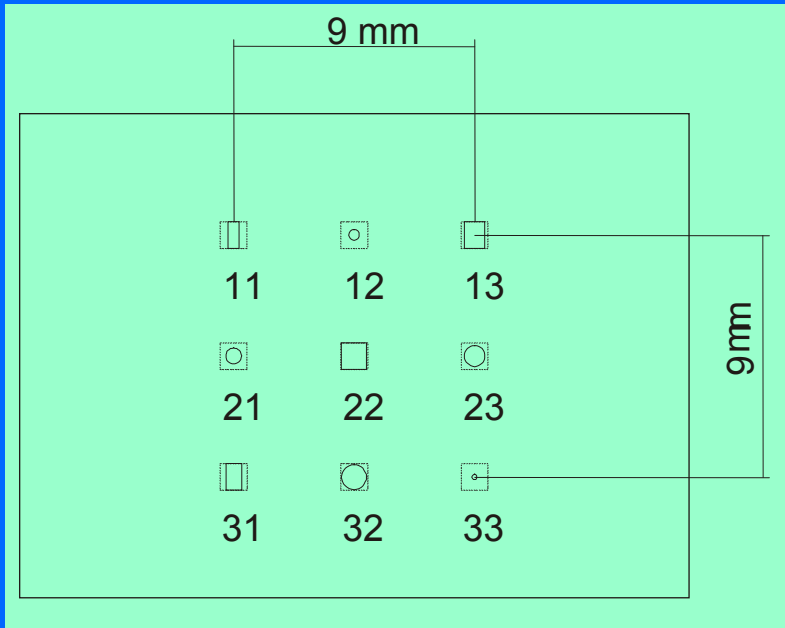


Res. \sim from 500 nm to 50 nm

Amplitude FZP

alternate zones - opaque
 efficiency $\sim 10\%$

FZP Si chip

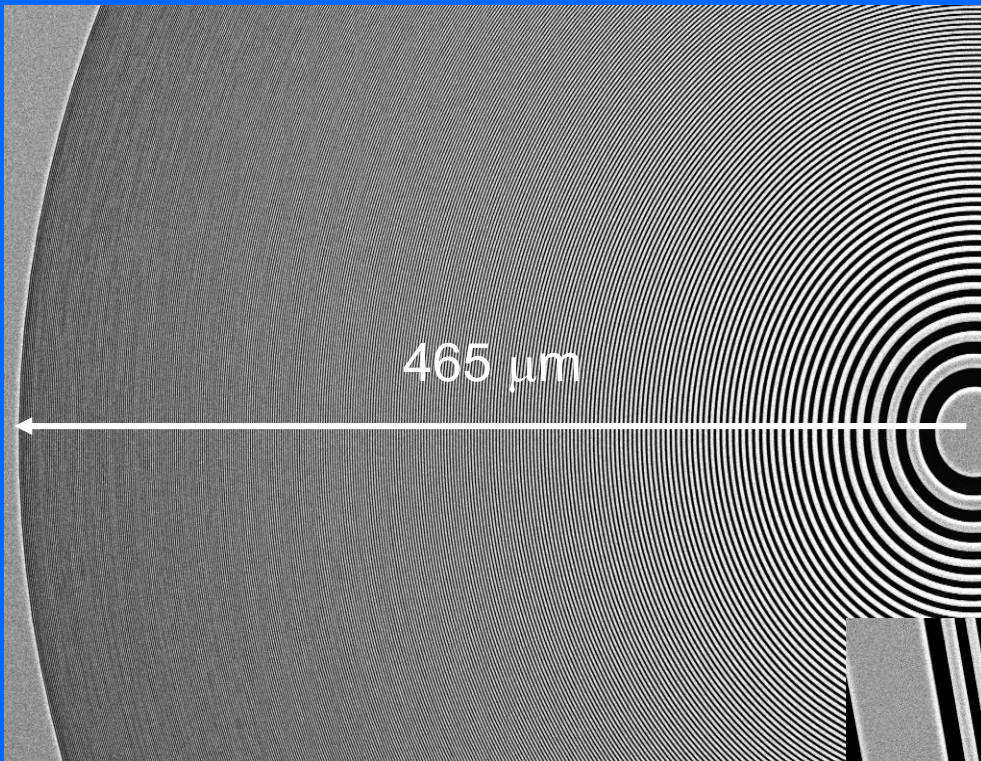


Lens parameters

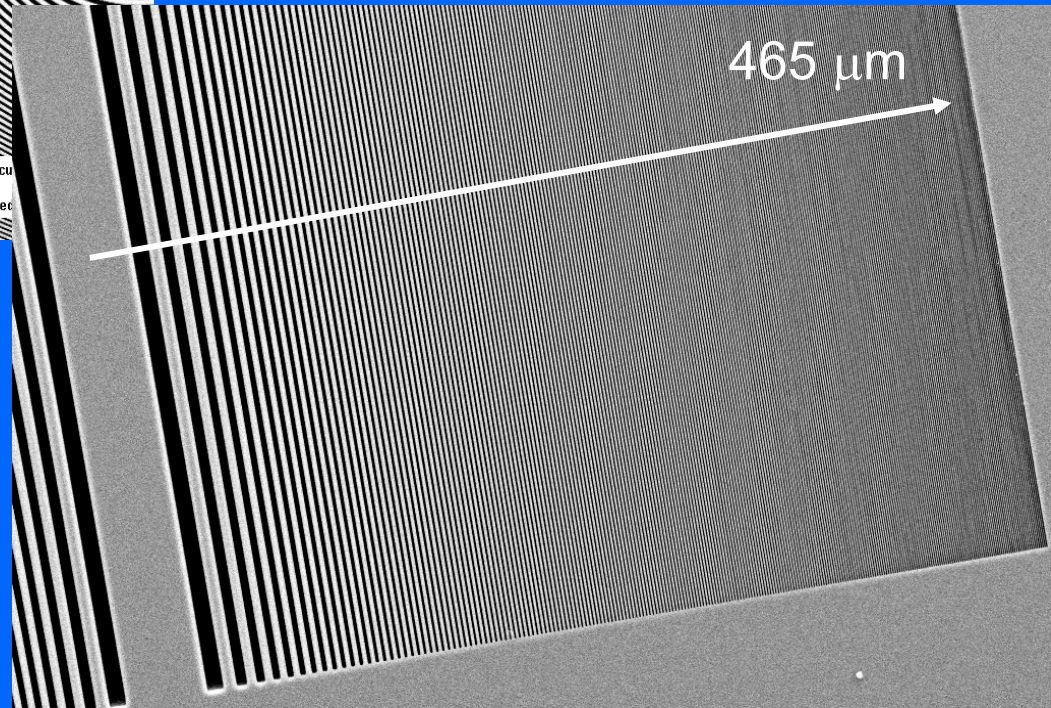
$$A = 2r_n = F\lambda / dr_n$$

DOE type	Focal length, F (cm) at 8 keV	Aperture of DOE, A (μm)	Outermost zone width, dr_n (μm)	Number of zones
33 (circular)	50	$A=194$	0.4	122
11 (linear)	100	$A=387; L=1000$	0.4	242
12 (circular)	100	$A=387$	0.4	242
21 (circular)	150	$A=582$	0.4	364
31 (linear)	150	$A=582; L=1000$	0.4	364
13 (linear)	200	$A=775; L=1000$	0.4	484
23 (circular)	200	$A=775$	0.4	484
22 (linear)	240	$A=930; L=1000$	0.4	582
32 (circular)	240	$A=930$	0.4	582

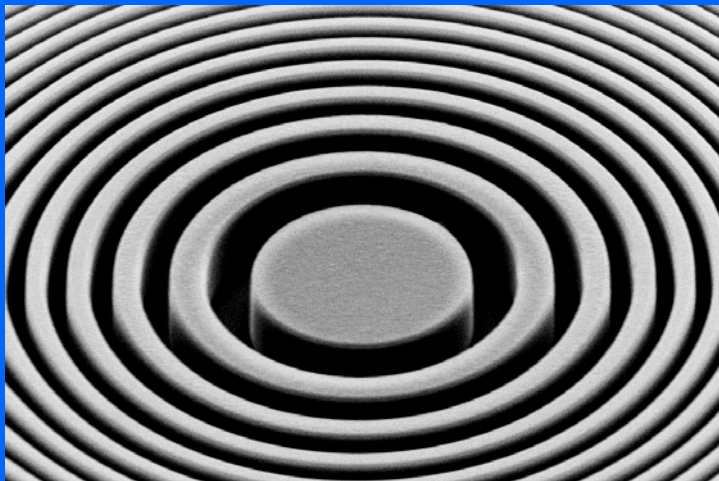
SEM images



LEO **LEO 1530** Mag = 744 X EHT = 20.00 kV Signal A = SE2 Date :14 Sep 2005 Gun Vacuum = 2.15e-009 Torr
Serial No. = LEO 1530-21-90 $20\mu\text{m}^*$ WD = 9 mm Output To = Display/File Time :9:54:20 Noise Reduction = Line Int. Done

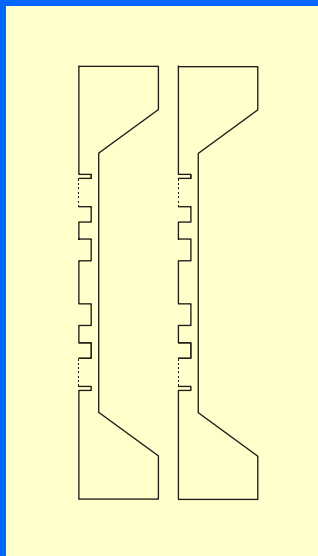


LEO **LEO 1530** Mag = 794 X EHT = 20.00 kV Signal A = SE2 Date :14 Sep 2005 Gun Vacuum = 2.15e-009 Torr
Serial No. = LEO 1530-21-90 $10\mu\text{m}^*$ WD = 9 mm Output To = Display/File Time :10:08:52 Noise Reduction = Line Int. Done

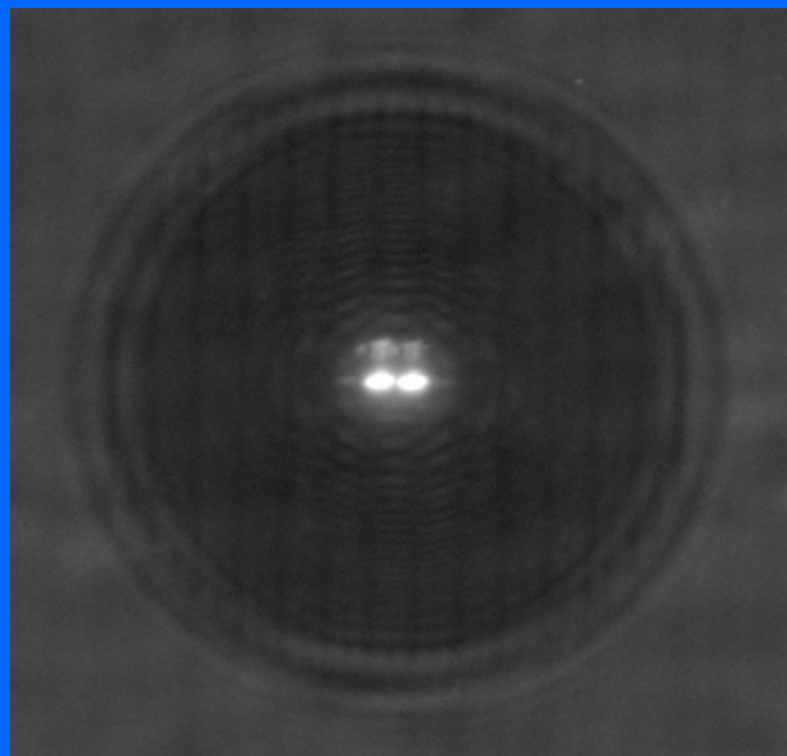
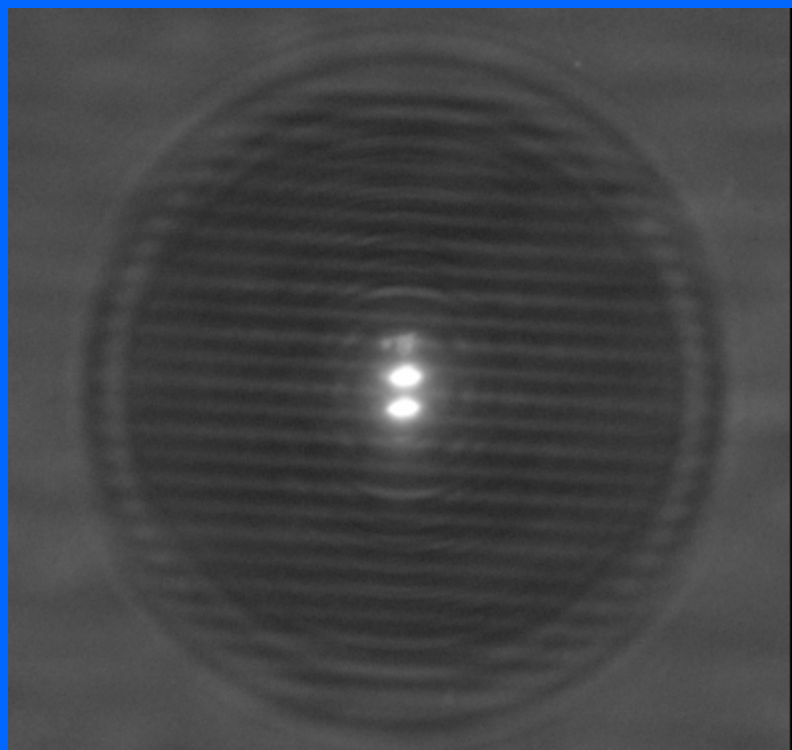


LEO **LEO 1530** Mag = 3,688 X EHT = 20.00 kV Signal A = SE2 Date :19 Nov 2004 Gun Vacuum = 1.32e-009 mBar
Serial No. = LEO 1530-21-90 $10\mu\text{m}$ WD = 7 mm Output To = Display/File Time :15:59:25 Noise Reduction = Line Int. Done

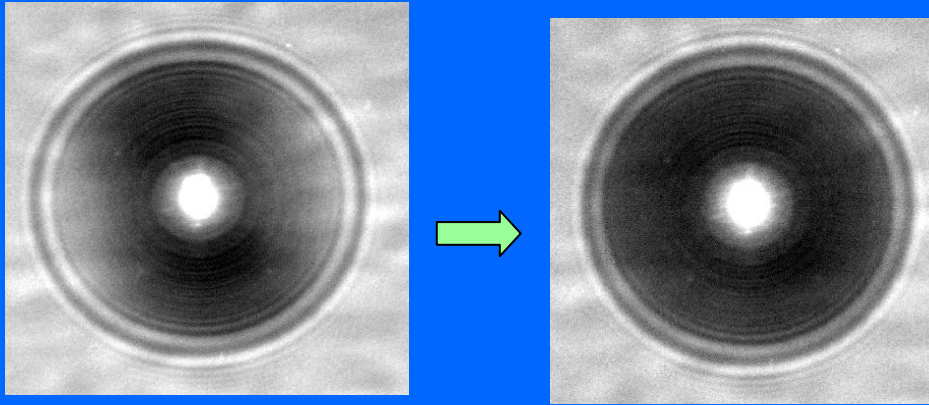
HR XCCD



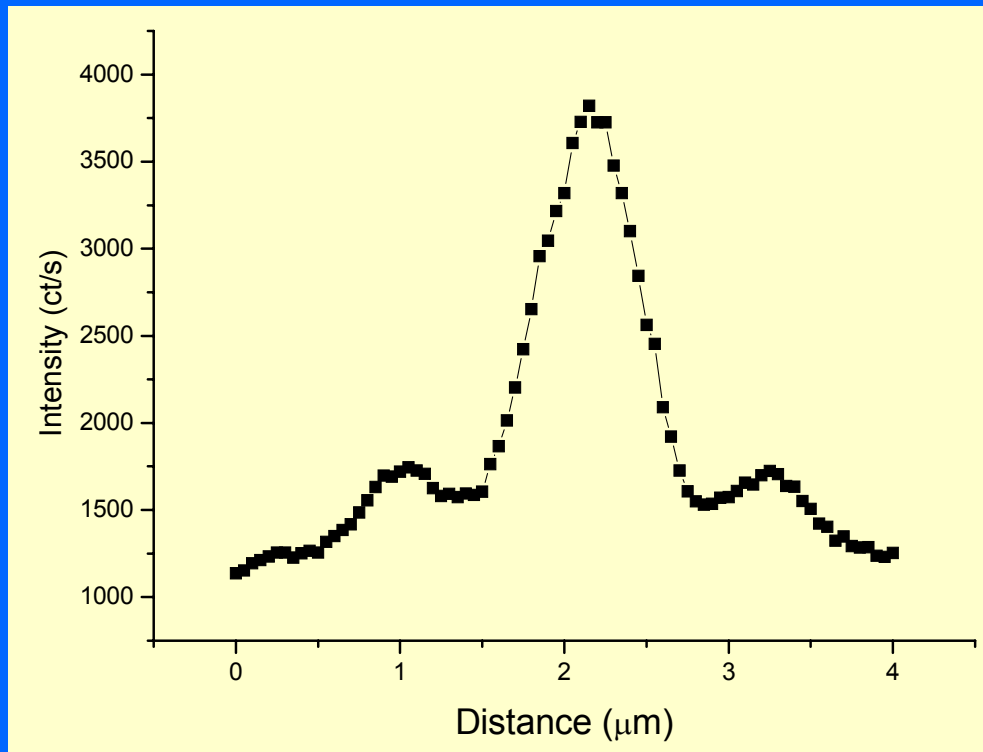
Stacking FZP



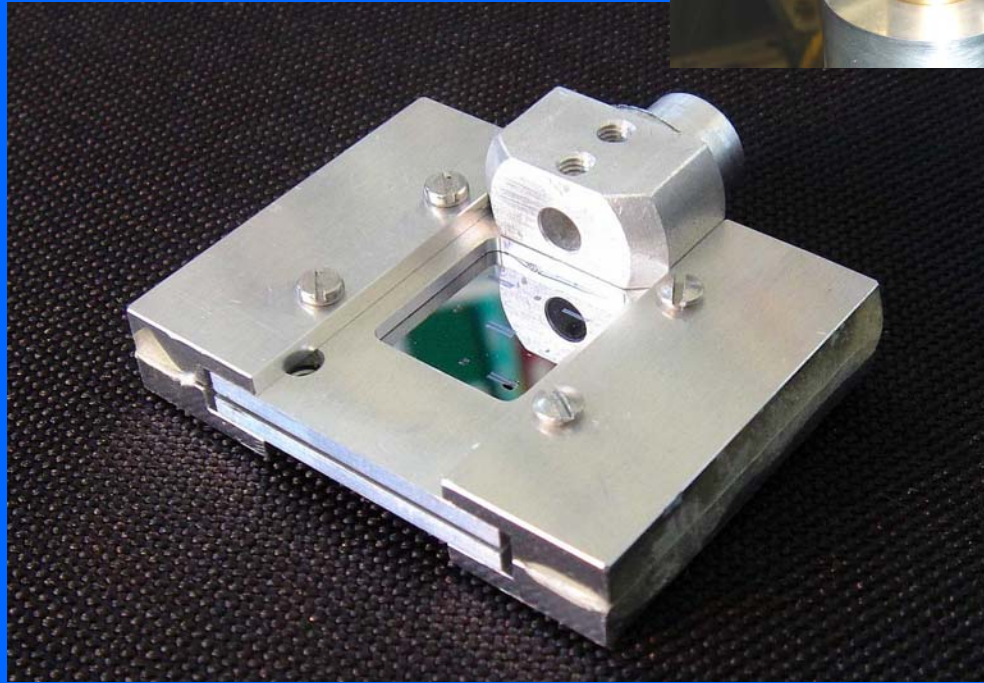
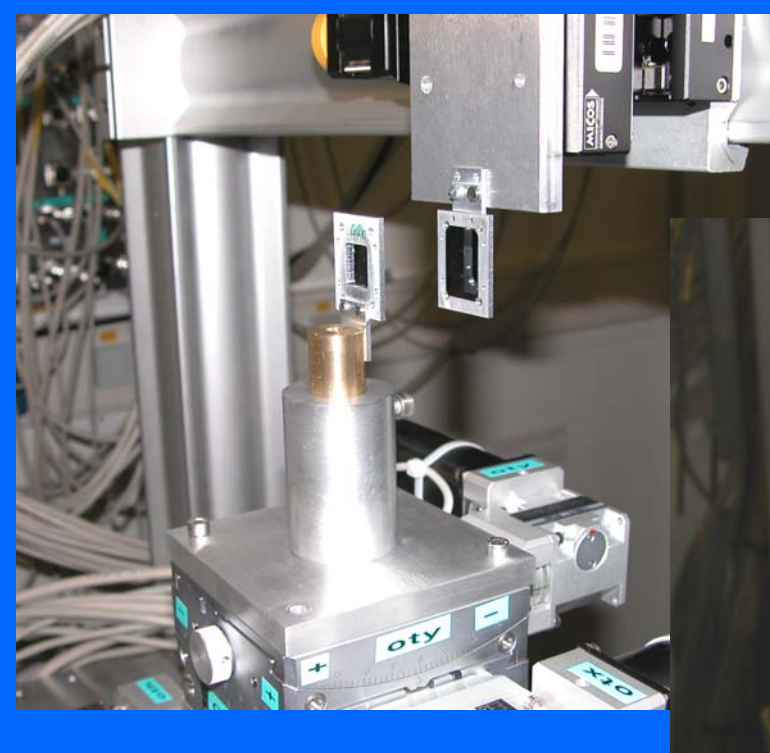
Fine alignment with 50 nm step



