



ERL Wake Fields and One Possible Recovery Technique

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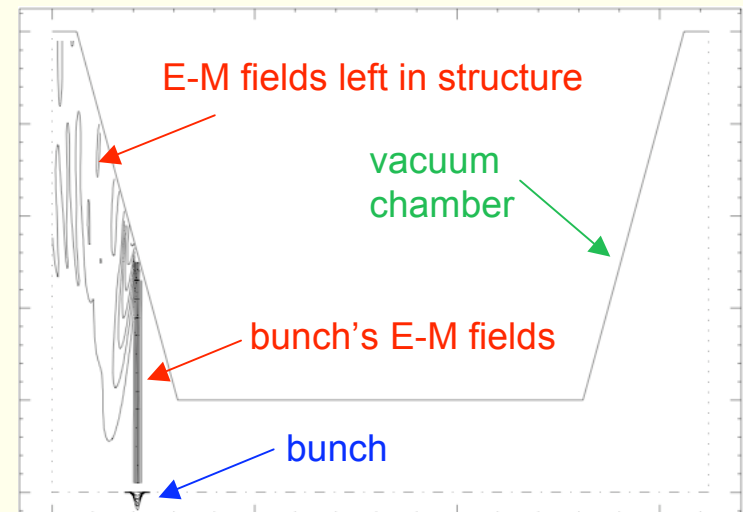
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Electromagnetic Self-Interaction of Beam: Wake Function

- Self-Wake Field

- Direct interaction of the bunch with vacuum chamber

- E-M fields of bunch couple to stationary E-M modes in the vacuum chamber structure. These are associated with discontinuities in the chamber's cross-section
 - In a smooth chamber, E-M fields travel unperturbed with the bunch, but when the chamber shape changes some field-lines get “disconnected” from the charges in the bunch
 - Strongest fields occur within the bunch since all of the different modes of the structure are excited “in phase”



Wake Voltage

- Beam-Chamber Interaction Can Written as an Induced Wake Voltage

- Voltage for particle following charge, q depends on its longitudinal position, s , within the bunch - due to the effect of all vacuum chamber components in ERL

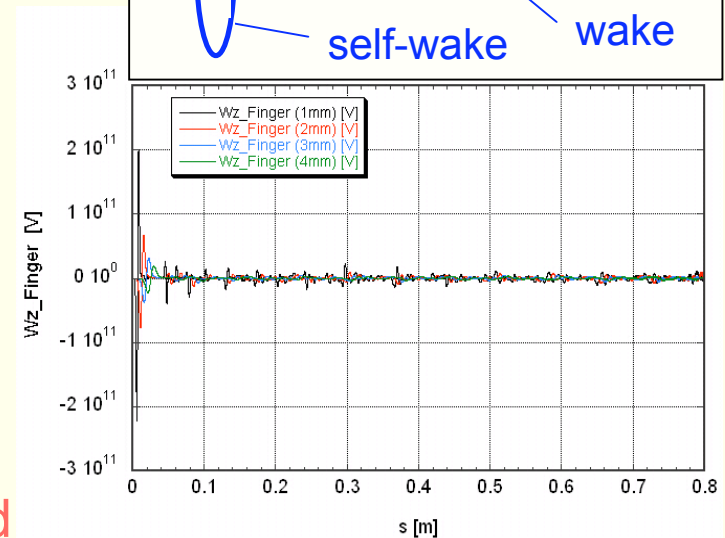
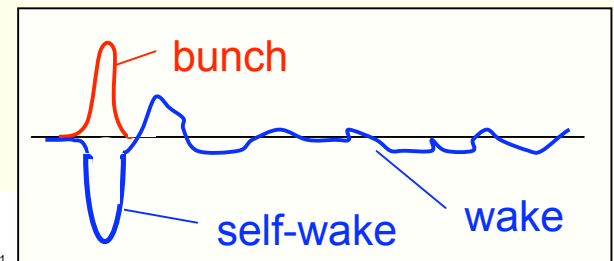
$$V_{\parallel}(s)\Big|_{\text{entire ERL}} = q W_{\parallel}(s)\Big|_{\text{entire ERL}}$$

- Increases the energy spread, ΔE , of the bunch

- Limitation:

- ERL accelerates beam to 5 GeV & the energy spread is usually not serious,
- BUT as the beam decelerates to 10 MeV, the effect is magnified x 500
- Maximum acceptable beam energy spread at the dump places a limit on the maximum wake field, i.e.

$$\max\left\{eV_{\parallel}(s)\Big|_{\text{entire ERL}}\right\} \leq \kappa \max\left\{\Delta E\Big|_{\text{dump}}\right\}$$



where $0 \leq \kappa \leq 1$
(e.g. $\kappa \sim 0.5$)

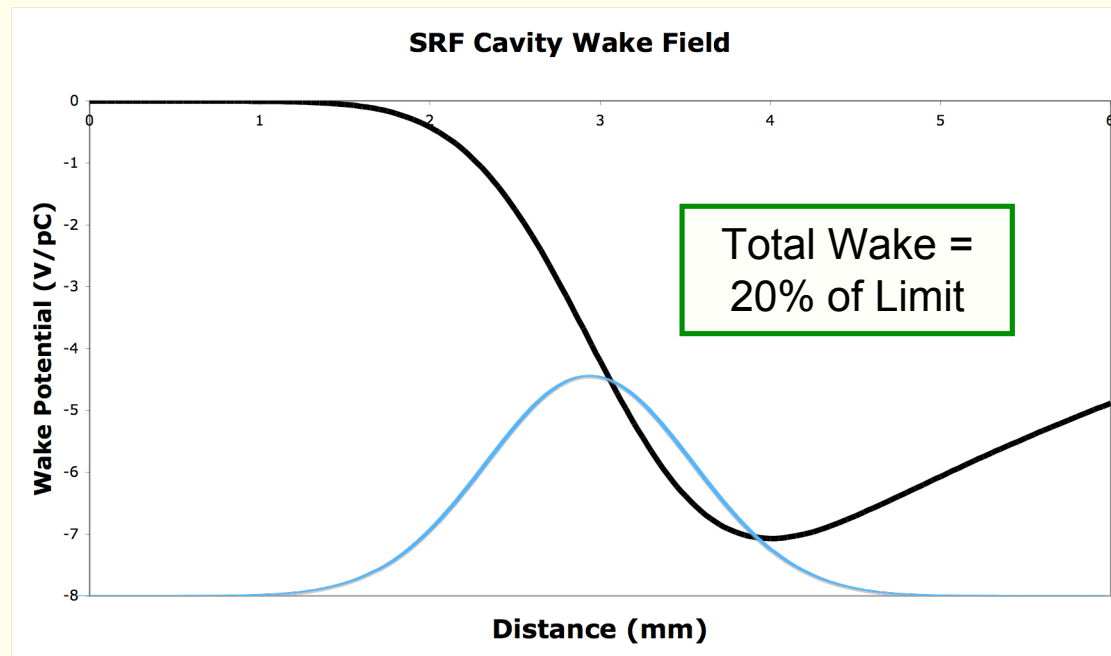
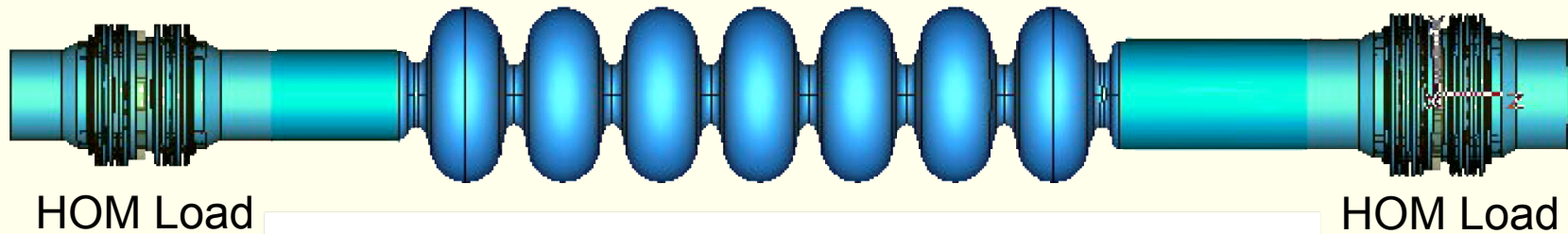
Peak Wake Function Limit