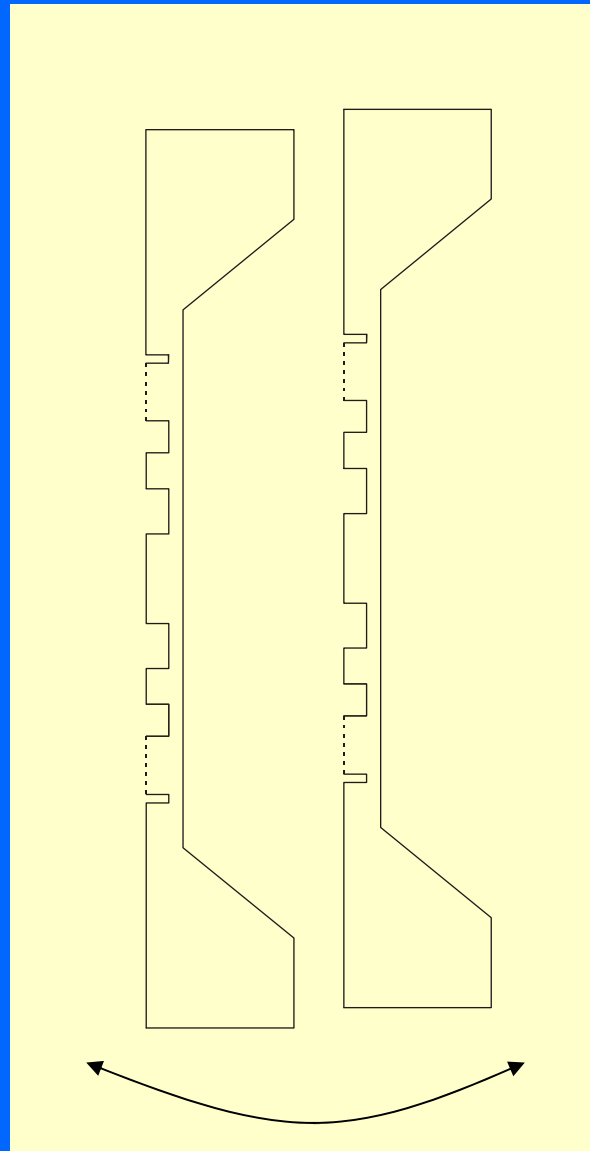
$$\Delta r_n/3$$

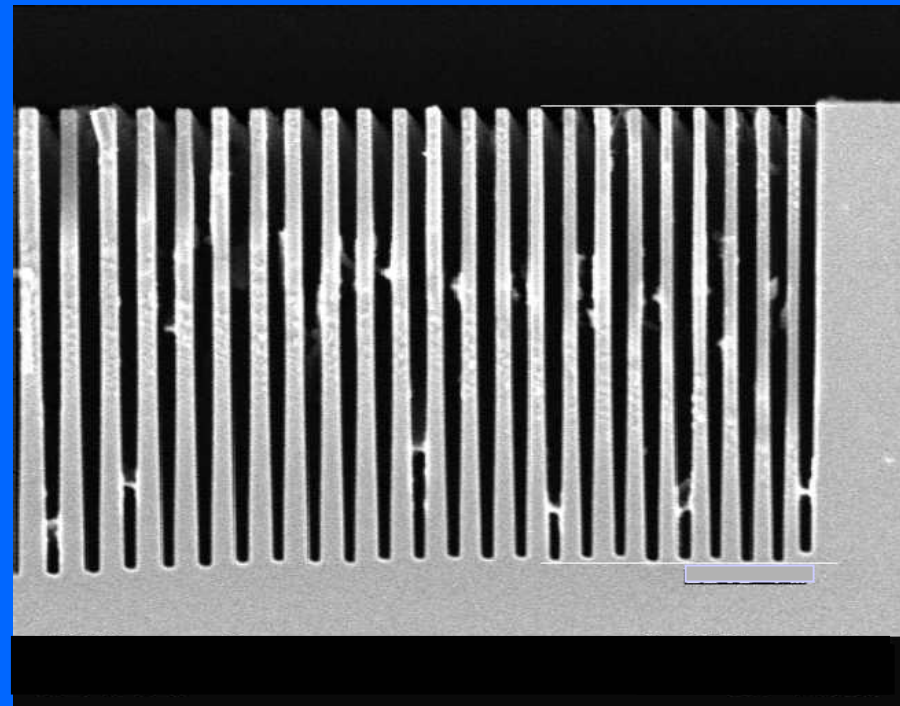
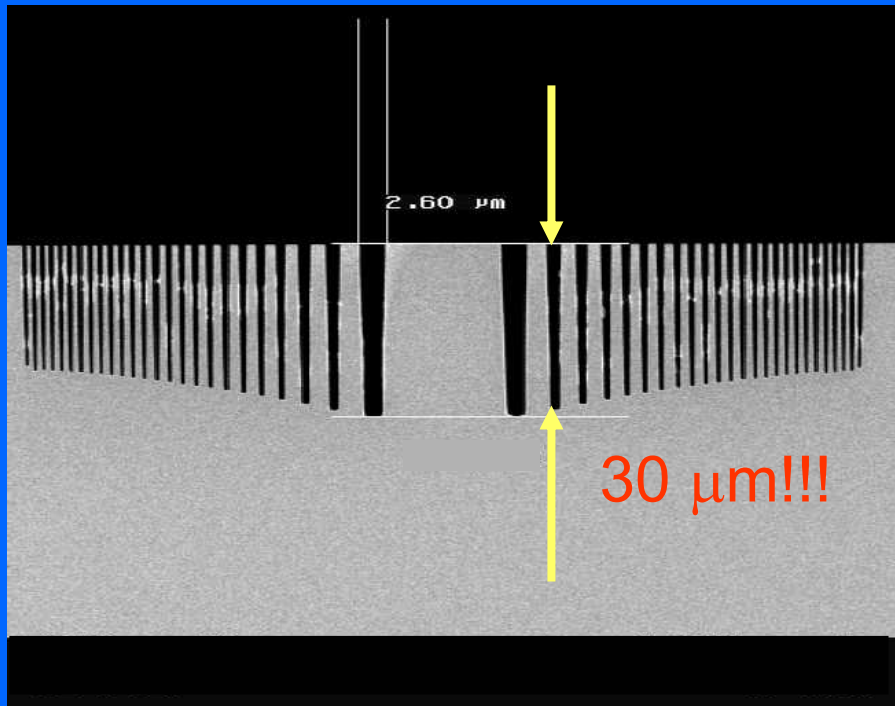


On-line FZP stacking



Tilt compensation
for linear displacement





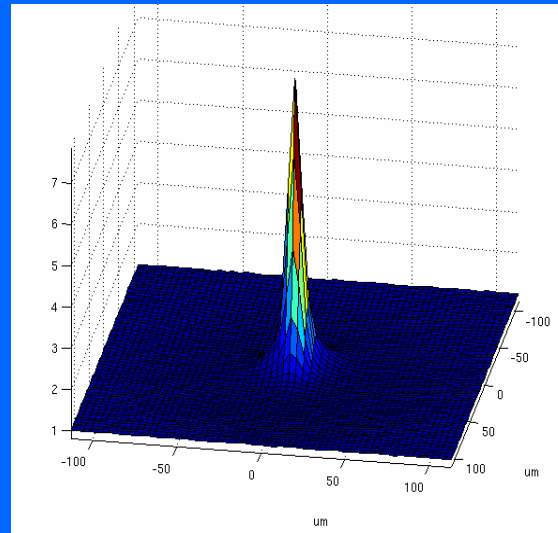
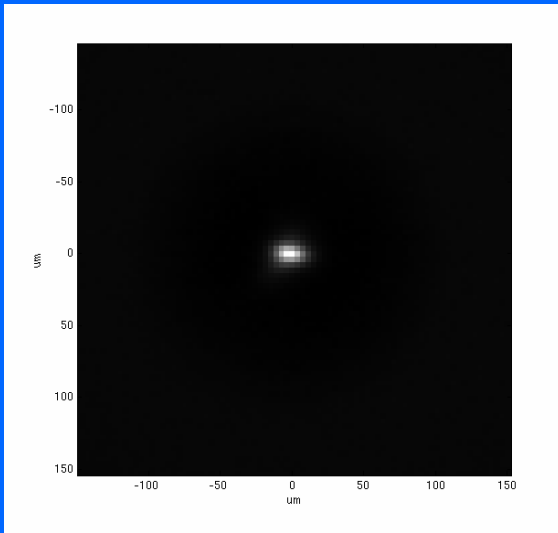
$E = 24 \text{ keV}$
eff $\sim 30\%$

2FZP at 50 keV
eff $\sim 35\%$

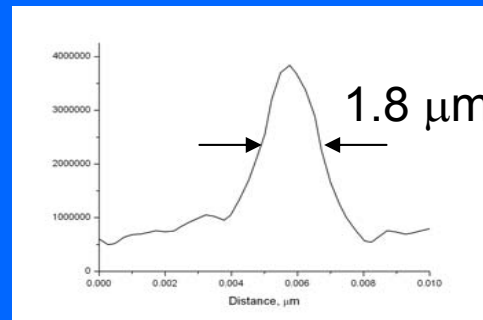
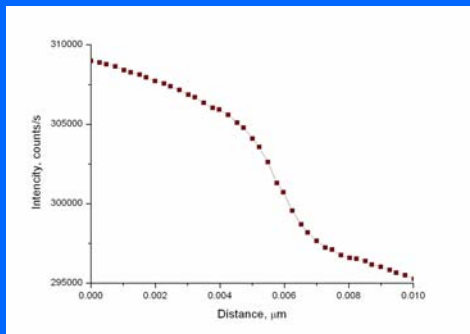
tested at ID15

$F = 3 \text{ m}$

50 keV X-ray focusing with two-stacked FZPs



Vertical scan



2xFZP DOE7/33

$E = 50 \text{ keV}$

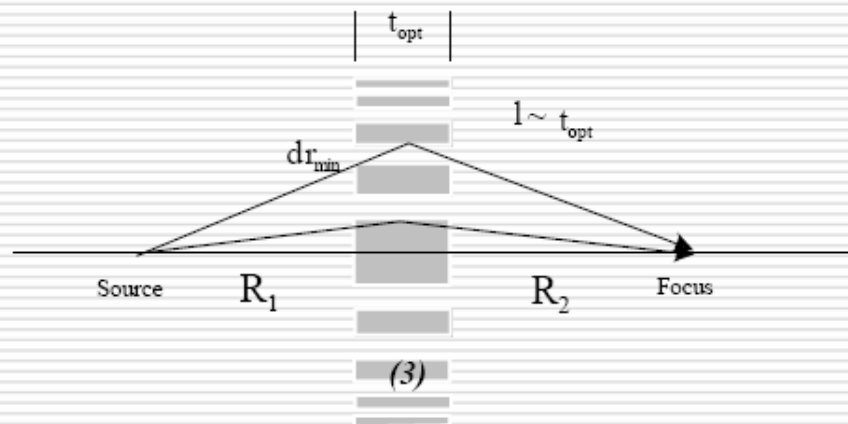
$L_1 = 60 \text{ m}$

$L_2 = 3.2 \text{ m}$

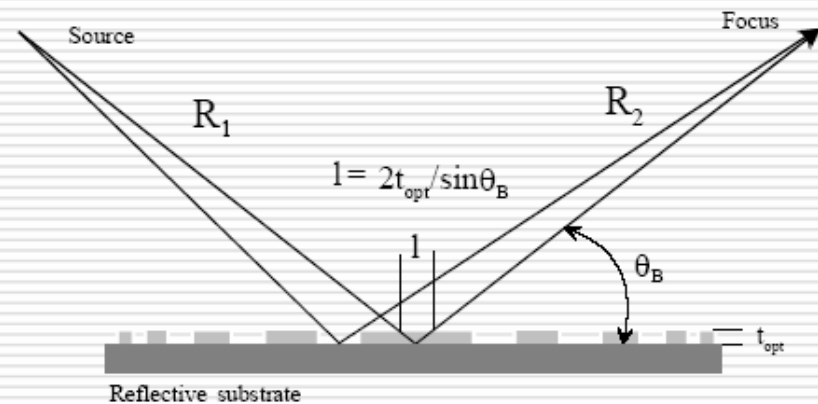
$A = 200 \text{ μm}$

Gain=450

Spatial resolution limit



Transmission zone plate

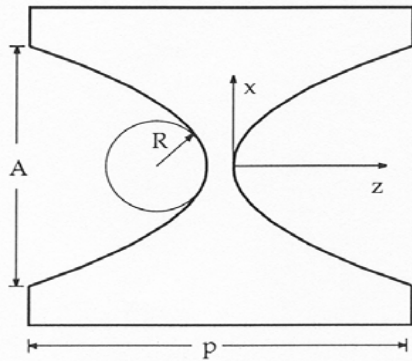


Reflection zone plate

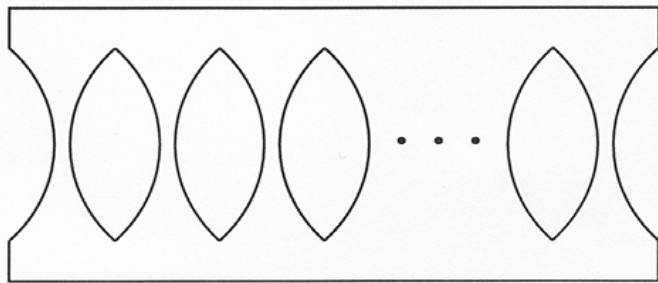
$$\delta r_{min} > \sqrt{m \lambda t_{opt}}$$



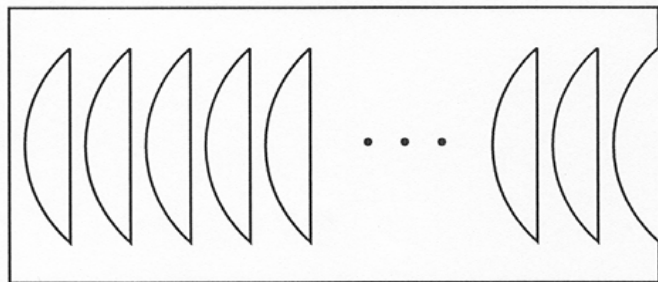
Microfabrication techniques for planar CRLs



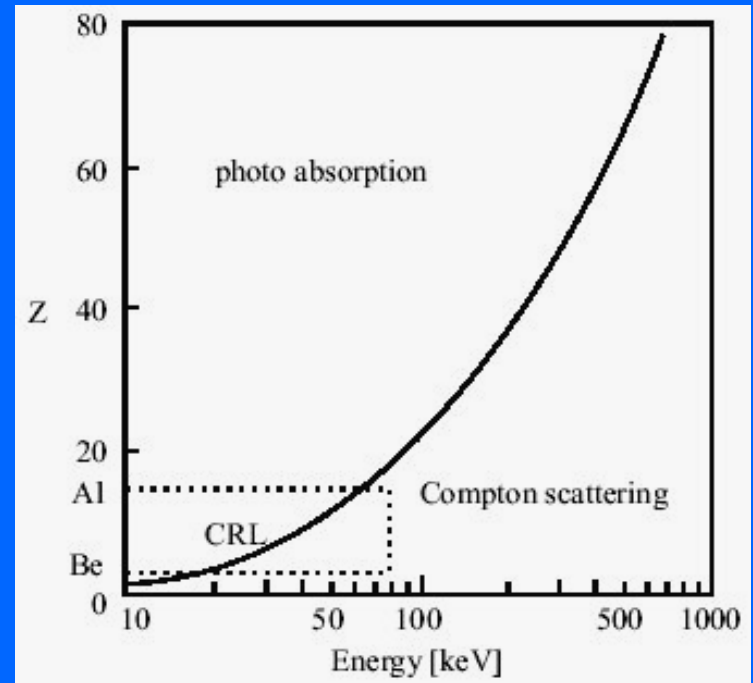
Single parabolic refractive lens



CRL with parabolically shaped holes

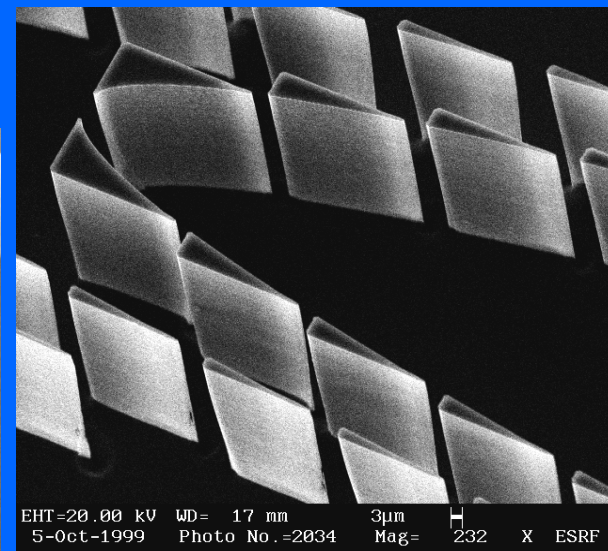
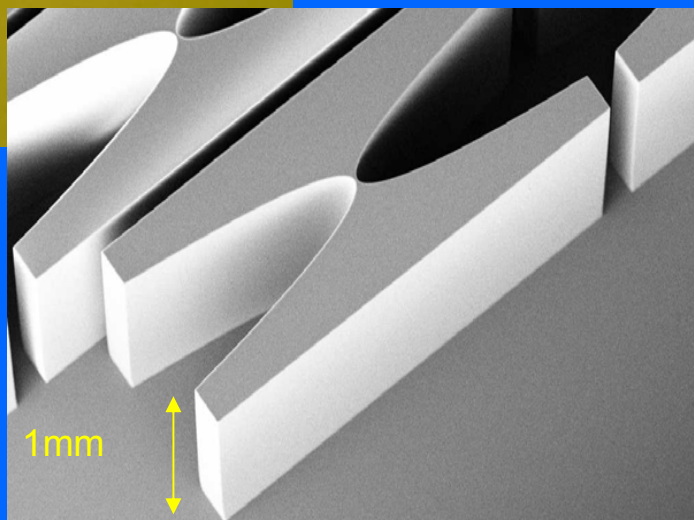
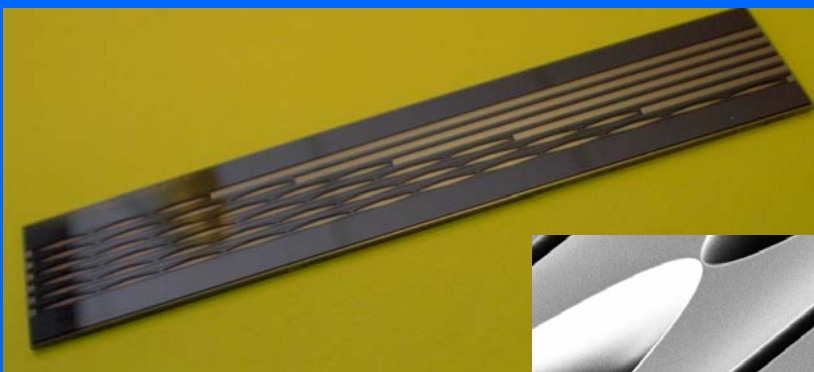
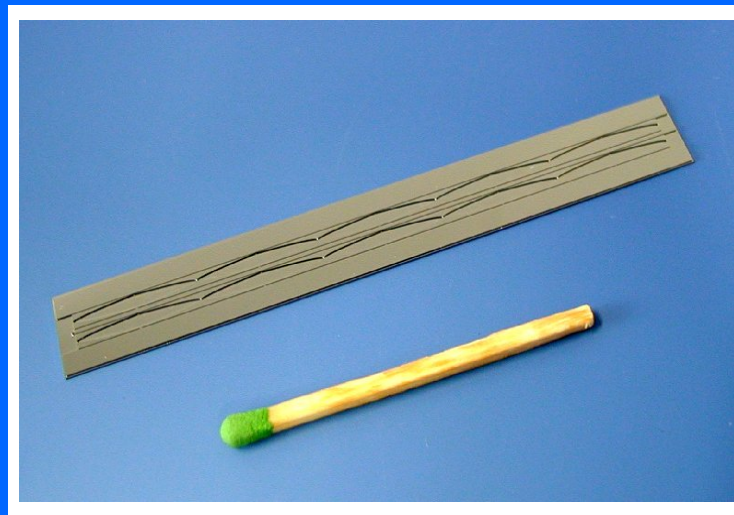
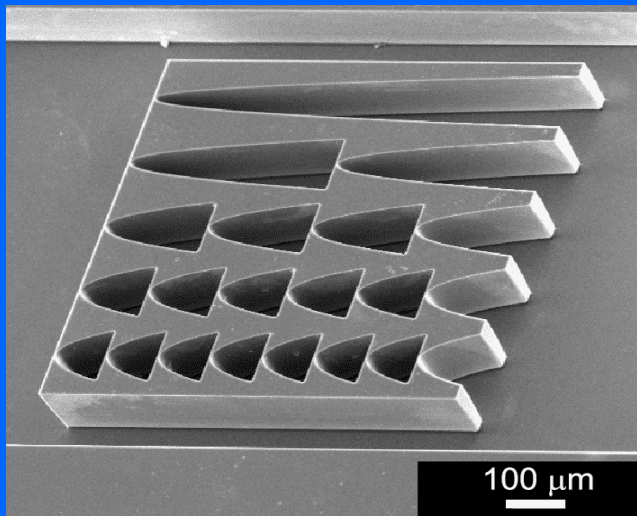


CRL with parabolically shaped half-holes



- R must be small $R < 0.5$ mm
- $\mu/\rho \sim Z^3/E^3$ must be small
low Z material: Li, Be, B, C, SU-8, Al, Si
- gain $\sim \delta/\beta$

	E, keV	δ	β	δ/β
Si	10	4.9E-6	7.4E-8	70
	20	1.2E-6	4.6E-9	250
Diamond	10	7.3E-6	6.9E-9	1000
	20	1.8E-6	3.6E-10	5000



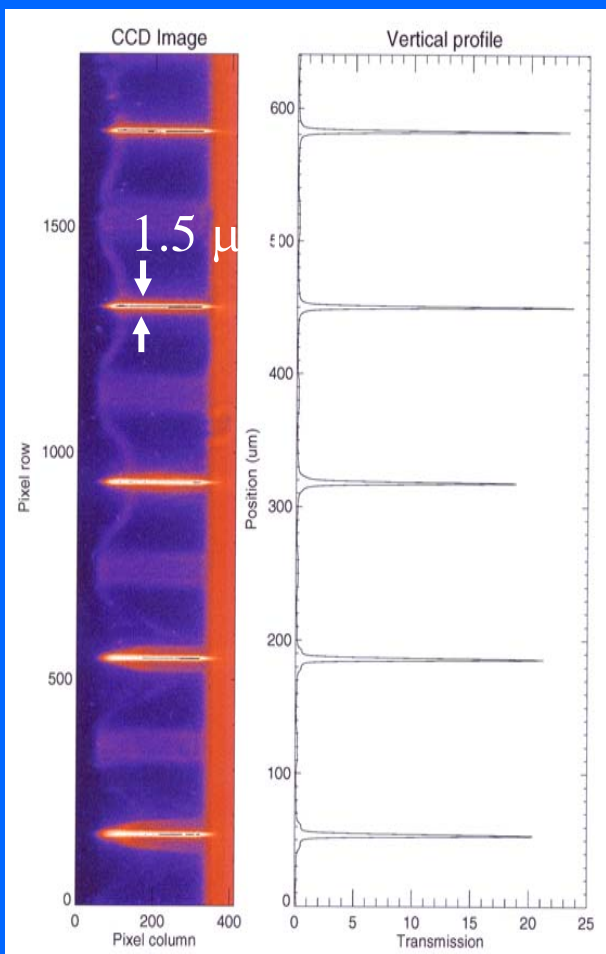
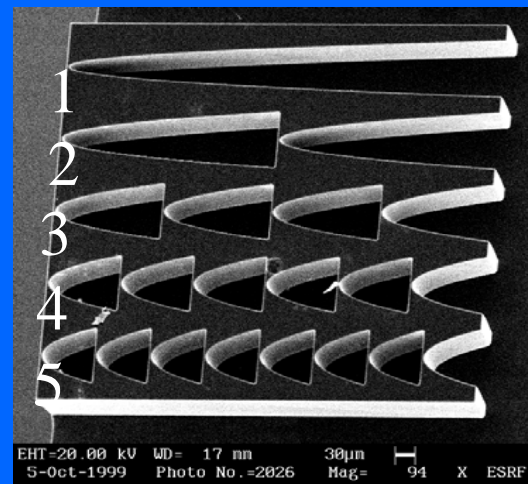
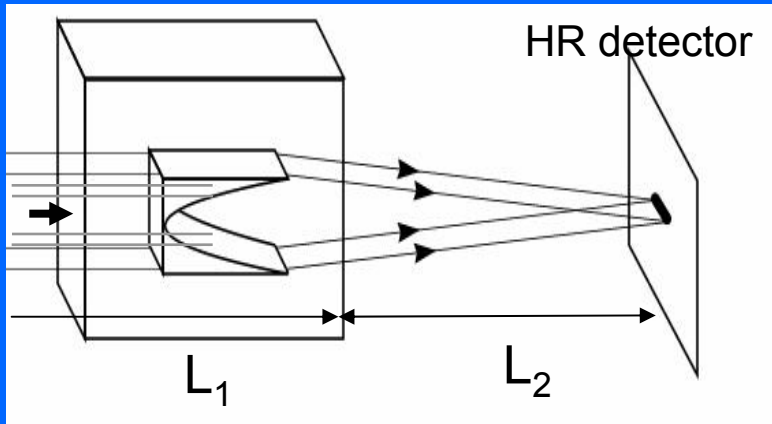
Advantages of micro-fabrication technology