- Estimating maximum energy spread at the dump
 - Decelerated beam at the Dump:
 - Average Beam Energy at the Dump: $E = 10 \text{ MeV}$
 - Acceptable Maximum Energy Spread at the Dump: $\Delta E = 5 \text{ MeV}$
- Cast limit in terms of wake field W_{\parallel}
- Limit depends on operating charge:
 - ERL operation (77 pC & $\sigma_z = 0.6 \text{ mm}$):

$$\begin{aligned} \max\left\{W_{\parallel}(s)\Big|_{\text{entire ERL}}\right\} &= \frac{1}{q} \max\left\{eV_{\parallel}(s)\Big|_{\text{entire ERL}}\right\} \\ &\leq 0.5 \frac{1}{q} \max\left\{\Delta E\Big|_{\text{dump}}\right\} \approx (0.5) \frac{5 \text{ MeV}}{77 \text{ pC}} \\ &\approx \boxed{32 \text{ kV/pC}} \end{aligned}$$

One Example of Self-Wake Functions

- Linac accelerator RF cavities
 - 7 cells (scaled from the 9 cell Tesla cavities)
 - Min, Max $\{W_{\parallel}\} = -8.1, 0.0$ V/pC $k_{\text{HOM}} = 7.3$ V/pC
 - Quantity = 400 (x 2 for the two passes thru the RF)

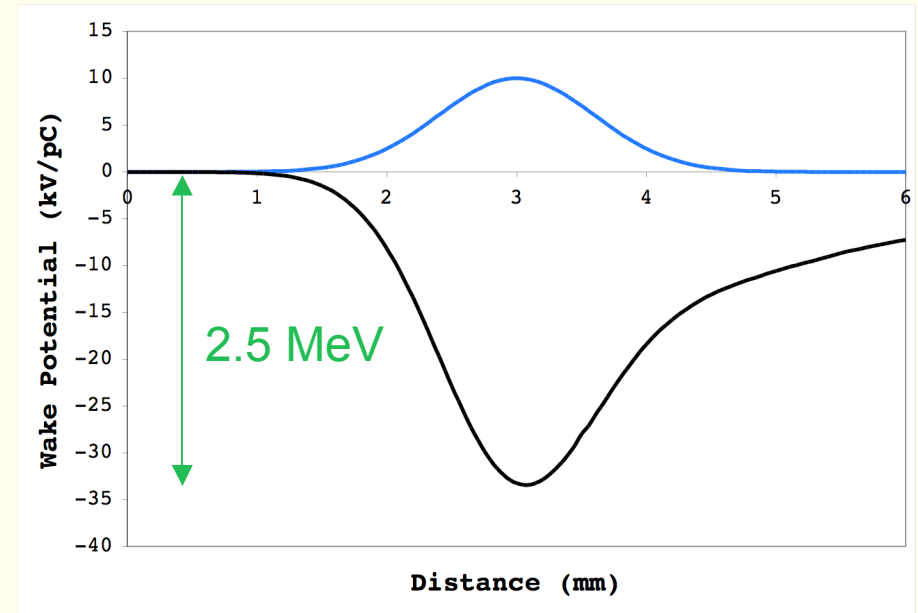


Estimated Total Self-Wake

- Peak Wake

$$\max\{W_{\parallel}(t)|_{\text{ERL}}\} = 33 \text{ kV/pC}$$

Same as 32 kV/pC Limit



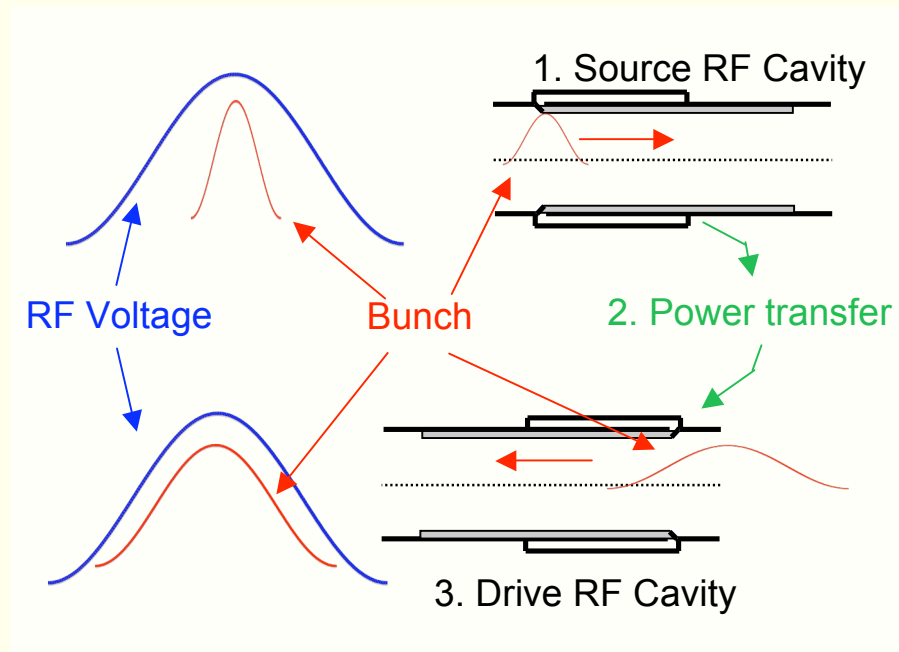
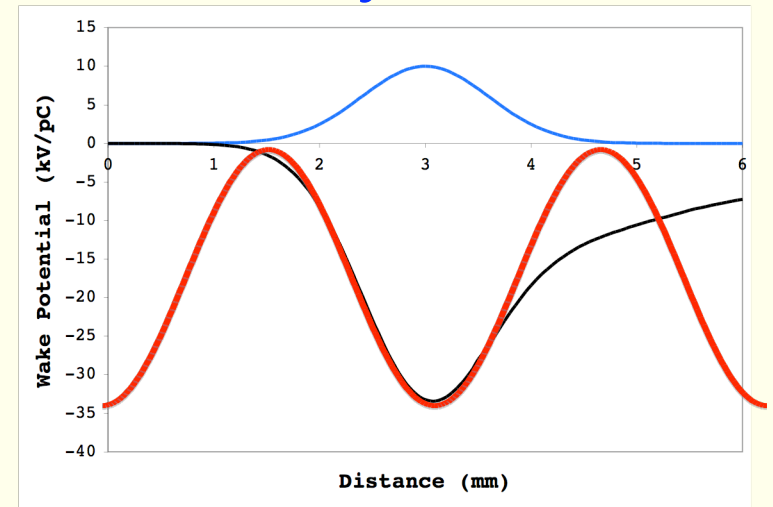
Component	Number	Total -Wake (KV/pC)	Total +Wake (KV/pC)	Total k (KV/pC)
7 Cell RF Cavity	800	-5.66	0	5.81
HOM Load (78 mm)	400	-0.89	0	0.64
HOM Load (106 mm)	400	-0.50	0	0.36
Expansion Joint	356	-0.74	0.10	0.53
BPM (Button)	664	-0.35	0	0.24
BPM (Stripline)	20	-0.01	0	0.01
Flange Joint	356	-0.90	0	0.64
Clearing Electrode	150	-0.18	0.14	0.04
Gate Valve	68	-0.71	0.69	0.42
Resistive Wall (12.7 mm)	2500	-4.00	0	2.75
Roughness (12.7 mm)	2500	-14.00	0.50	8.75
Undulator Taper (3 mm)	18	-0.61	0.37	0.36
Resistive Wall (3 mm)	144	-0.98	0	0.69
Roughness (3 mm)	144	-3.60	0.12	2.52

Total k
= 23.8KV/pC

Total HOM Power
= 183 KW

Possible Wake Field Correction

- Correcting curvature is hardest - use very High Frequency RF system
 - Good idea, but no large power sources are available
 - Use beam as the power source



1. Use a short bunch to resonantly excite the Source RF Cavity (less curvature)
2. Extract RF power to
3. Excite the Drive RF Cavity, which re-accelerates a longer bunch (more curvature)

Tasks for the Summer

- Recalculate the Wake Fields
 - The bunch length has increased

$$\sigma_z = 0.6 \text{ mm} \implies \sigma_z = 1 \text{ mm}$$

This changes (largely reduces) the Wake Field shape

- Test Different RF Structure Designs
 - Model the cavities
 - Look into technical details