- Any combination of refraction and diffraction properties
- Computer-aided design (from incident wavefront correction to pre determined exit wavefront generation)
- No diffraction-limited aperture
- Use of low-Z materials that are hard for machining (Si, B, diamond)

Advantages of Linear focusing

- Astigmatic focusing
vertical source size is smaller than horizontal one.
- Combination with other BL focusing elements as crystals, mirrors.
- Needs for high resolution diffraction and scattering techniques including surface analysis, high resolution diffraction experiments, standing waves technique

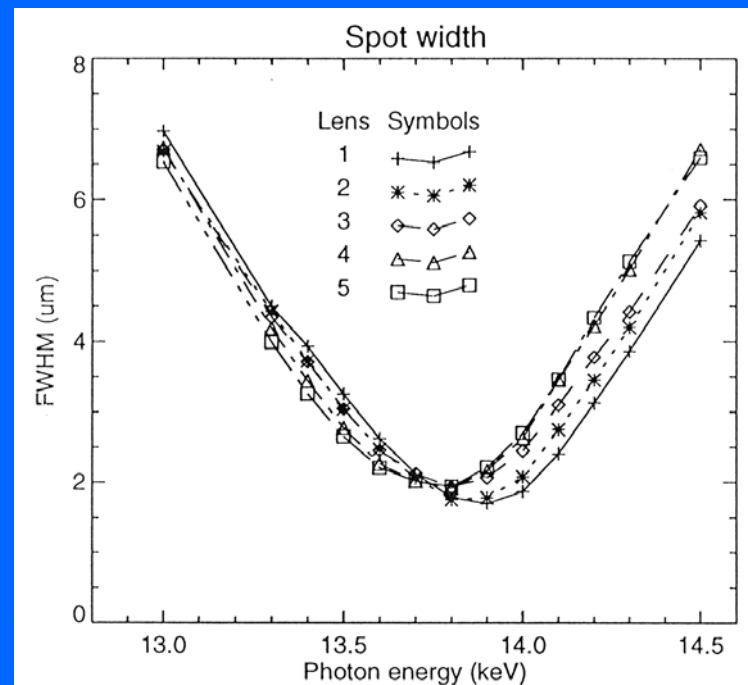
Si lenses with 0.3 – 0.4 μm profile deviation



aperture 100 μm
 high 100 μm
 web size 5 μm

lens R_{parabola tip}
 1 - 3.2 μm;
 2 - 6.4 μm;
 3 - 12.8 μm;
 4 - 19.1 μm;
 5 - 25.4 μm

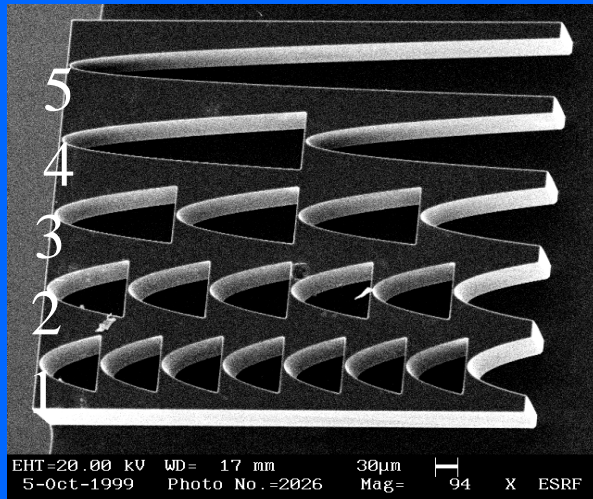
E = 14 keV
 F = 75 cm
 Source size 30 μm
 Source-to-lens
 distance 60 m
 FWHM = 1.5 μm



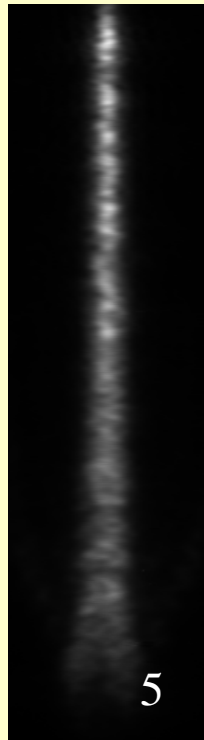
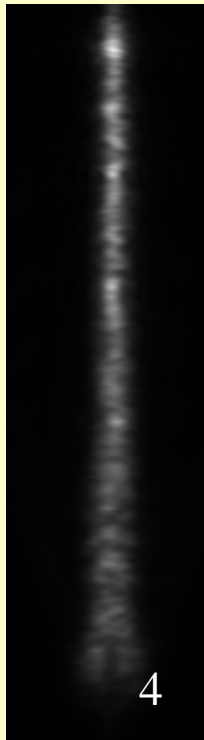
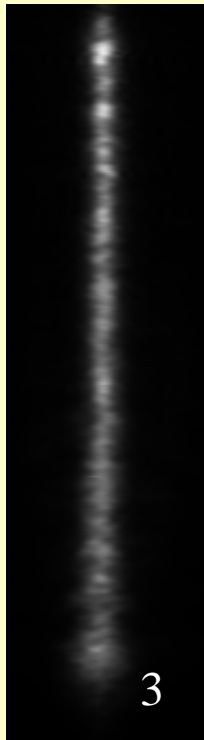
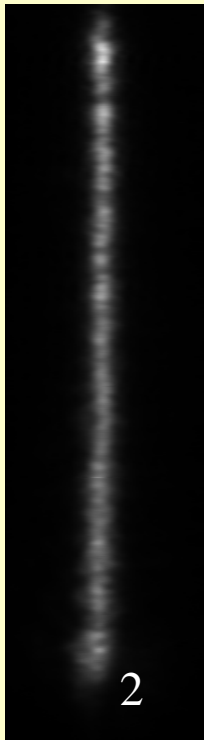
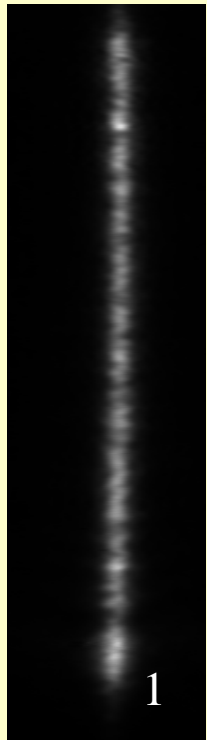
Focus depth energy scan for 5 lenses

Test of Si lenses with 0.3 – 0.4 μm profile deviation

at SPRing-8

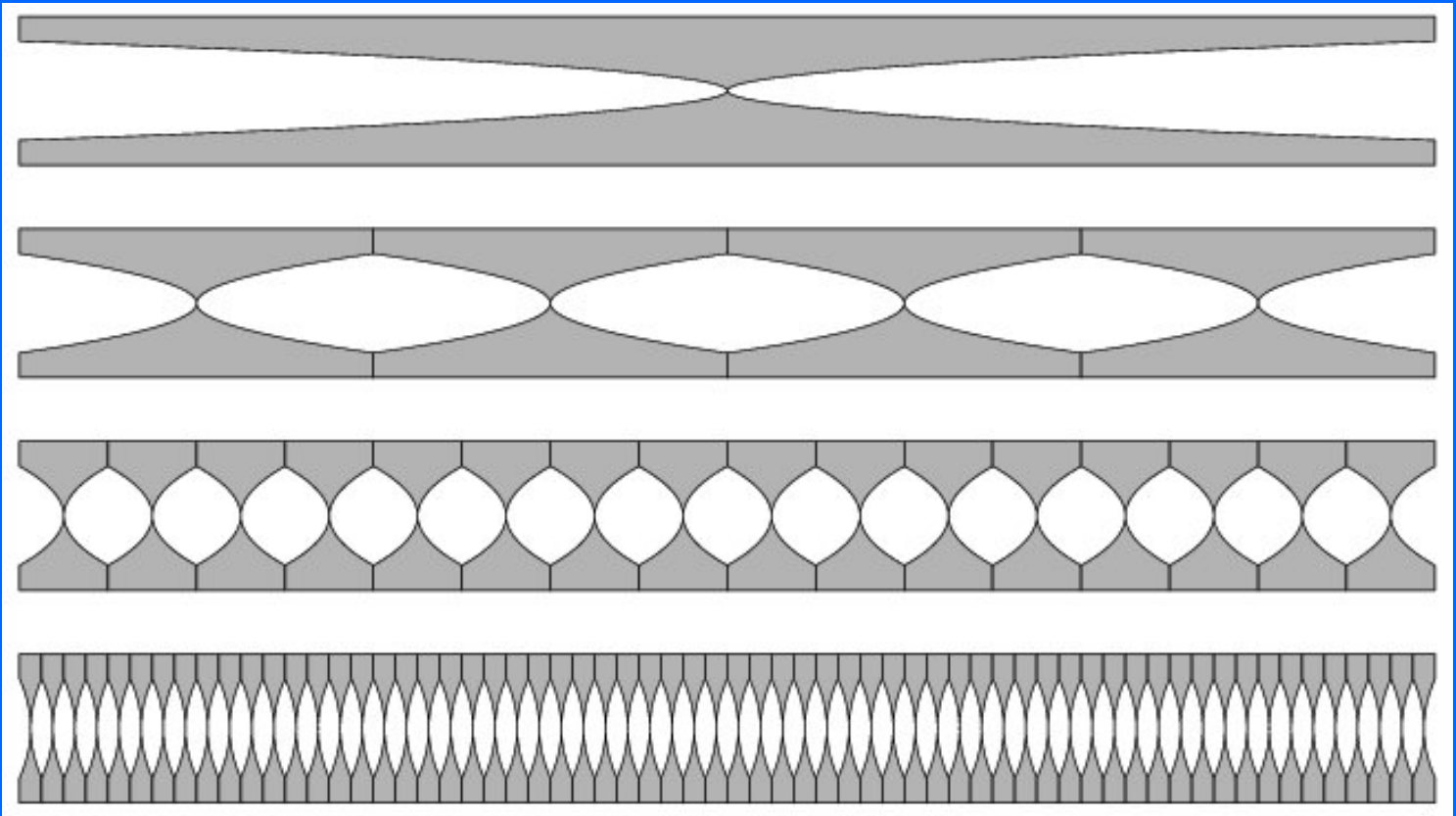


$E = 17 \text{ keV}$ $F = 100 \text{ cm}$
Source size $15 \mu\text{m}$
Source-to-lens distance $1 \text{ km} !!!$
 $\text{FWHM} = 0.9 \mu\text{m}$

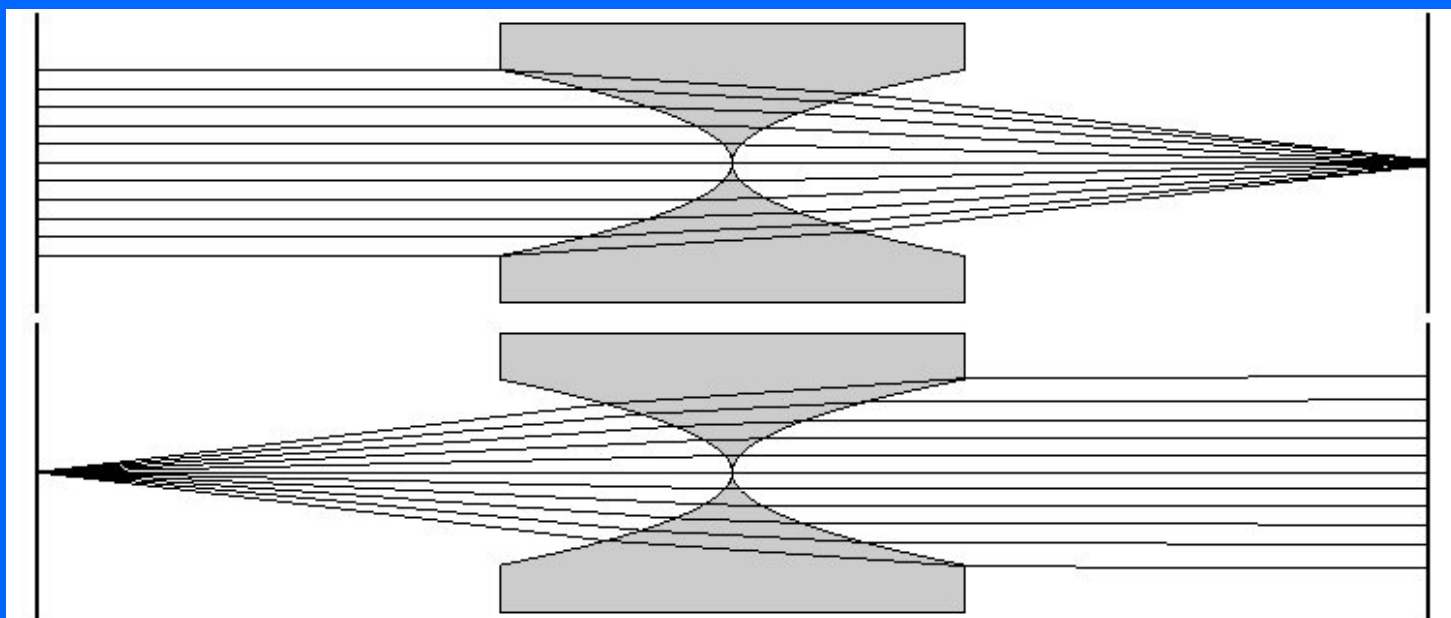
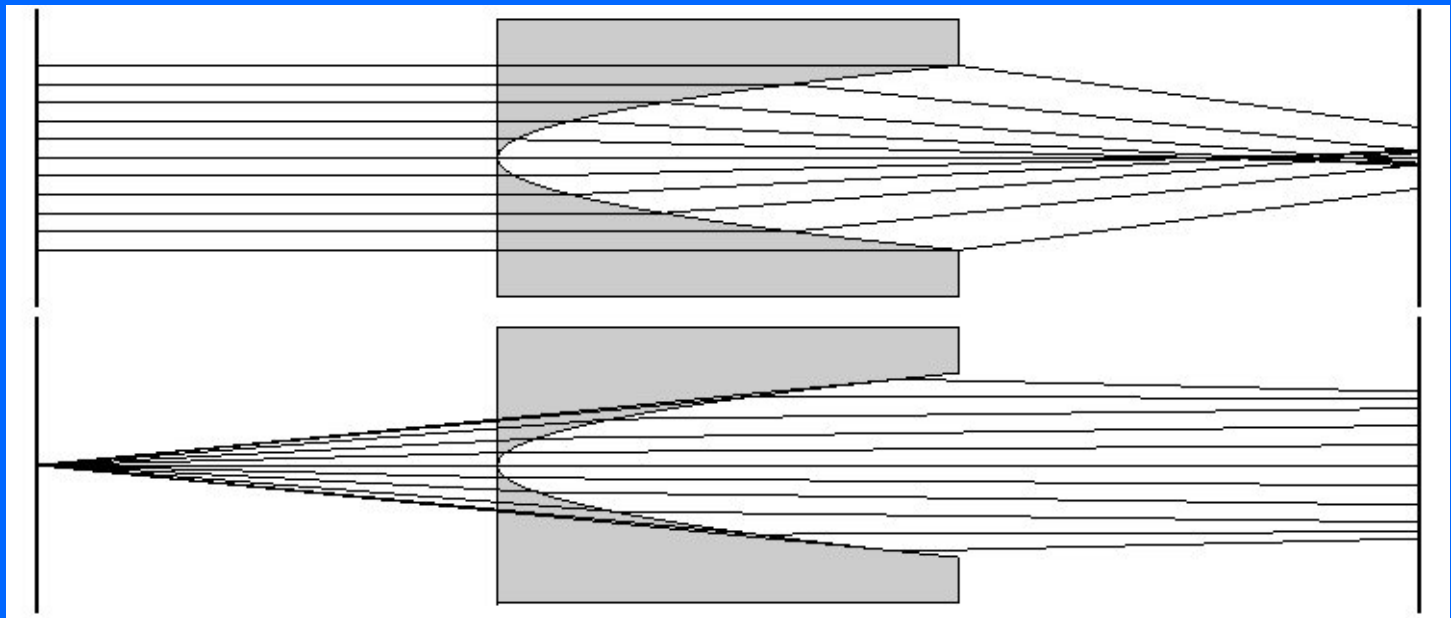


Detector resolution
 $0.3 \mu\text{m}$

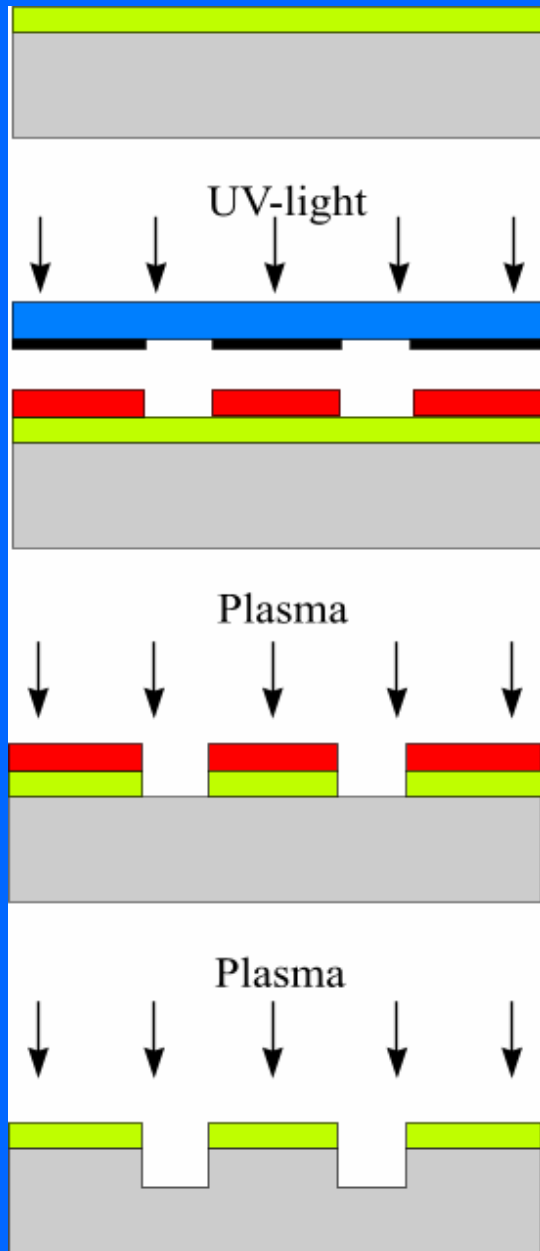
A. Souvorov et al



$$F = \frac{R}{2N\delta}$$



Fabrication of silicon parabolic lenses



SiO_2
Si

Thermal oxidation of Si wafer

UV-light

Photomask
Photoresist
 SiO_2
Si

Resist spin, exposure and development

Plasma

Photoresist
 SiO_2
Si

Anisotropic oxide etching in CHF_3 plasma

Plasma

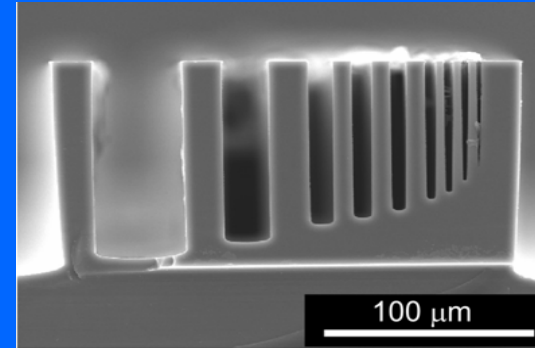
SiO_2
Si

Deep silicon etching in "Bosch process"

Inaccuracies in deep silicon etching

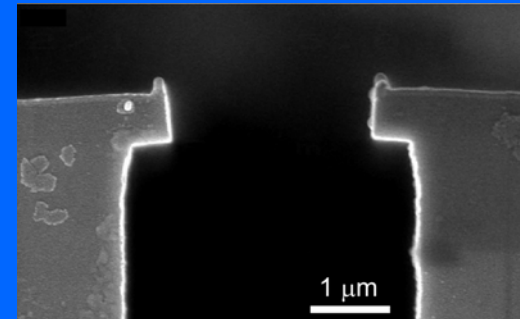
Etched depth and shape of trenches depend on aspect ratio and/or trench width

- **1 mm**-wide trenches have negatively sloped sidewalls
- **20 μm** trench exhibits nearly vertical profile

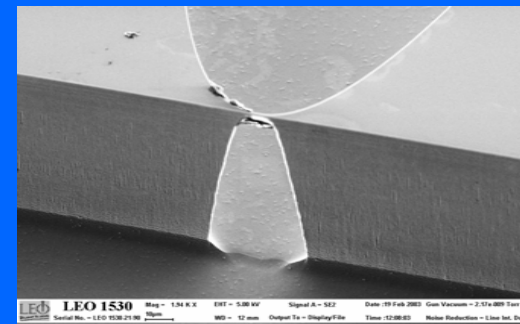


Mask undercut is:

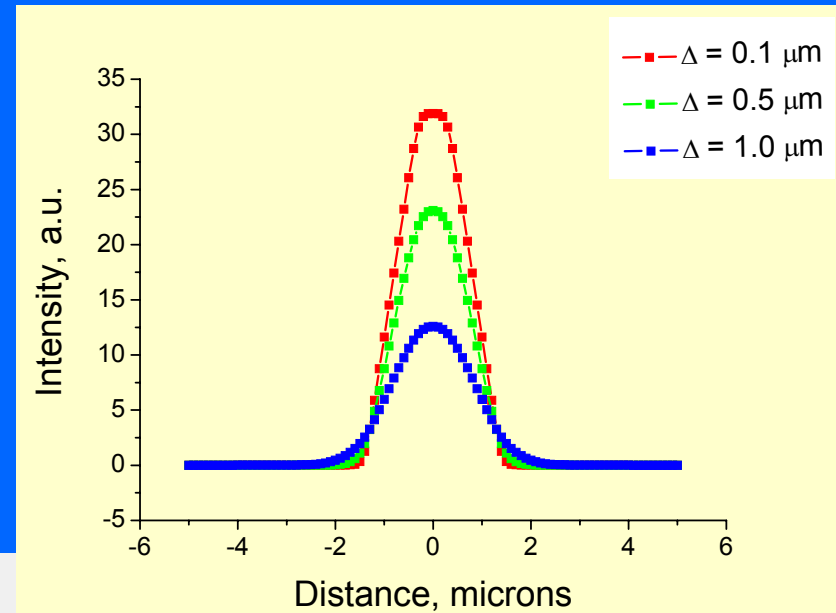
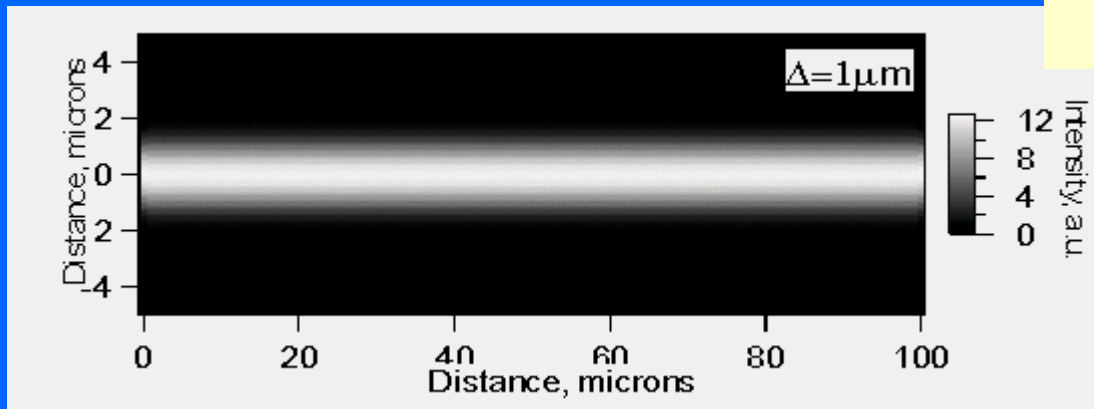
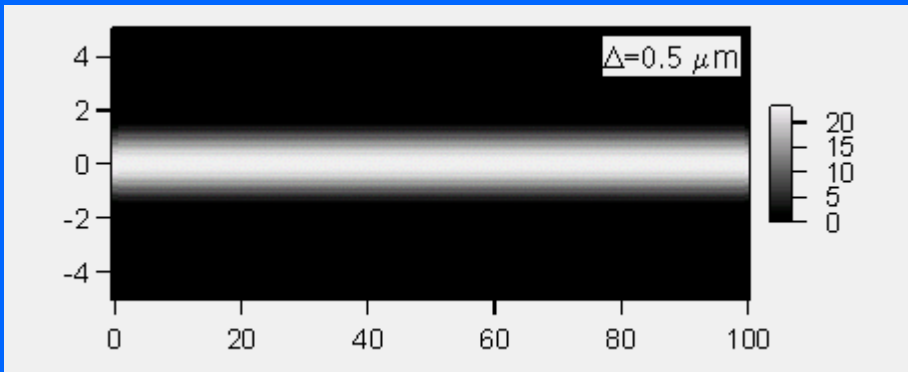
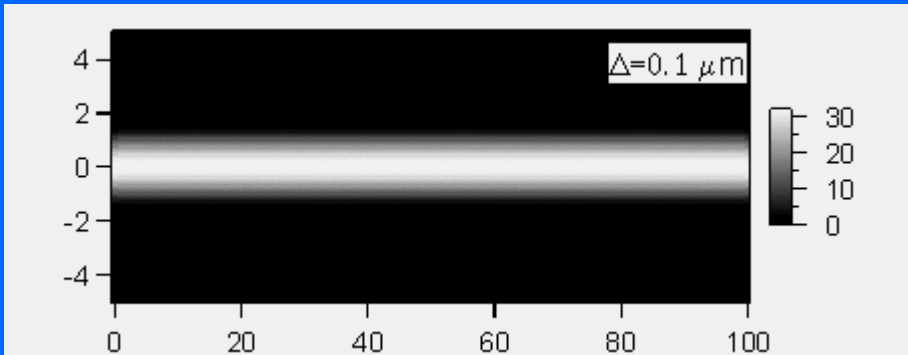
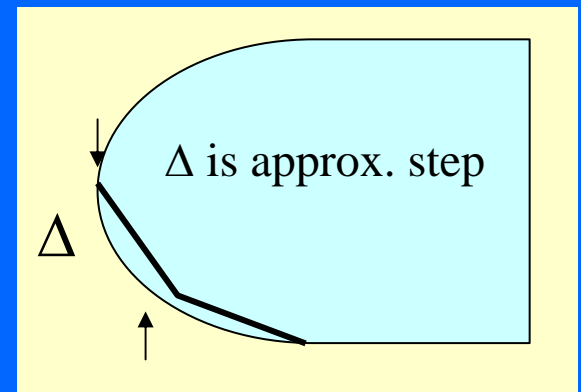
- in the range of **0.5-0.6 μm**
- independent on the trench width



Deviation of the parabolic refractive profile from the ideal one caused by mask undercut and sidewall etching during silicon etching down to **200 μm**

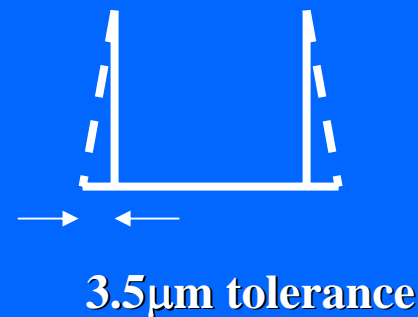
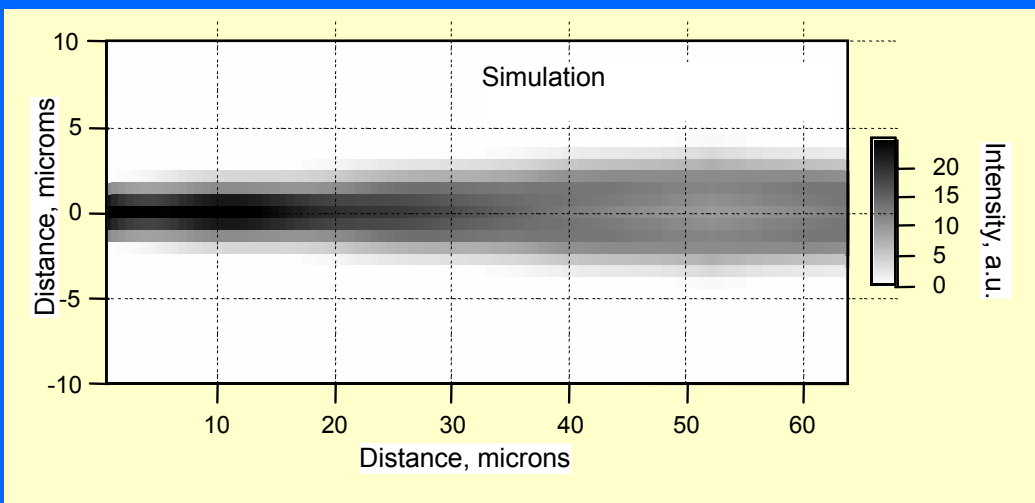
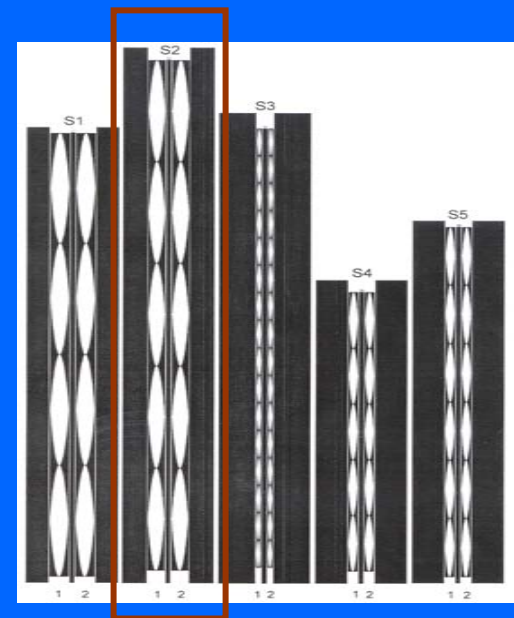
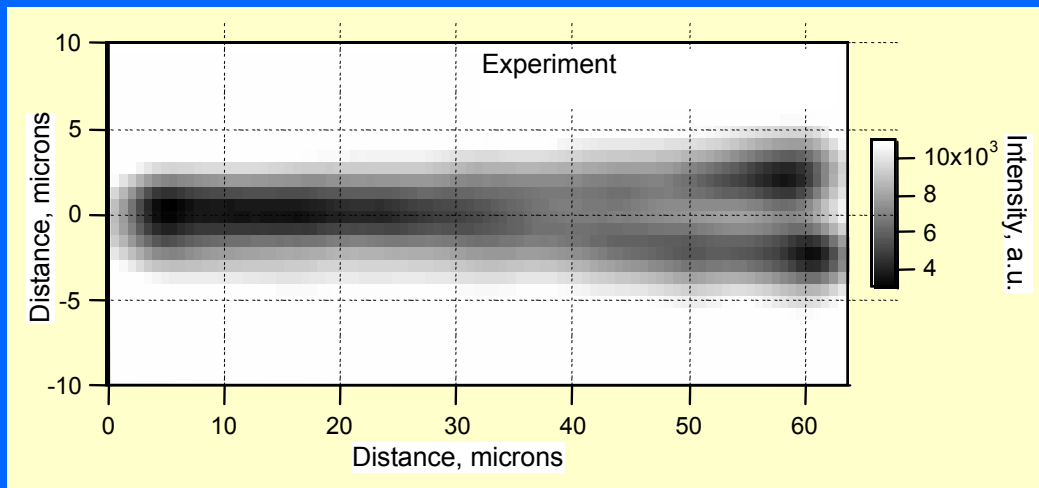


Parabola approximation



optimization of parabolic profile approximation is compromise between a precise parabola and a size of data file for lithography.

Profile deviations: experiment and simulation



$E = 20 \text{ keV}$

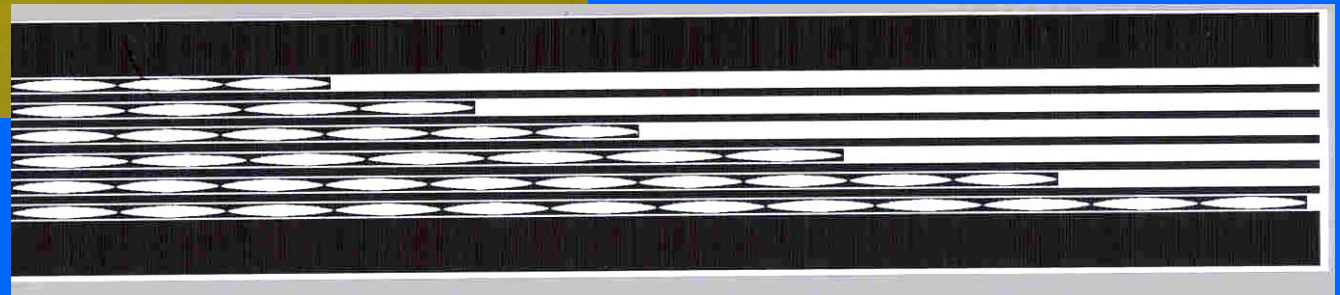
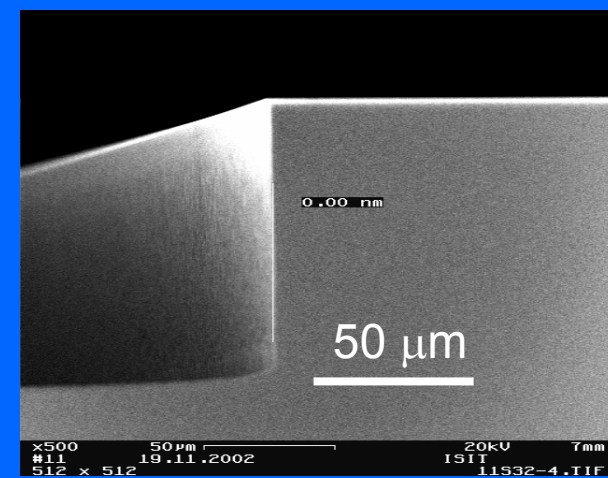
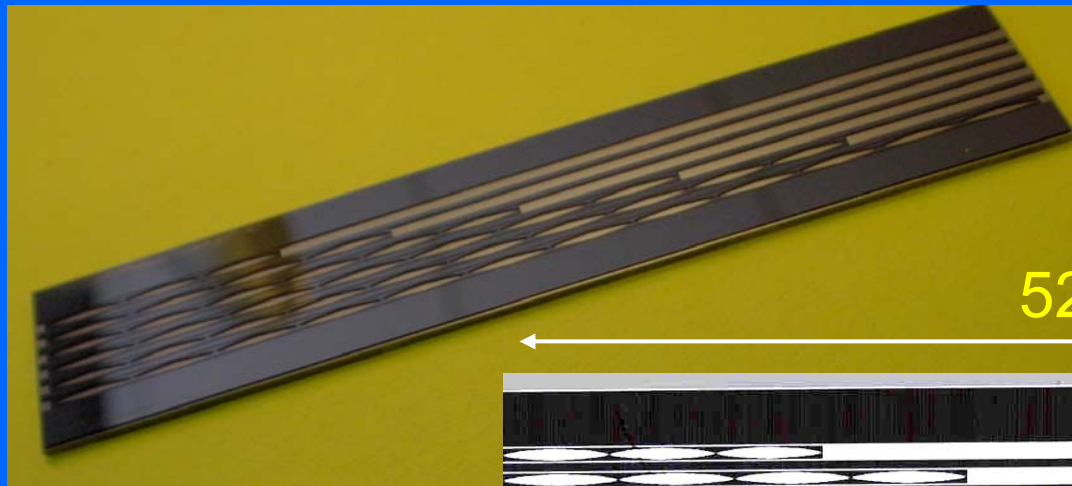
$F = 40 \text{ cm}$

$A = 500 \mu\text{m}$

$N = 32$

Lens-to-detector distance 43 cm

Test of Energy-Tunable Si-lens

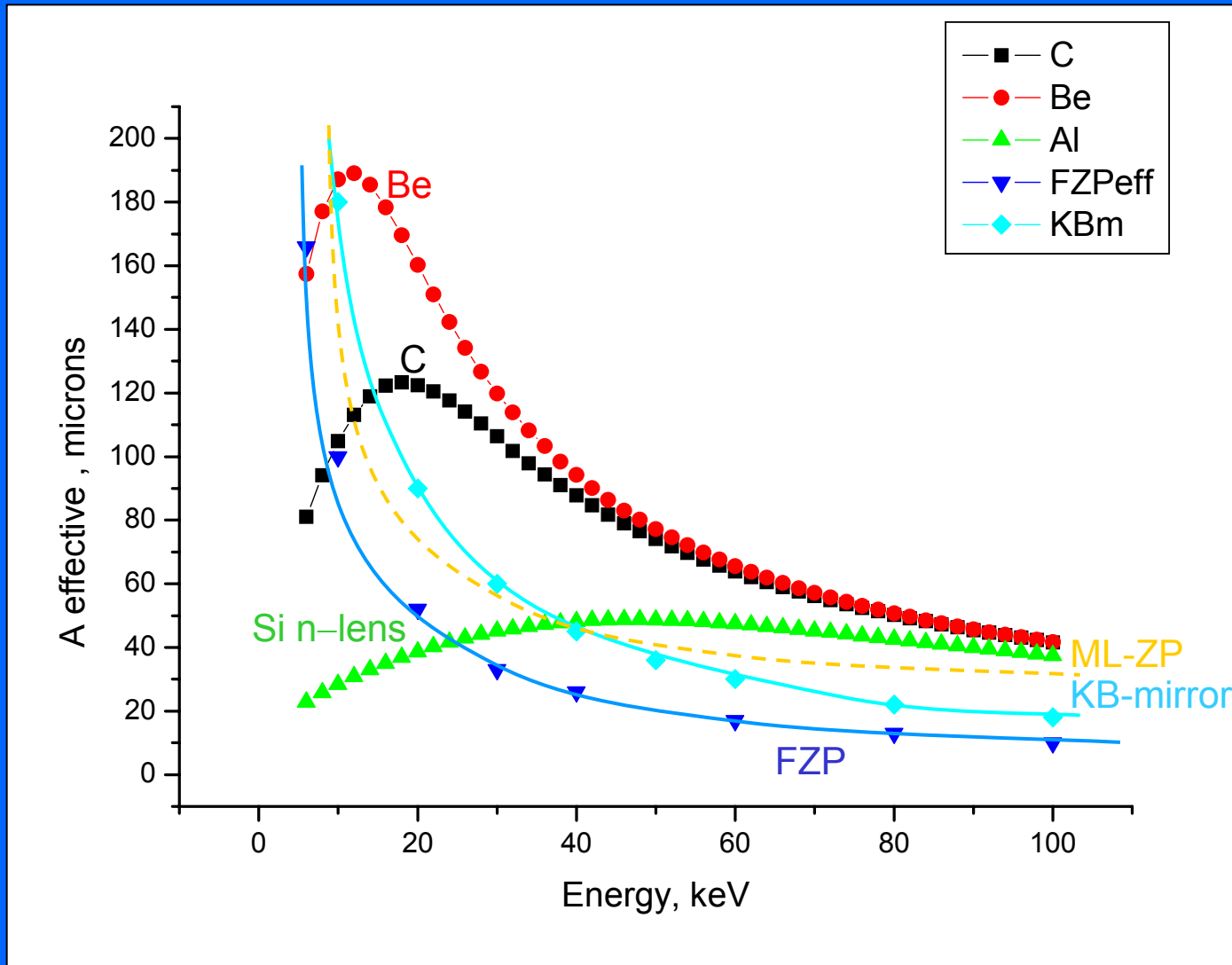


Lens number	Energy, keV	Number of lenses, 2N	Lens length, cm	Aperture, μm	Focal spot, μm	Focal distance, cm
S6 - 1	10	6	1.28	500	3.6	50.4
S6 - 2	12	8	1.86	500	3.7	51.1
S6 - 3	14	12	2.51	500	3.6	50.8
S6 - 4	16	14	3.33	500	3.7	50.1
S6 - 5	18	20	4.18	500	3.9	50.5
S6 - 6	20	24	5.17	500	3.6	51

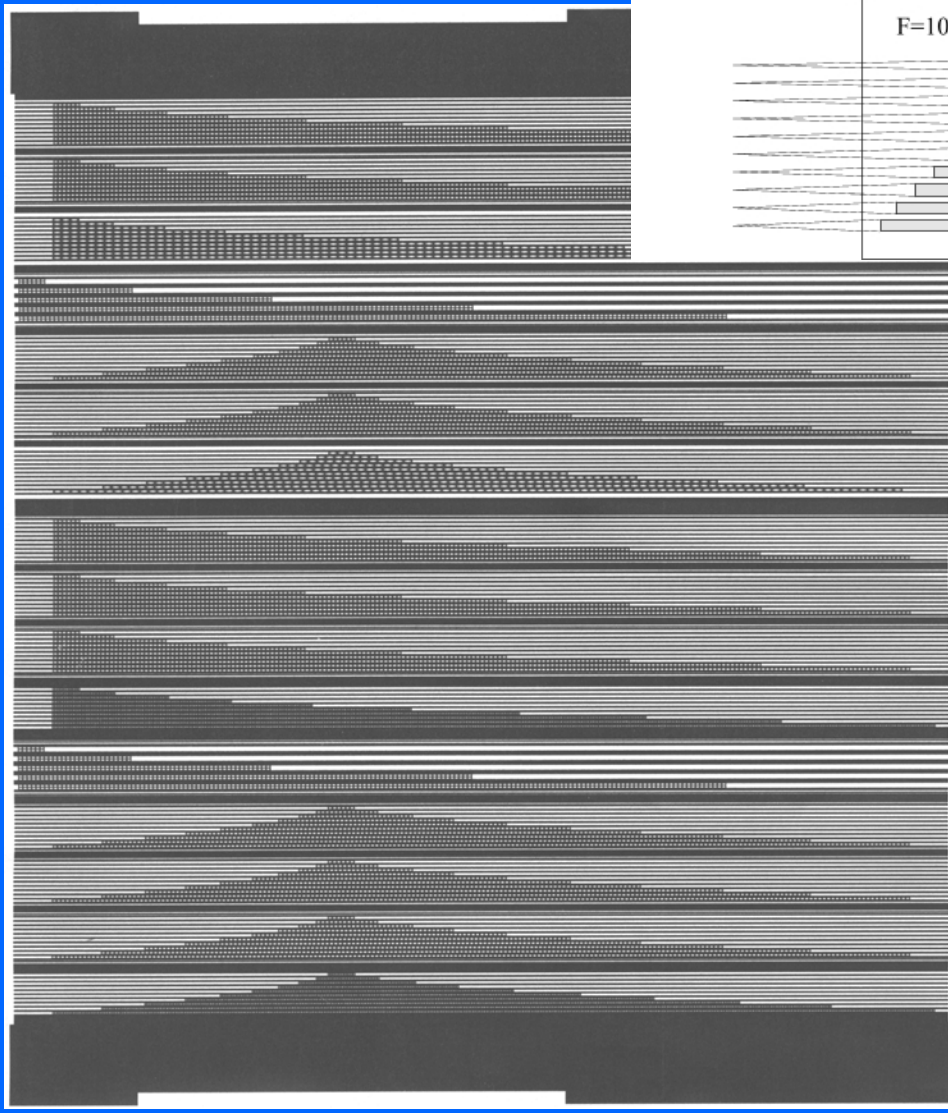
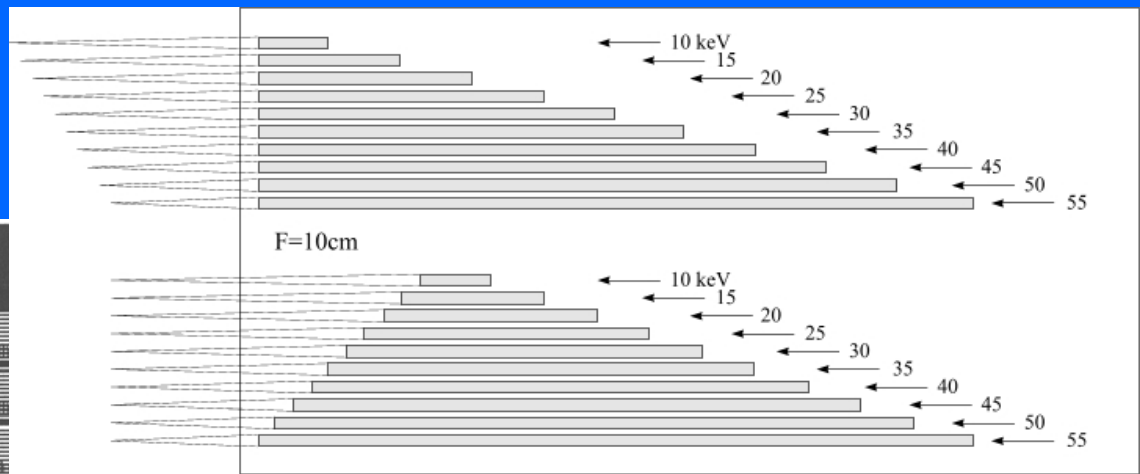
Long BL: 100m
Source $50\mu\text{m} \times 150\mu\text{m}$

$F = 10 \text{ cm}$

$50 \text{ nm} \times 150 \text{ nm}$
Demagnification X 1000



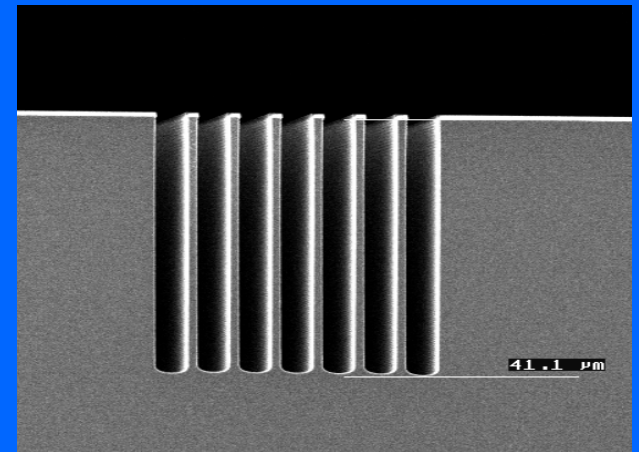
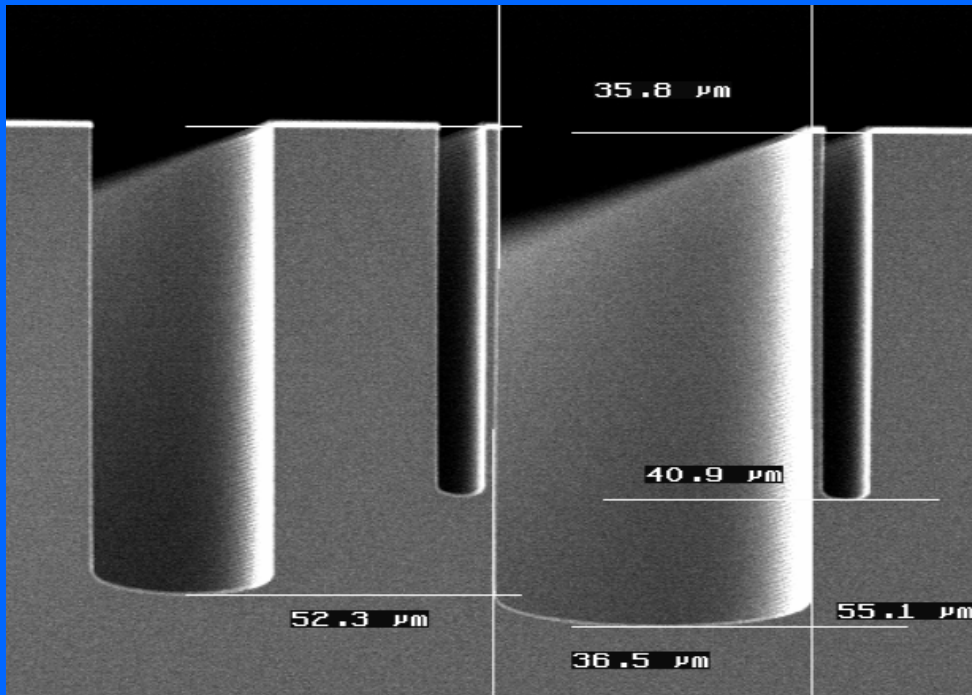
Lens chip design

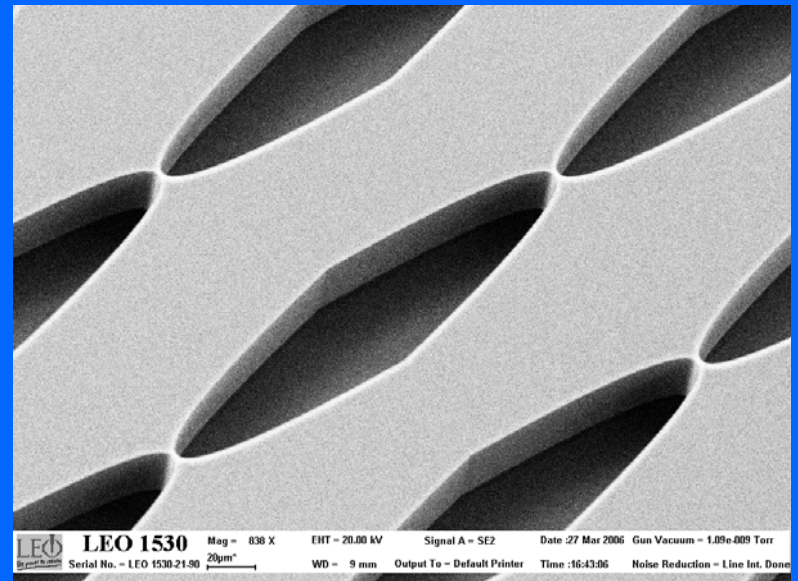
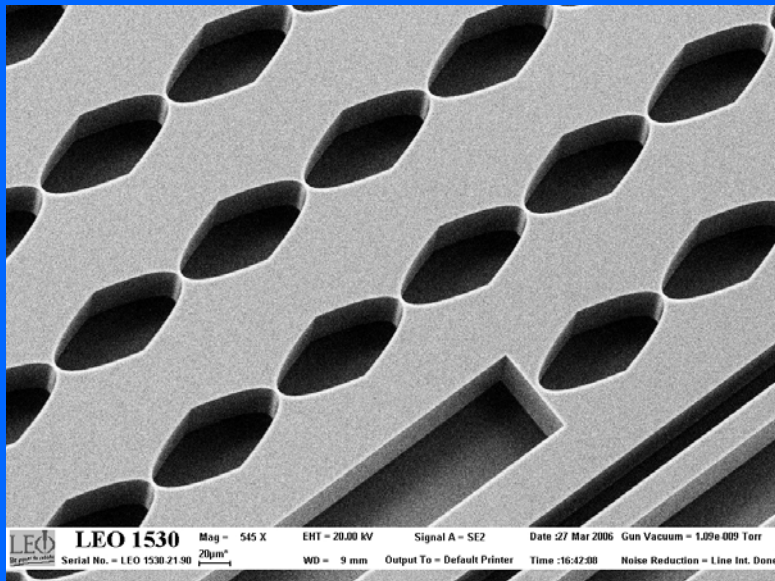
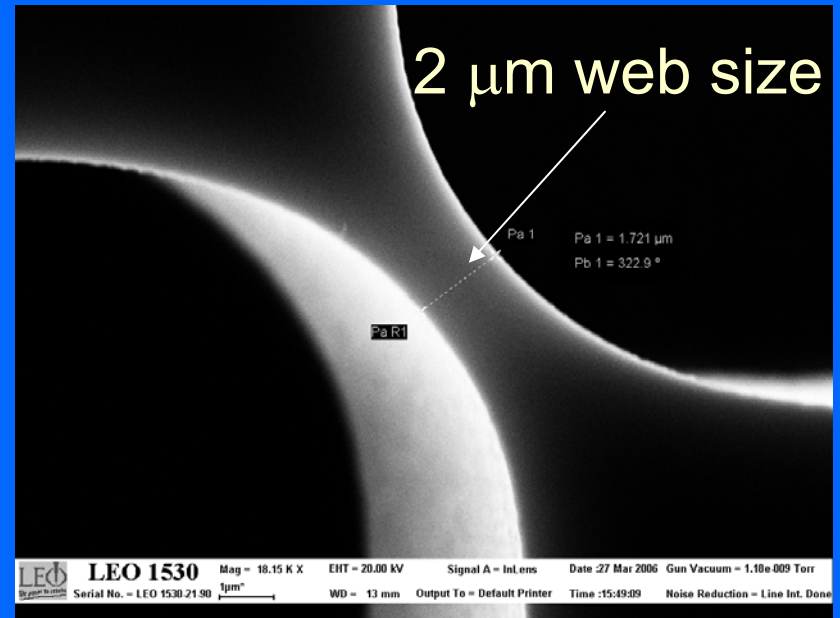
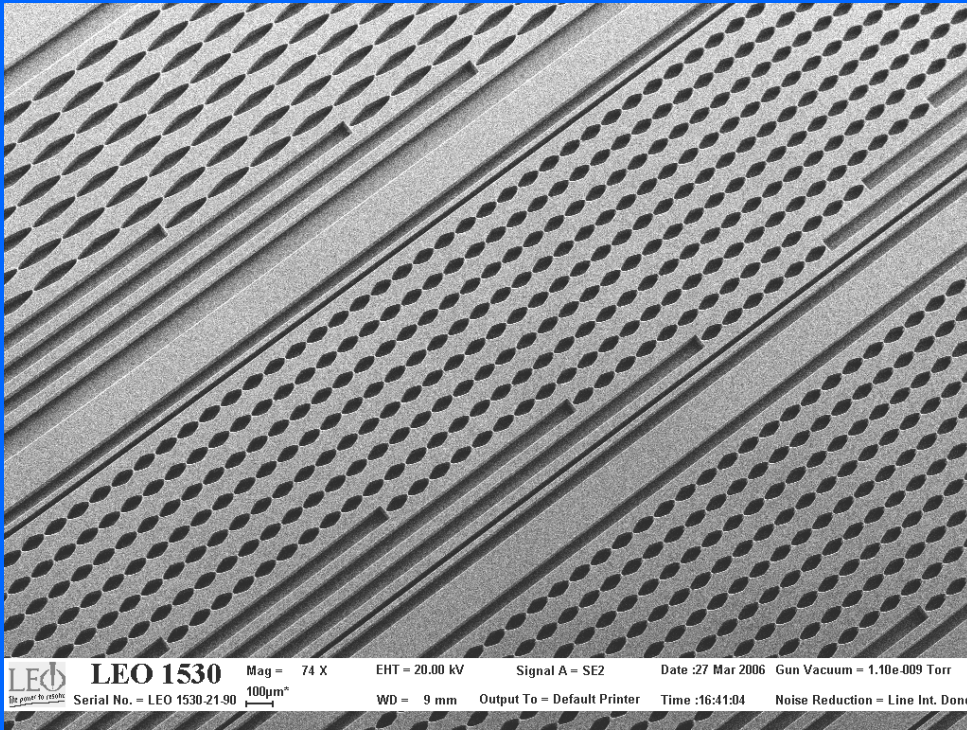


25 mm

22 mm

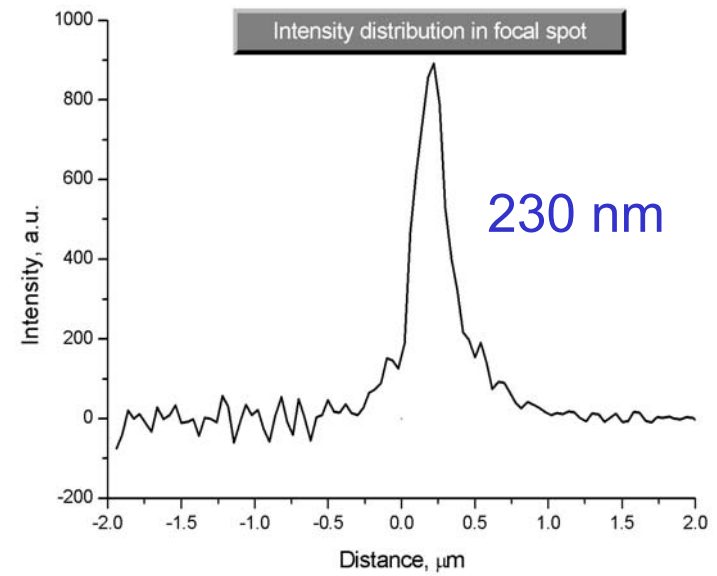
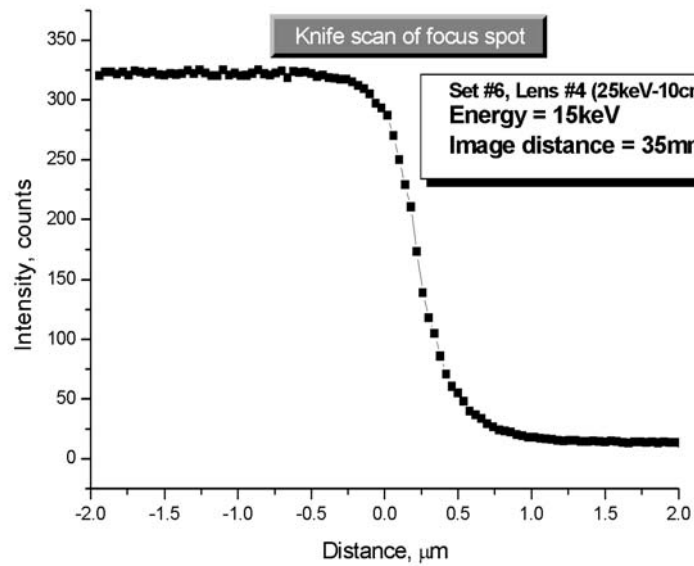
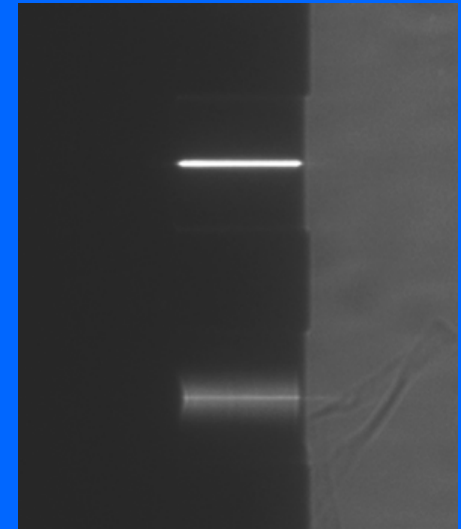
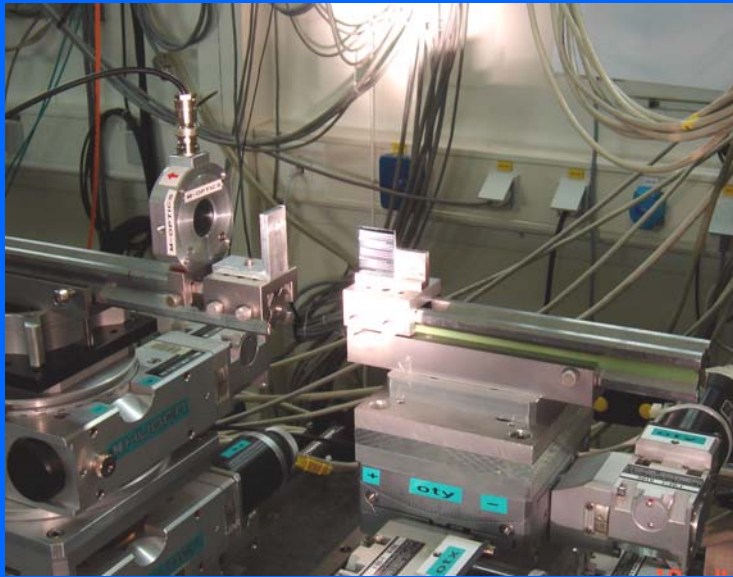
> 150 CRLs !





Test at BM05/MOTB in April 2006

E = 15-30 keV
resolution 200-300 nm



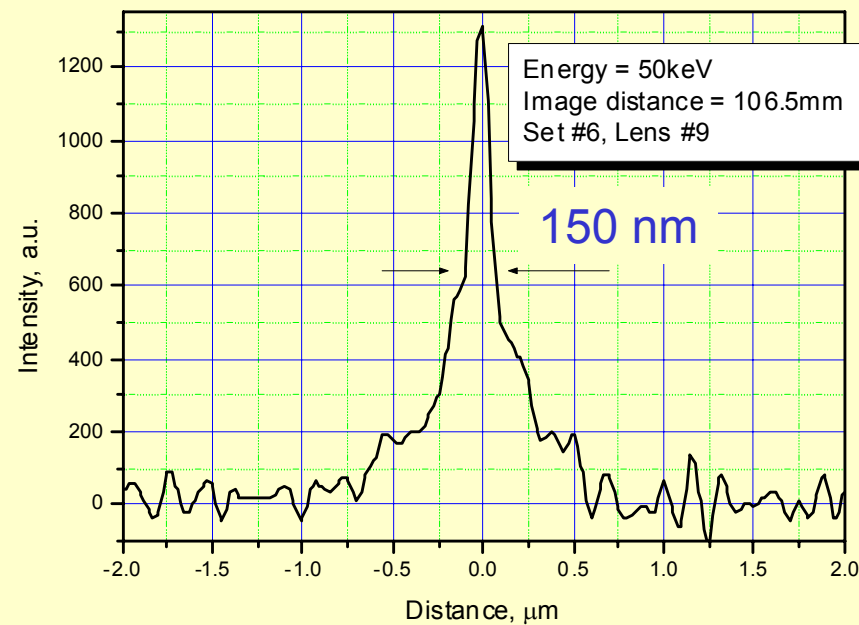
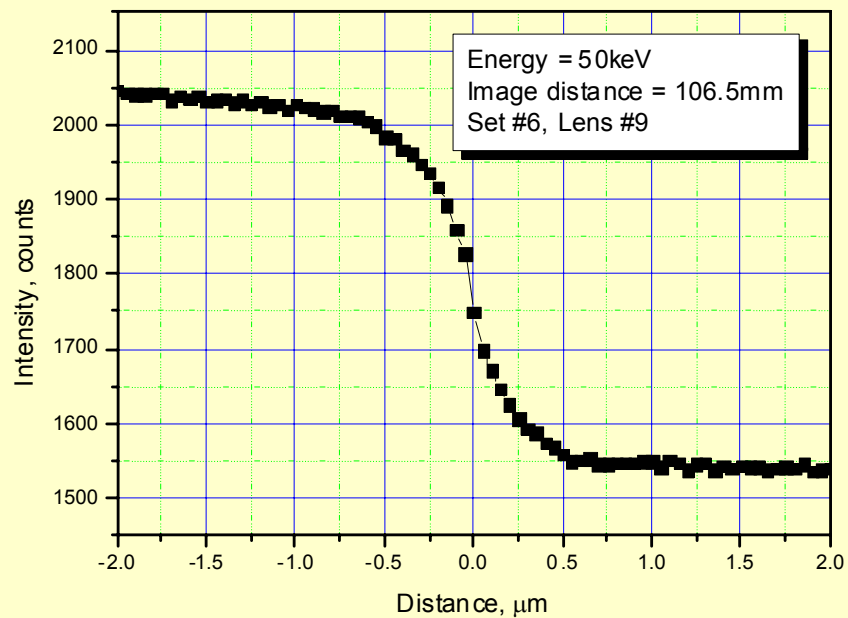
Test at ID15 in May 2006



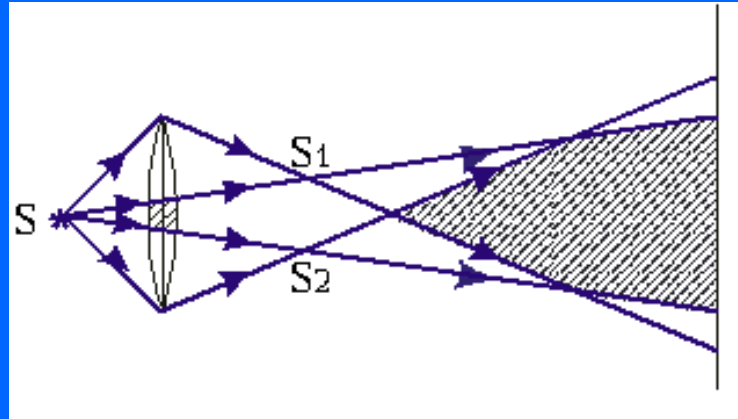
E = 40-80 keV

resolution 200-300 nm

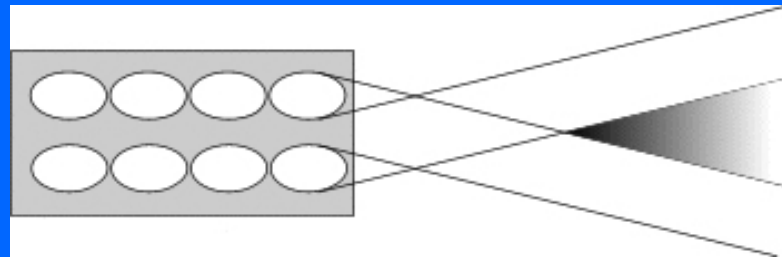
Best: 150 nm at 50 keV!



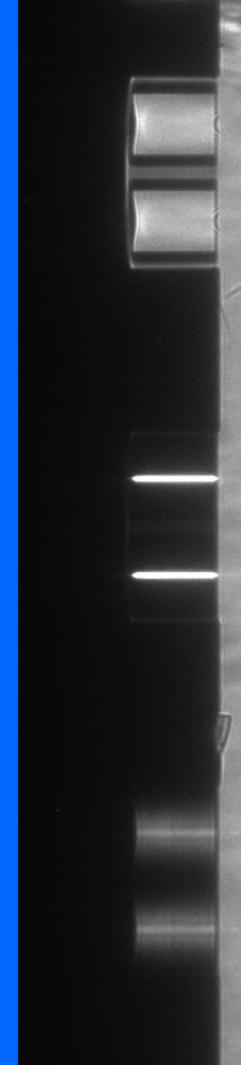
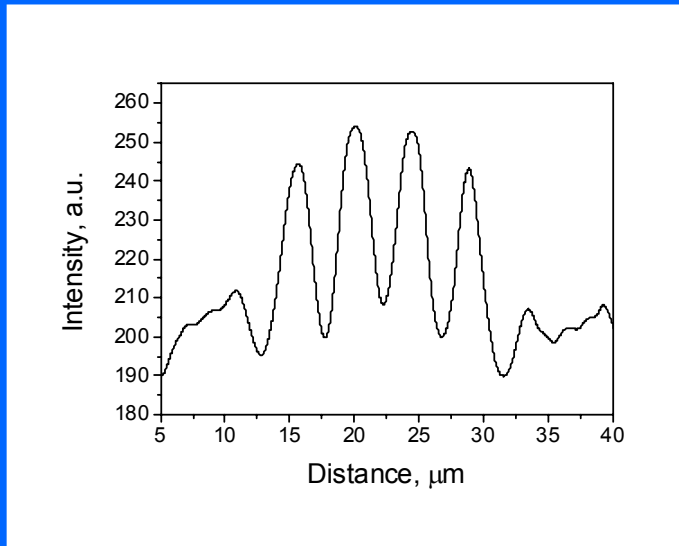
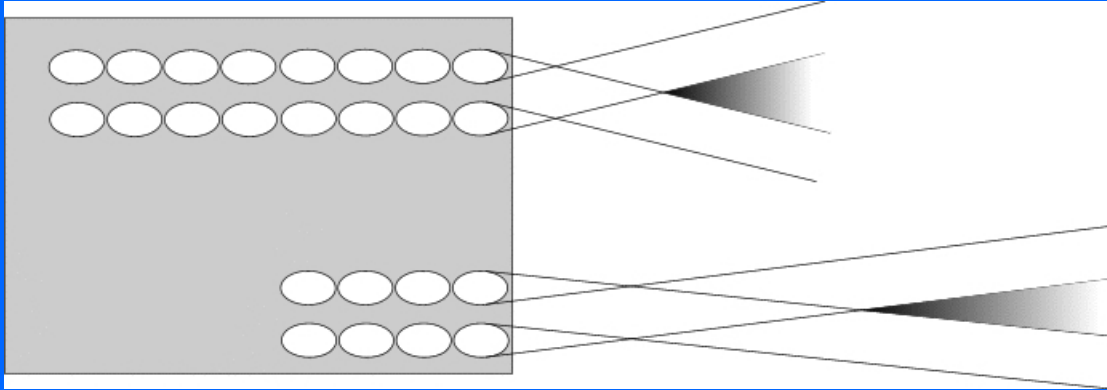
Bi-lens / Billet split lens



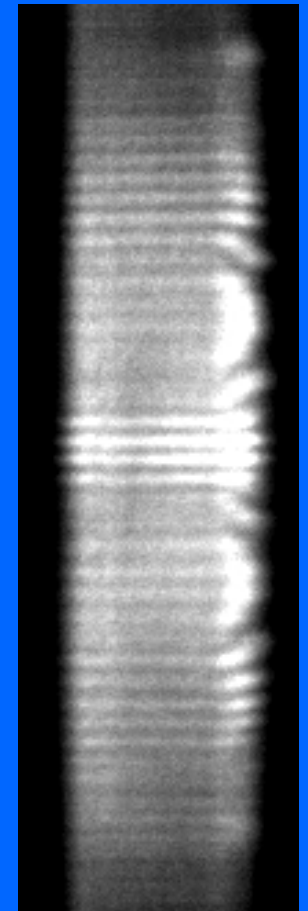
50 - 100 μm



Spatial coherence characterization MOTB/BM5



50 μm



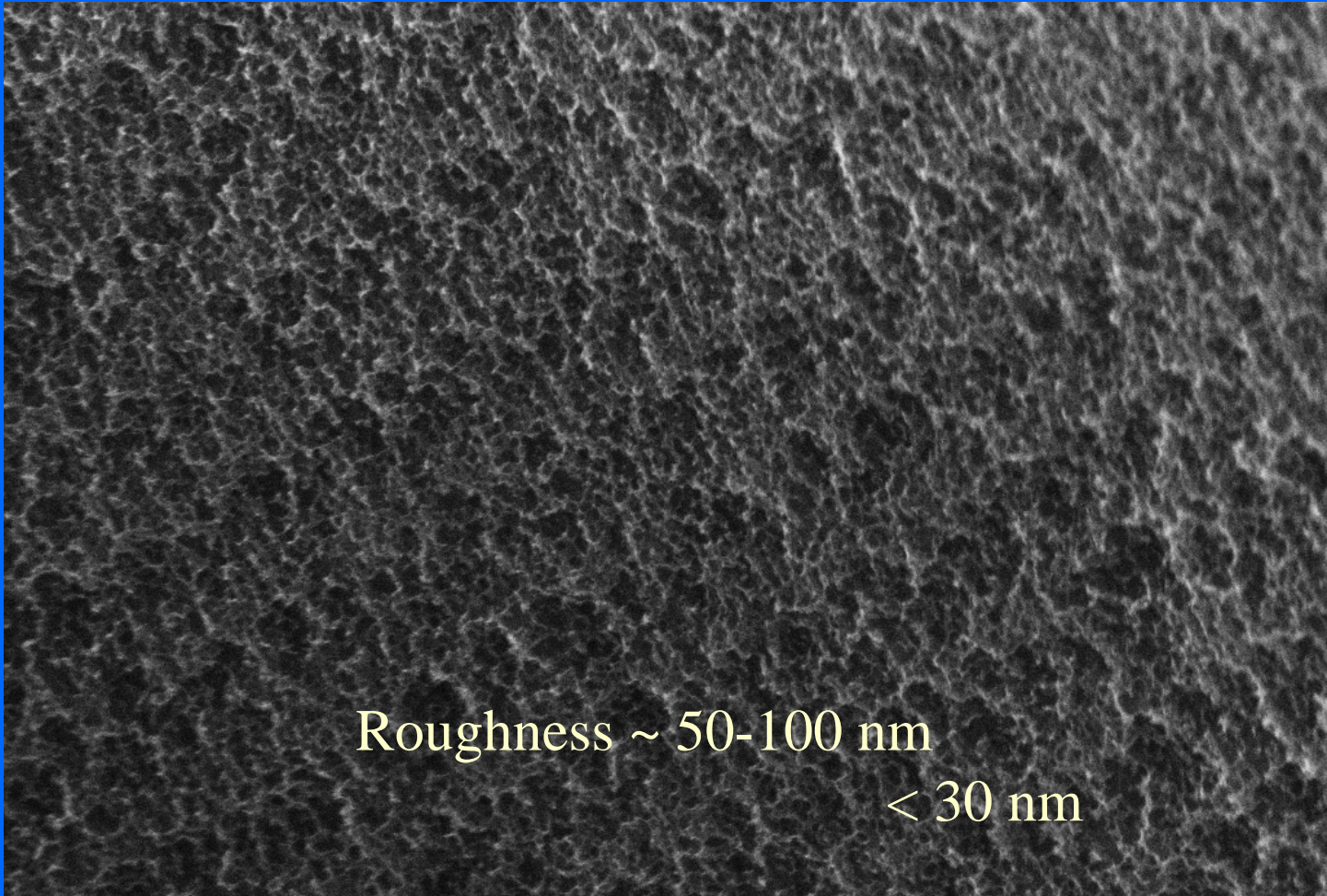
25 μm

$E = 13 \text{ keV}$

Effective source size $\sim 100 \mu\text{m}$

Applications

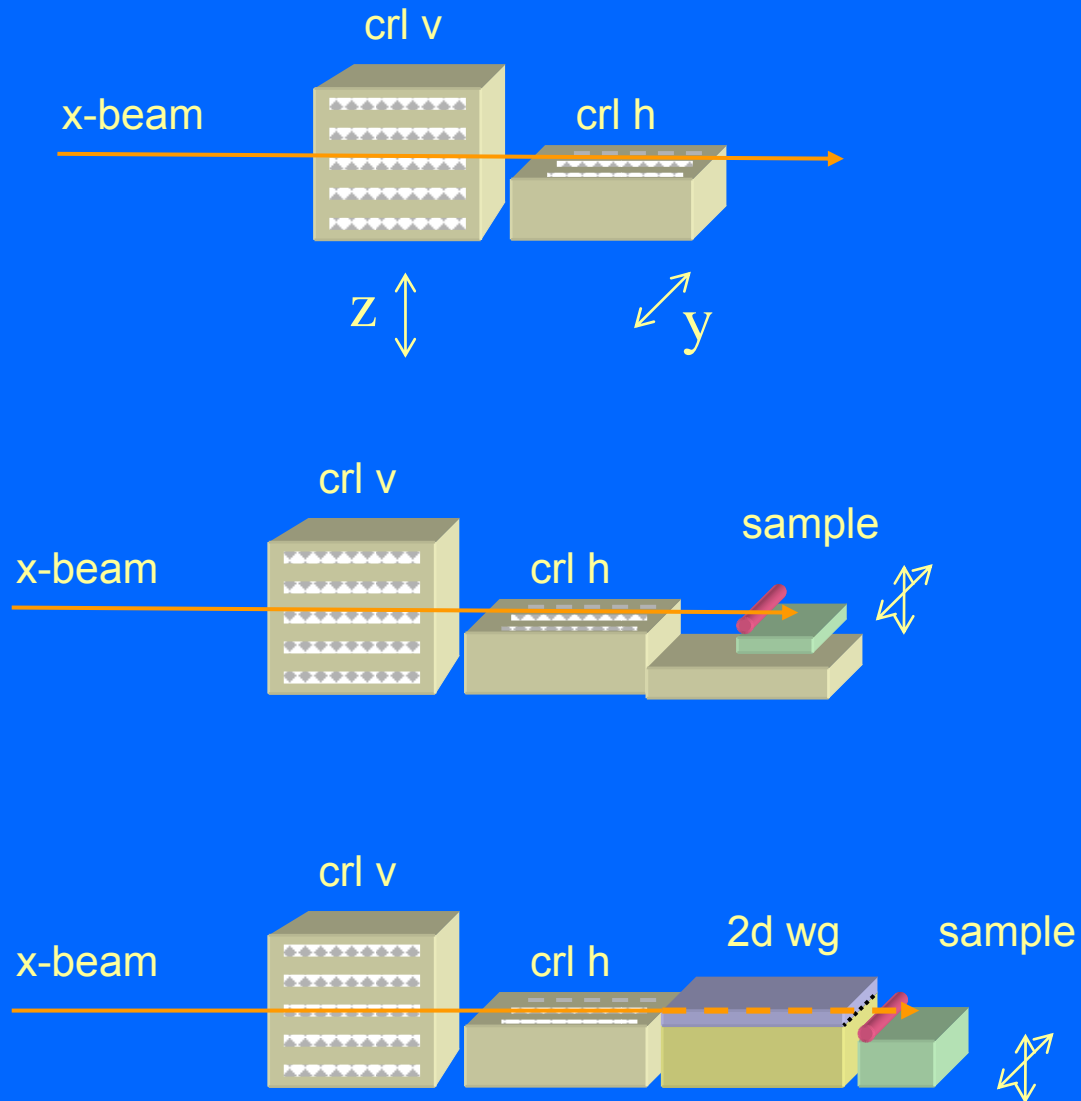
- High energy X-ray microscopy: diffraction, spectroscopy, imaging
- Beam collimation for high resolution diffraction ($< \mu\text{rad}$)
- Beam shaping elements / Wave front correction
- Interferometry
- Beam diagnostics
- Optics for X-ray Free Electron Lasers



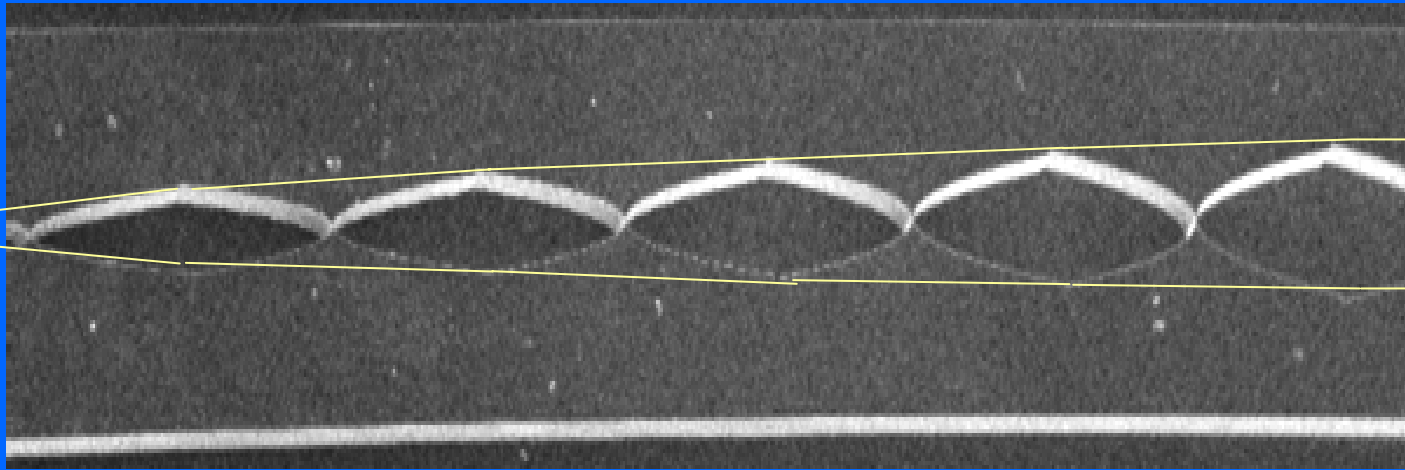
Roughness ~ 50-100 nm

< 30 nm

Integrated X-nanoprobe system



Planar parabolic lenses with scaled reduction of curvature radii



I. Snigireva, A. Snigirev, S. Kuznetsov, C. Rau, T. Weitkamp, L. Shabelnikov,
M. Grigoriev, V. Yunkin, M. Hoffmann, E. Voges,
"Refractive and diffractive optical elements", Proceedings of SPIE 4499, 64-74 (2001)

Number of lenses, N	Entrance radius	Aperture max.	Scaling factor, q	Exit radius
20	250 μm	500 μm	0.93	63 μm

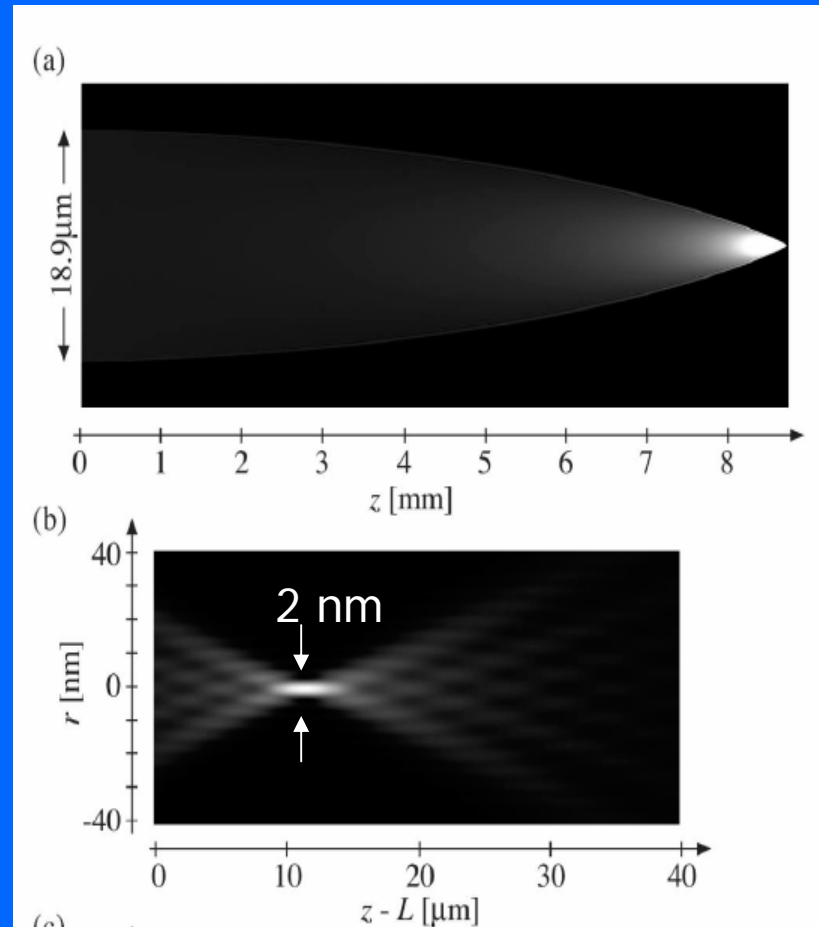
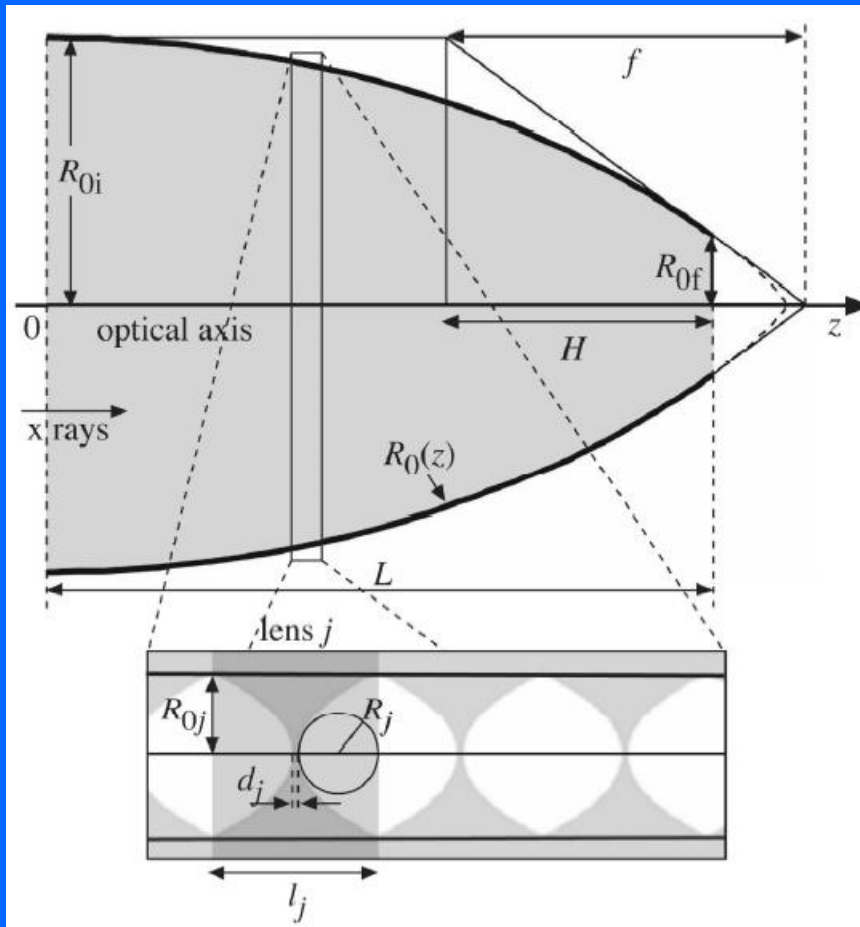
$E = 17.45 \text{ keV} / F = 25 \text{ cm}$

Focusing Hard X Rays to Nanometer Dimensions by Adiabatically Focusing Lenses

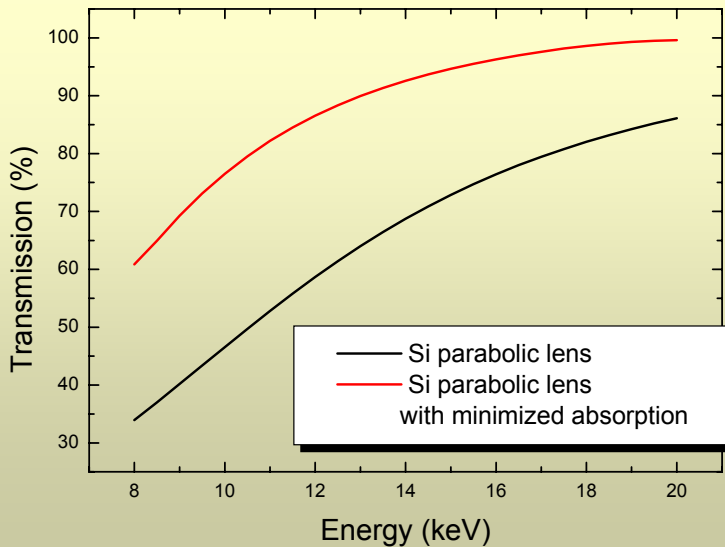
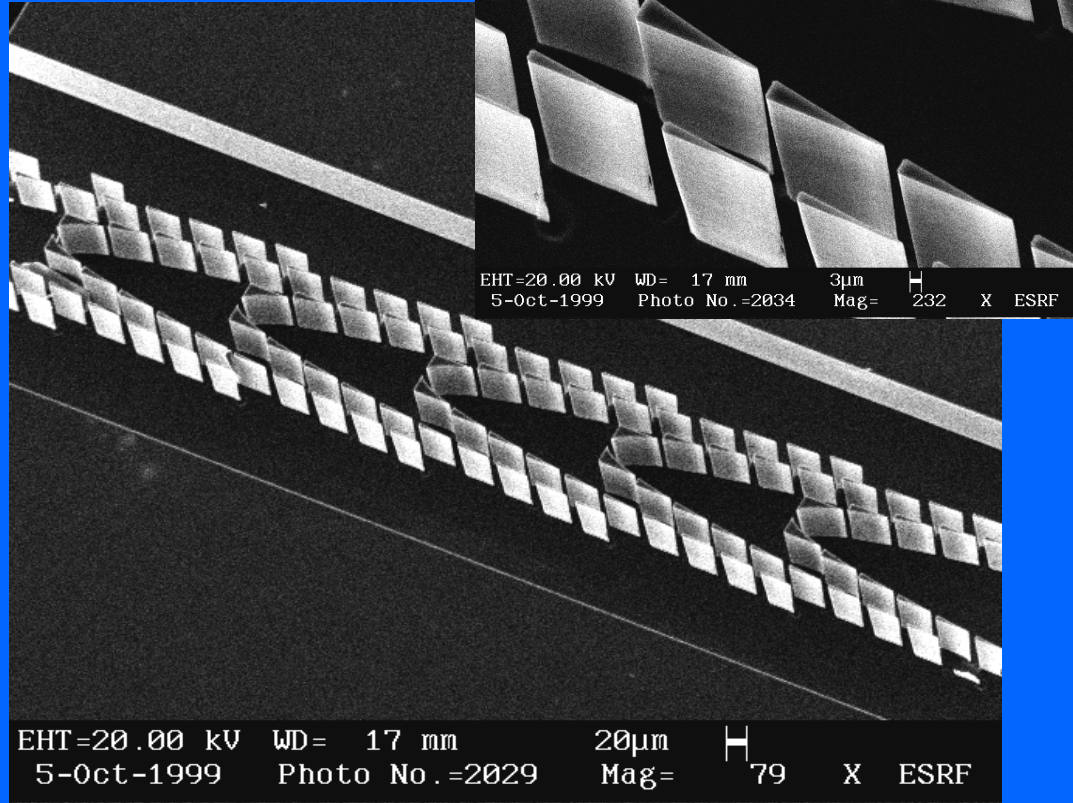
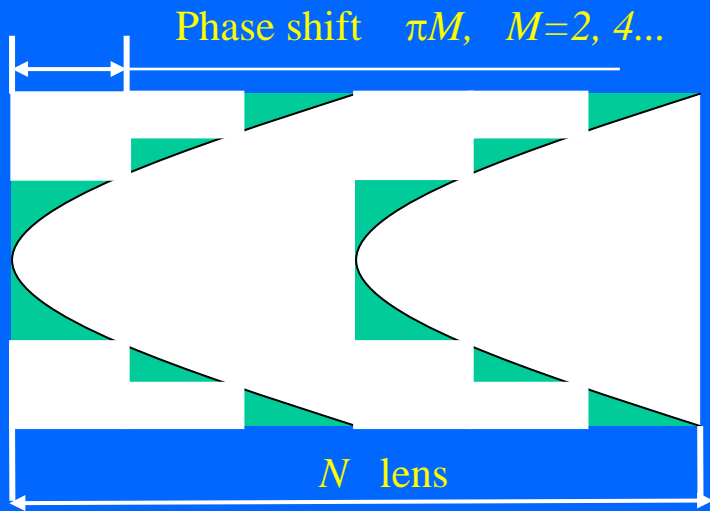
C. G. Schroer¹ and B. Lengeler²

¹HASYLAB at DESY, Notkestrasse 85, D-22607 Hamburg, Germany

²II. Physikalisches Institut, Aachen University, D-52056 Aachen, Germany



Si lens with minimized absorption



Aperture = 150 μm

Height = 100 μm

Number of lenses 5

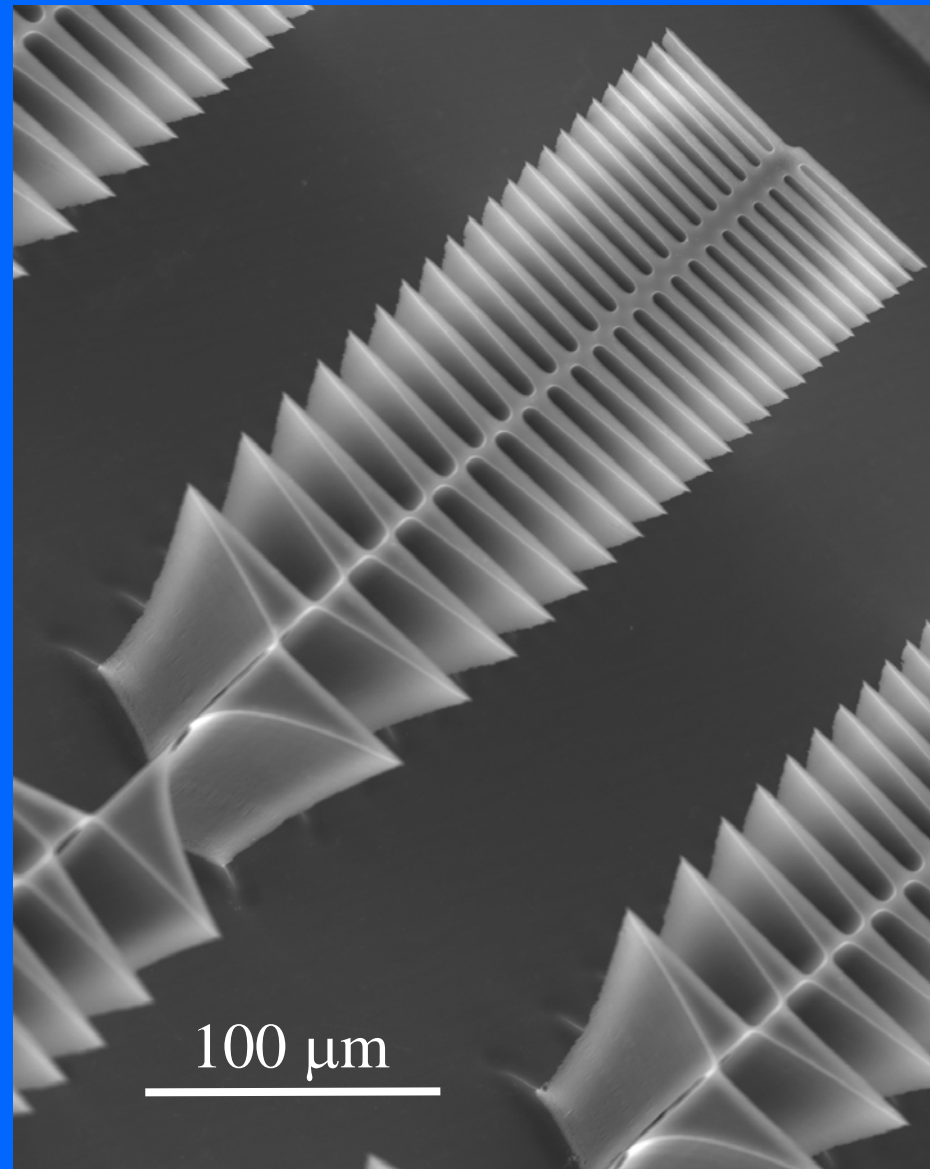
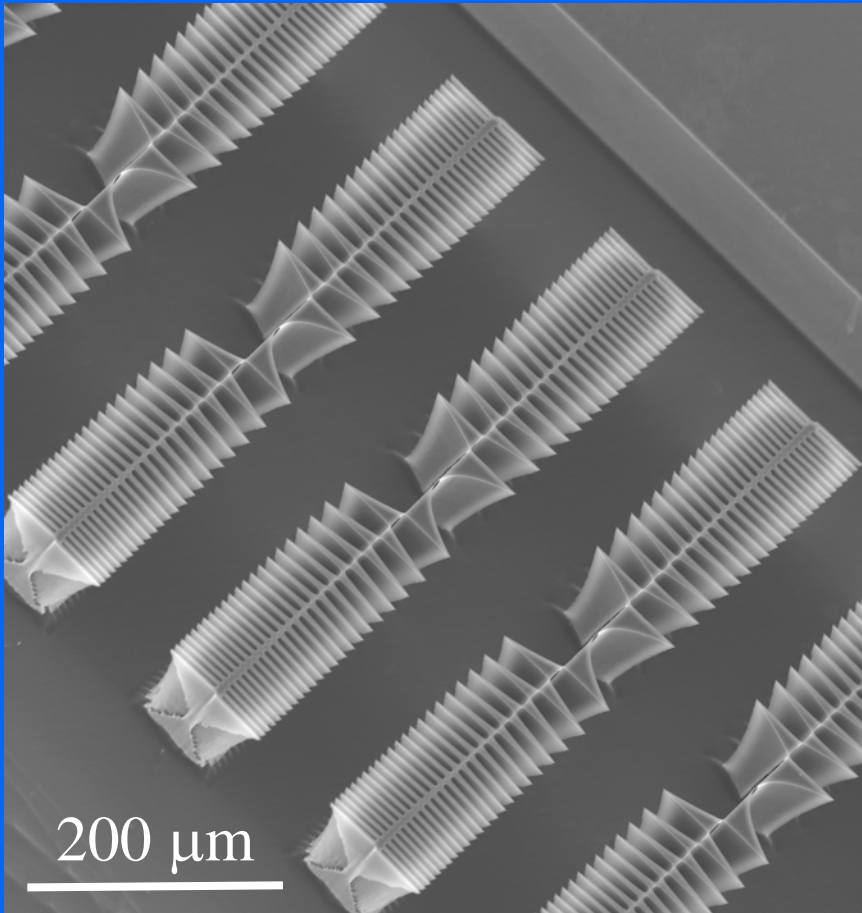
N of segment pairs 10

$$R_{\text{parabola apex}} = 12.72 \mu\text{m}$$

For $E = 17 \text{ keV}$

$F = 80 \text{ cm}$

“Fern”- like profile Si lens



$A = 505 \mu\text{m}$

20 lenses

$\Delta r_n = 2.8 \mu\text{m}$

$E = 17.48 \text{ keV}$

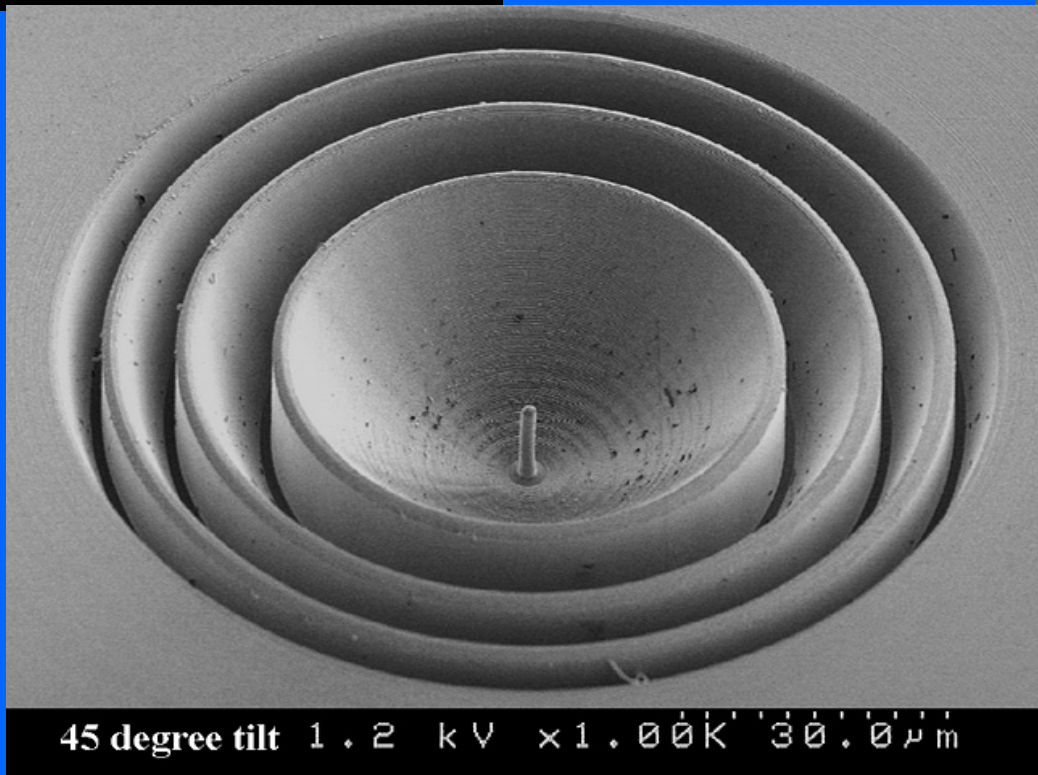
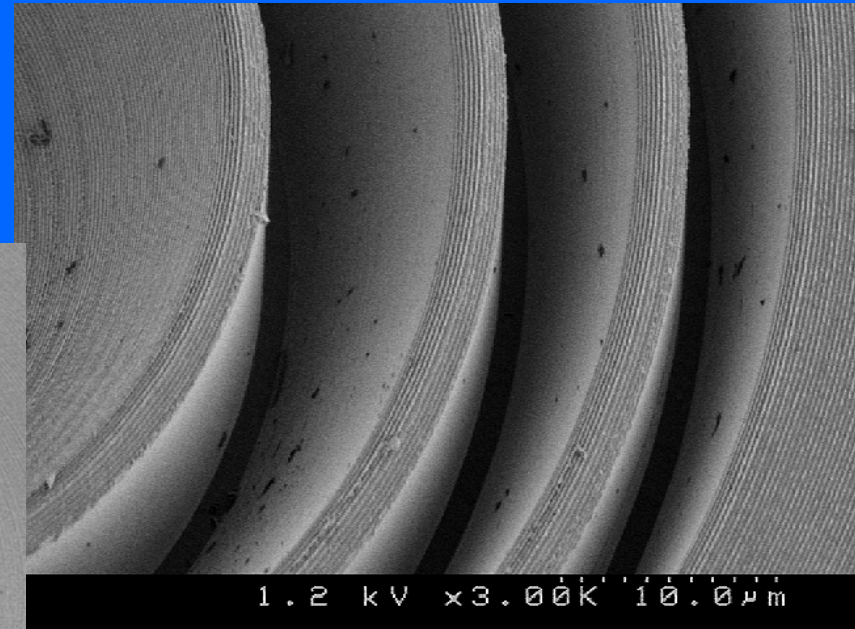
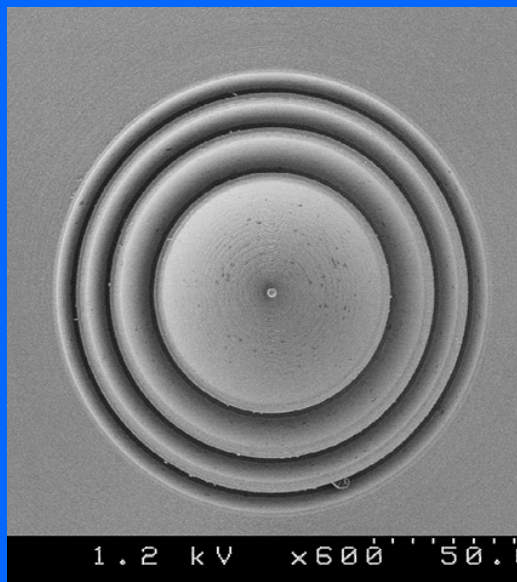
45 zones

2π phase shift

Refractive lens with kinoform profile (inline segments) has minimum total length but this design is complicated for realisation due to extremely wide range of feature width.

To narrow this range “fern”- like profile is proposed where even (or odd) segments are inverted

Prototype Focusing Element for the LCLS Warm Dense Matter Experiment



“blazed phase lens”
Diam. 100 μm
Al 79 μm
Groove height 18.7 μm
Designed for 8 keV

Bragg-Fresnel Optics

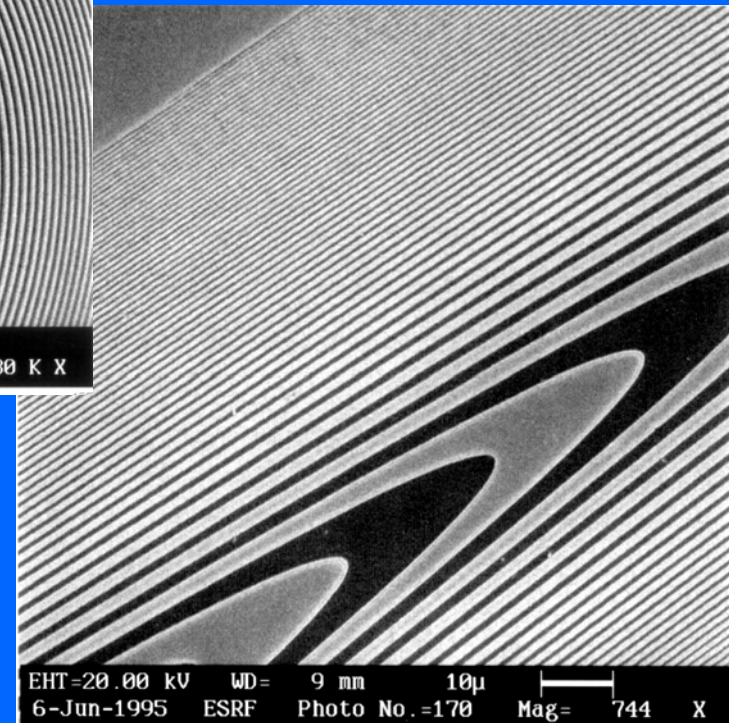
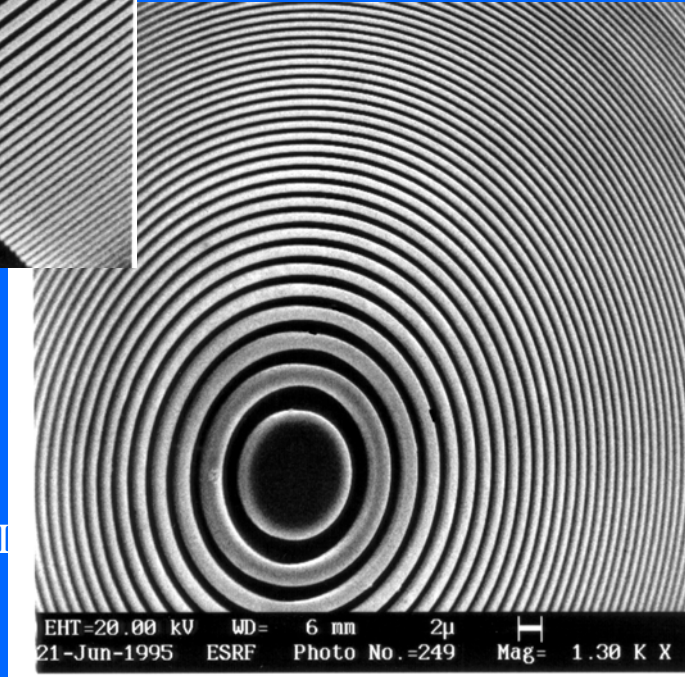
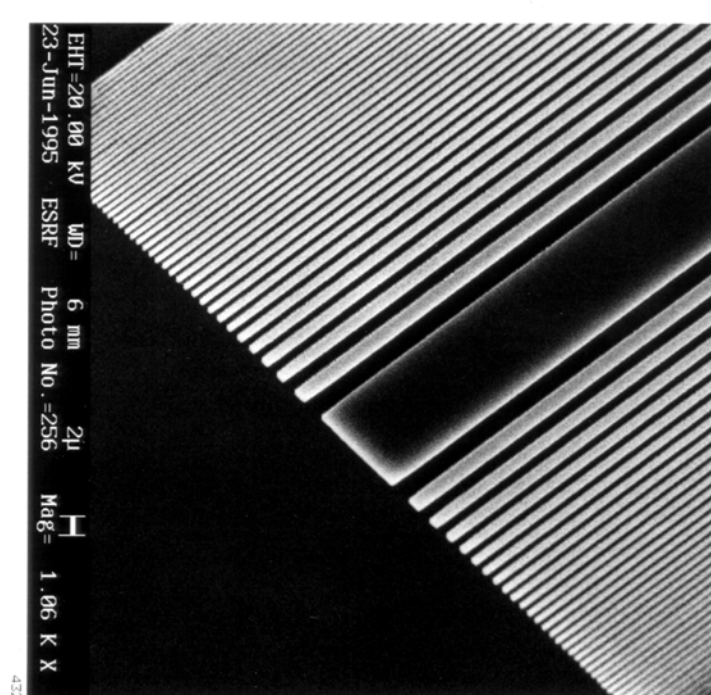
Bragg-Fresnel optics
based on

- Crystal
- Multilayer
- Photonic crystals

Linear BFL
Si (111)
 $A = 200 \mu\text{m}$
 $\Delta r_n = 0.3 \mu\text{m}$

Circular BFL
Ge (111)
 $A = 200 \mu\text{m}$
 $\Delta r_n = 0.3 \mu\text{m}$

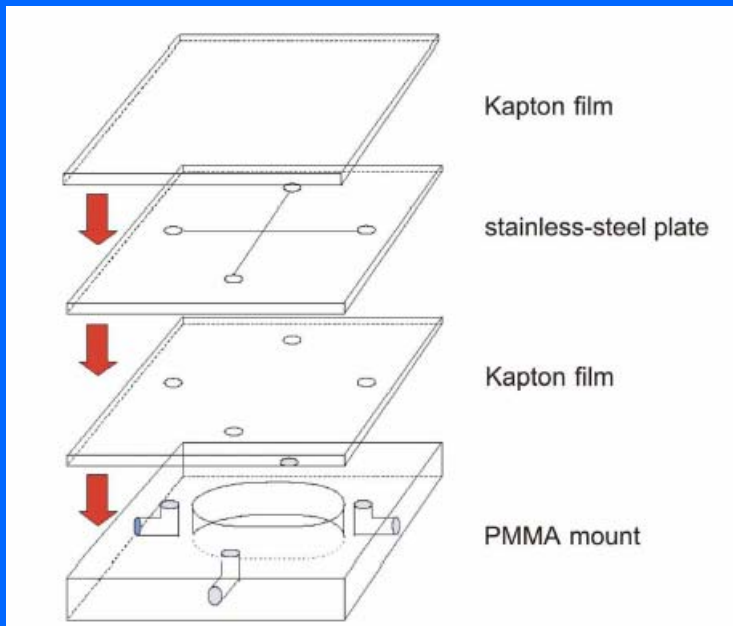
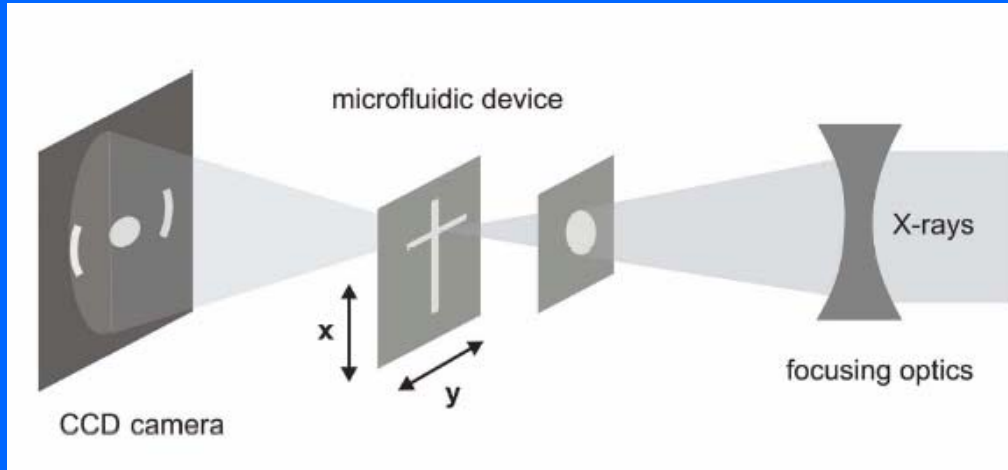
Multilayer BFL elliptical
W / Si, 56 periods
length = 18 mm
width = $136 \mu\text{m}$
 $\Delta r_n = 0.3 \mu\text{m}$



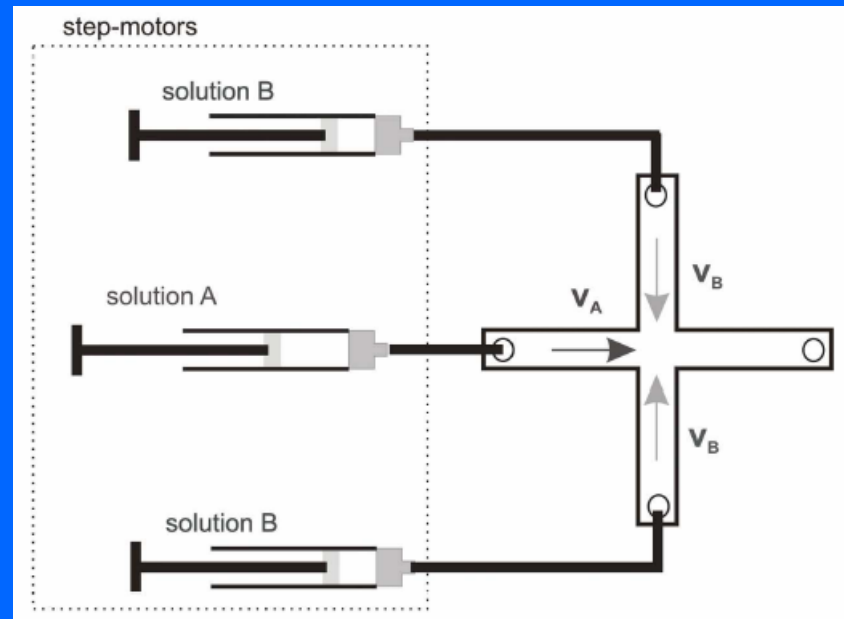
Microfluidics of soft matter investigated by small-angle X-ray scattering

Alexander Otten, Sarah Köster, Bernd Struth, Anatoly Snigirev and Thomas Pfohl

J. Synchrotron Rad. (2005). 12, 745–750

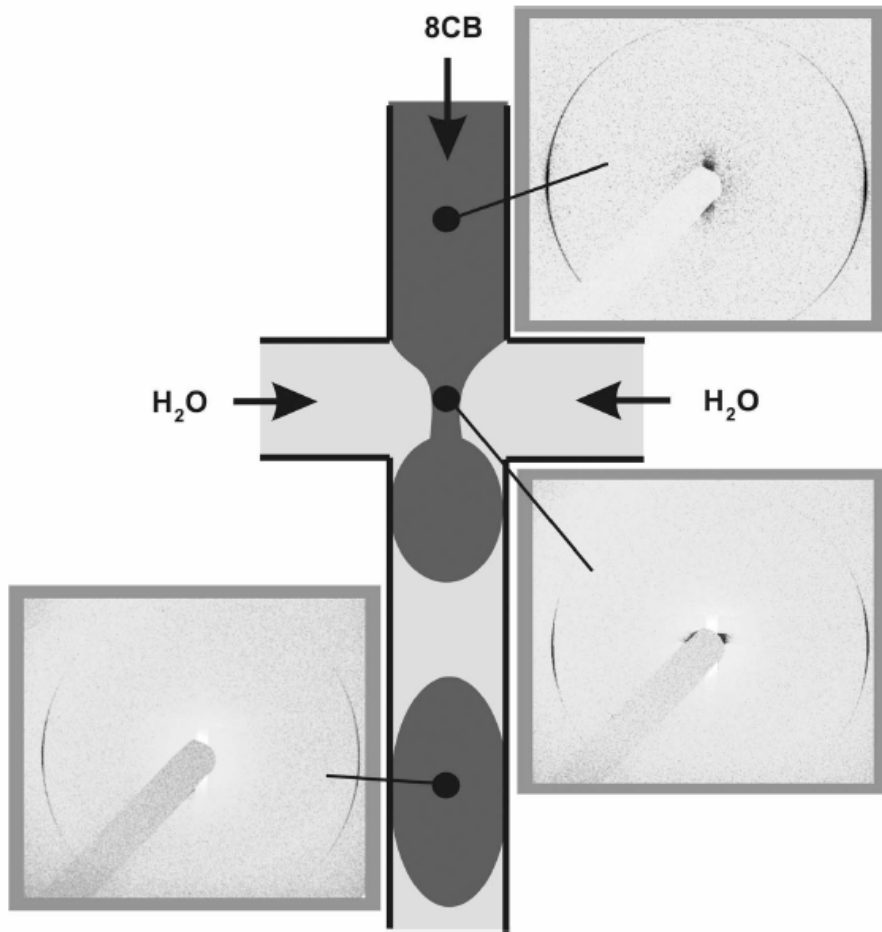


design of the microfluidic device

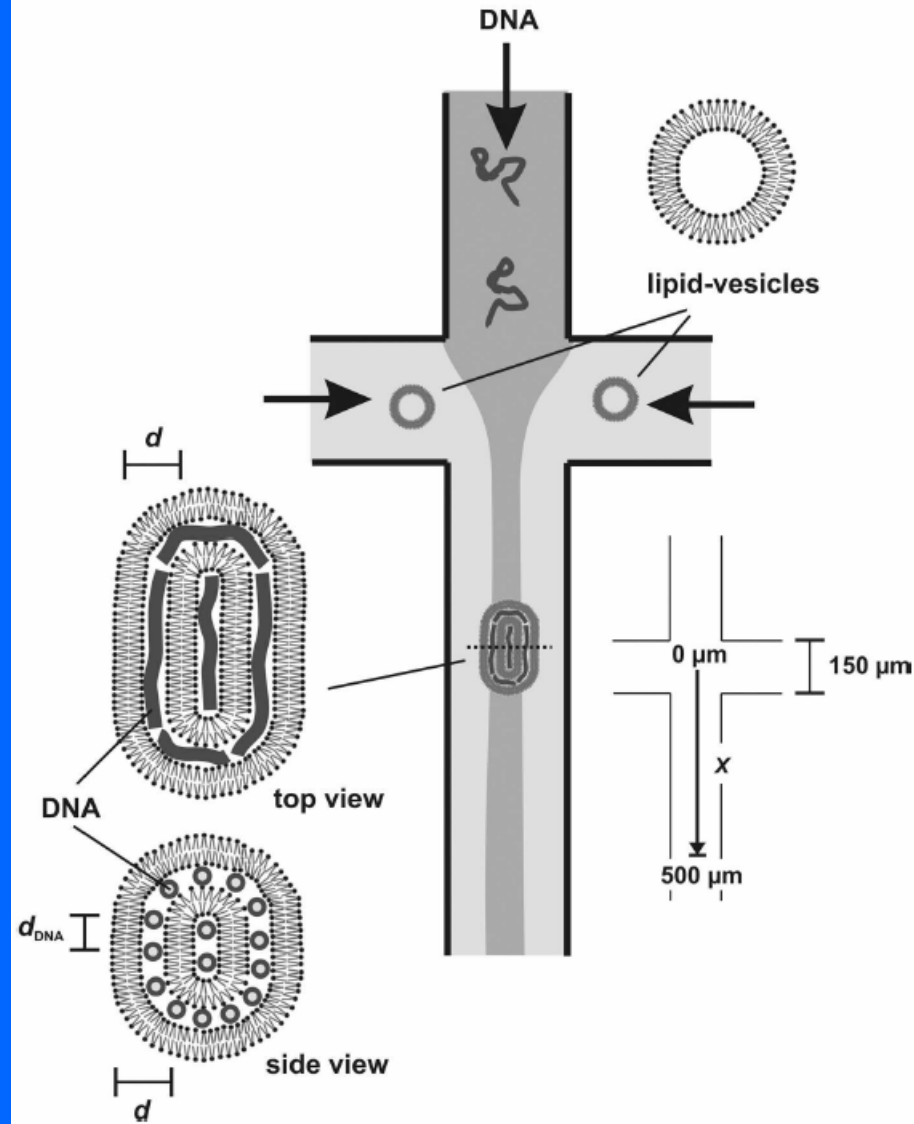


microfluidic pumping system.

Microfluidics: microbeam small-angle X-ray scattering

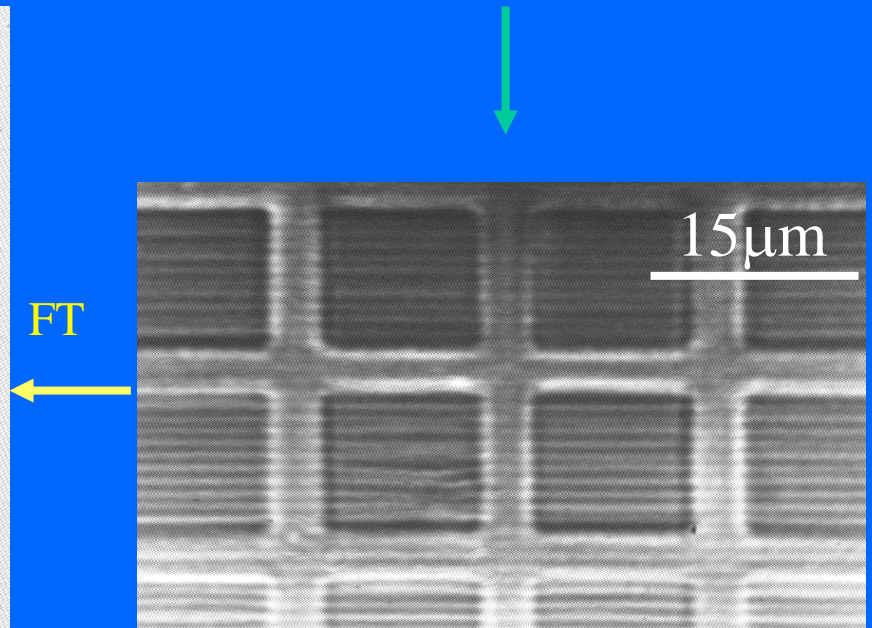
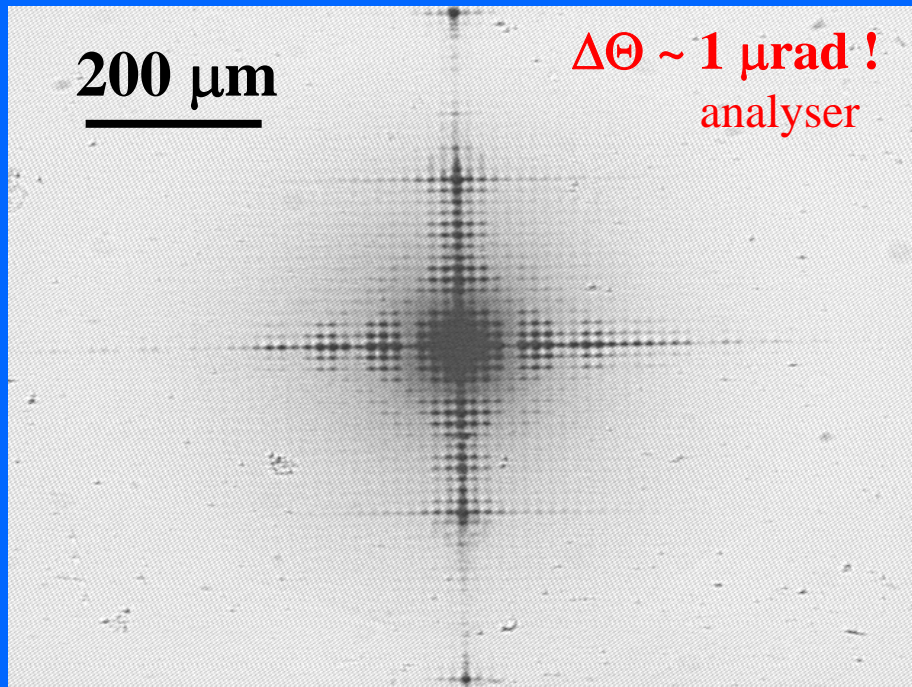
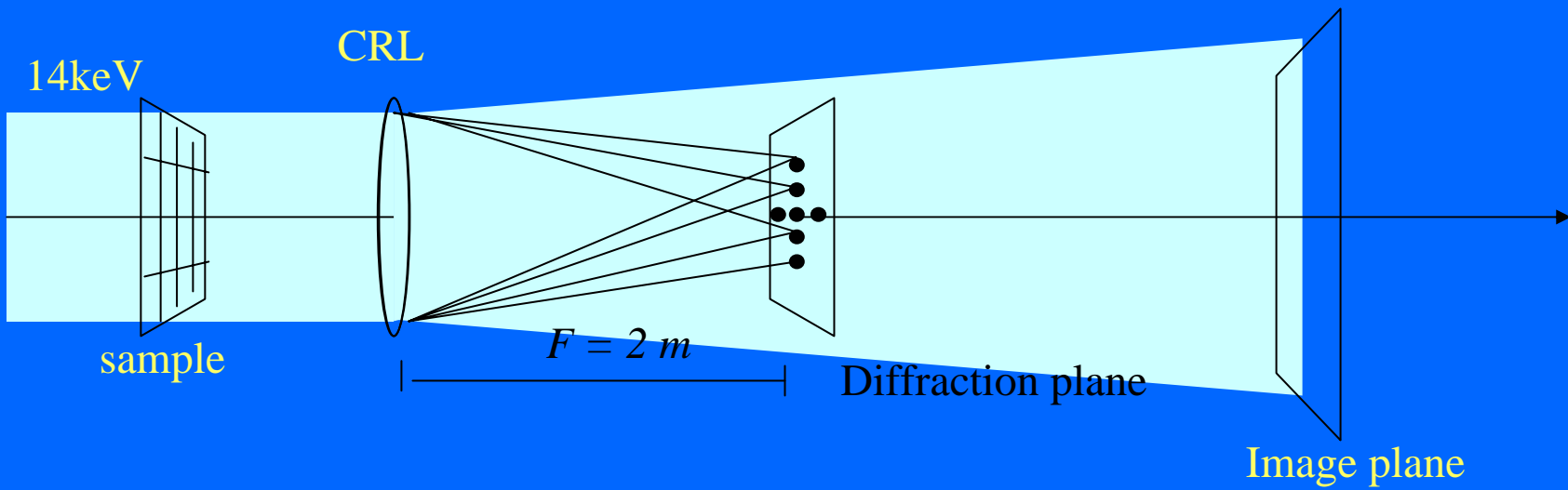


Schematic of the 8CB droplet formation with diffraction patterns observed at three different observation positions along the formation process.



Schematic of the self-assembling of DNA multilamellar membranes in a hydrodynamic focusing and mixing device.

Fourier Transform Diffraction/Imaging



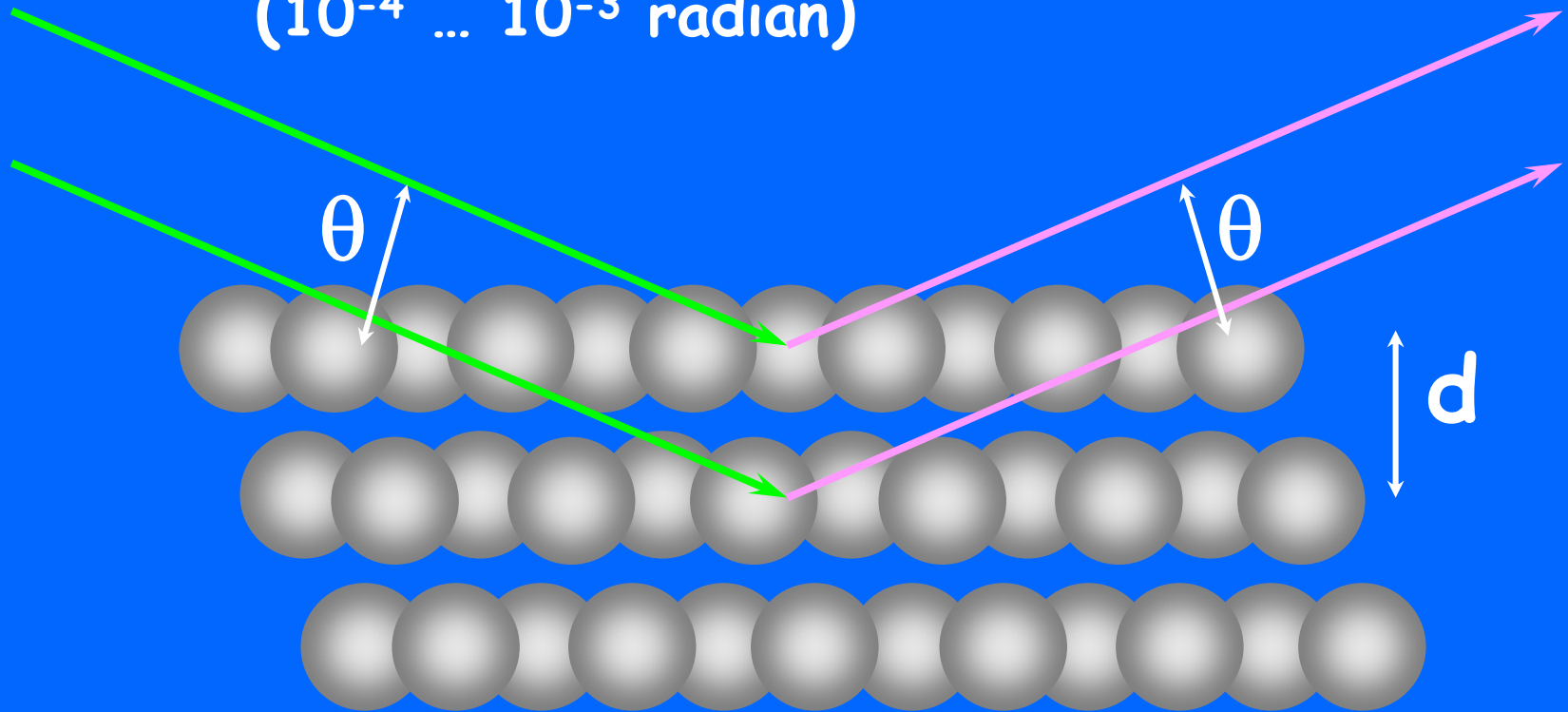
Theory: the Bragg law

Ordinary (atomic) crystals: $d \sim \lambda$
=> large diffraction angle 2θ

X-rays: $\lambda \sim 1 \text{ \AA}$

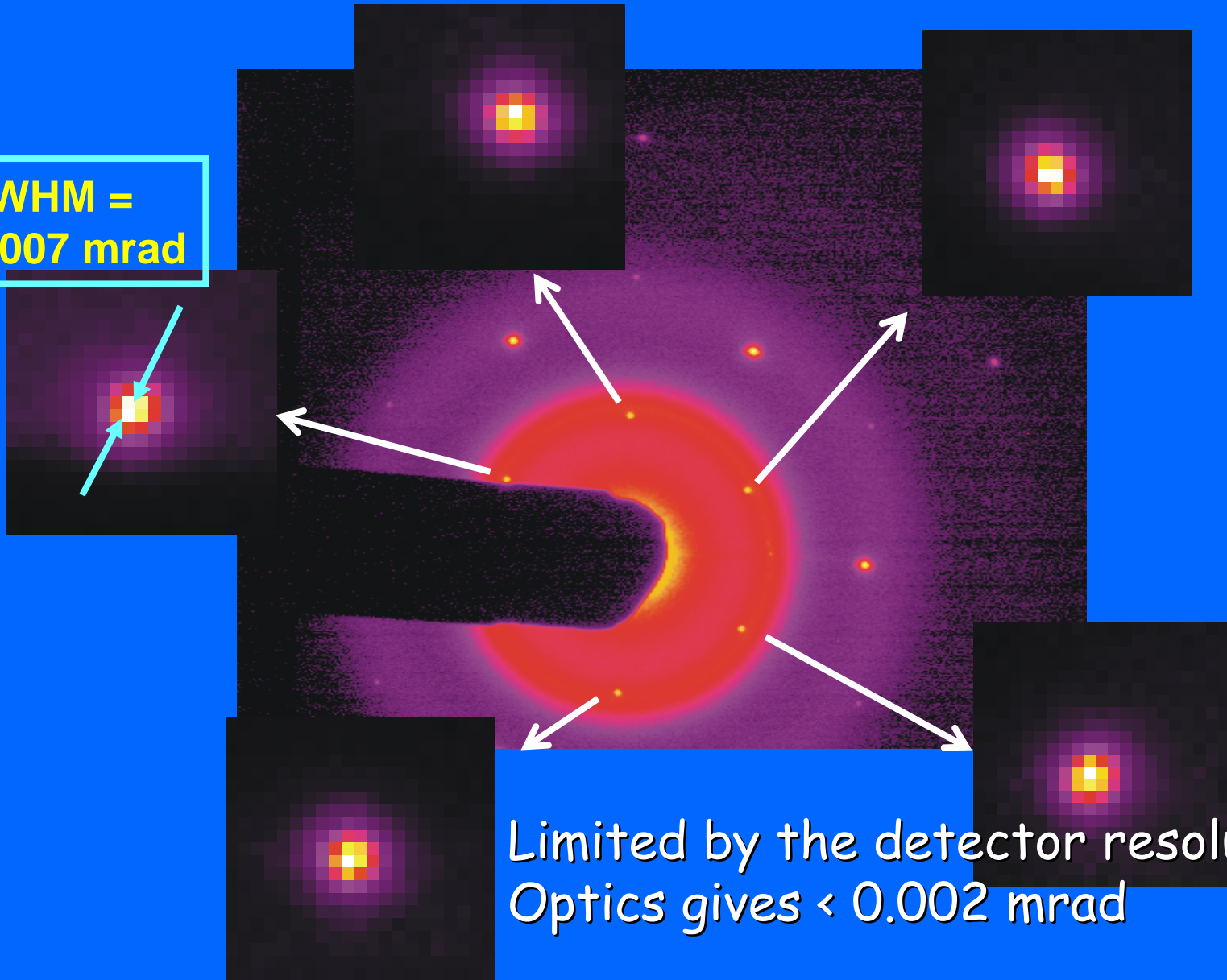
Colloidal crystals: $d \gg \lambda$
=> small diffraction angle 2θ
($10^{-4} \dots 10^{-3}$ radian)

$$\sin\theta = n\lambda/2d;$$
$$n=1,2,\dots$$



Latest news:

FWHM =
0.007 mrad



Limited by the detector resolution;
Optics gives < 0.002 mrad

SOI technology – strained Si - charge carrier mobility

Needs:

- Local strain analysis
- Depth structure analysis of dislocations
resolutionn < 10 nm !

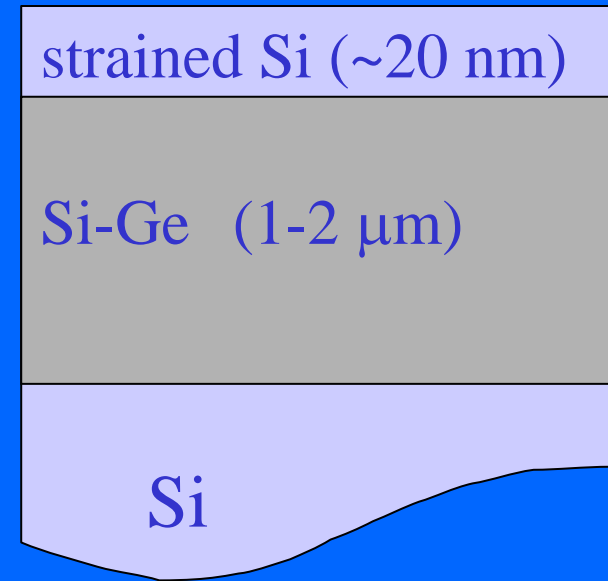
wafer level → transistor level

TEM: converging e-beam diffraction
problems:

- does not see dislocation density 10^4
- sample preparation
thin sample – relaxations!

X –ray diffraction microscopy

converging coherent x-ray beam diffraction ?



The first experiments with ERL will very quickly develop new classes of experiments as they gain experience with their unique source properties