



Cornell University

**LEPP REU**  
**ERL Wake Fields (Wakefields?) and**  
**Methods for Their Reduction**

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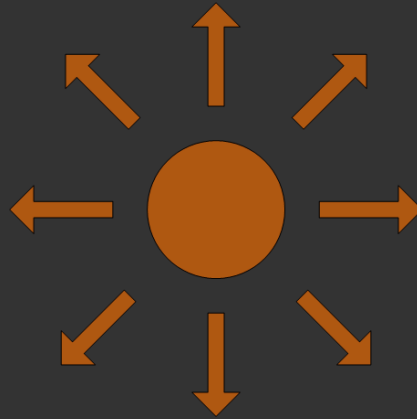
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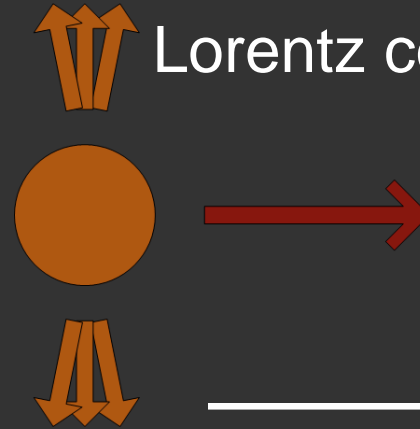
# Overview of Wake Dynamics

Stationary charge:

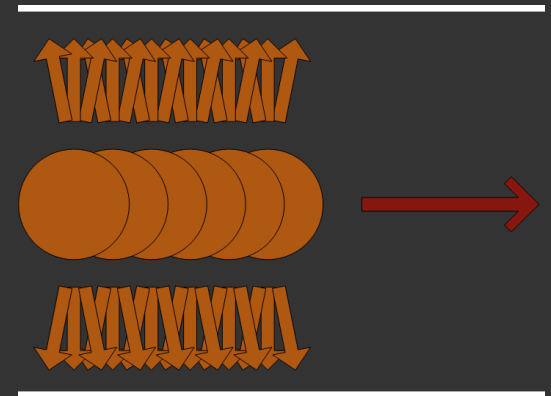


Field lines experience  
Lorentz contraction

Moving charge:



Charges (bunch) in a pipe:

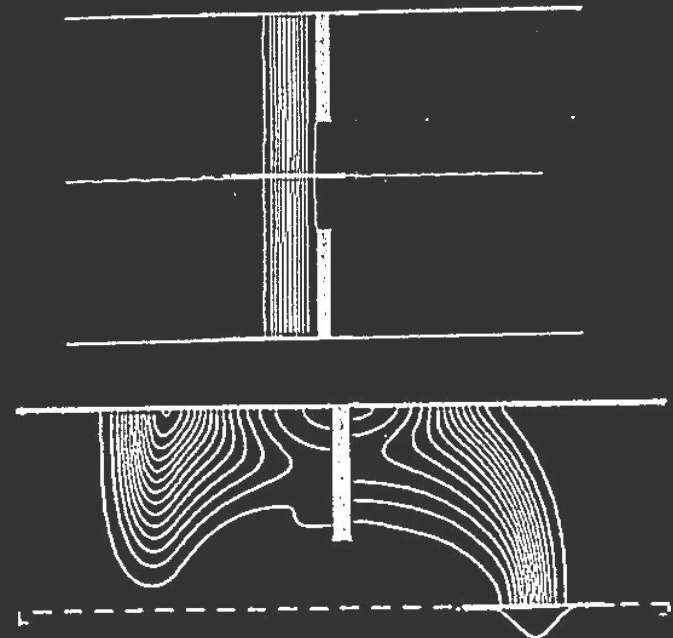
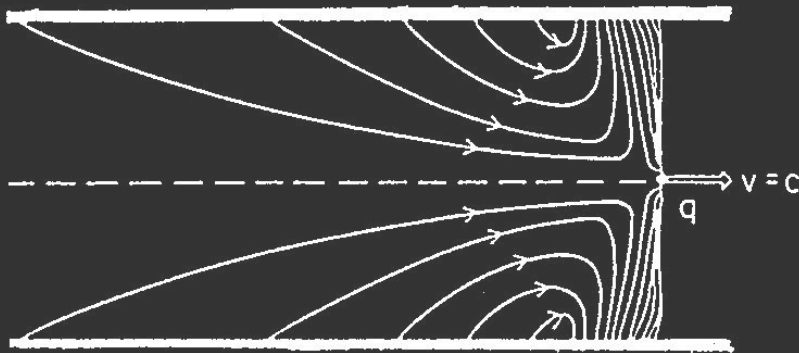


Currents induced  
in pipe wall



## Where do wakes come from?

- Geometrical non-uniformities (dominant effect: thousands of kV/m)
- Dielectric coatings on pipe wall ( $\sim 500$  kV/m)
- Finite conductivity in pipe wall ( $\sim 1$  kV/m)





## Numerical Wake Field Solvers

- URMEL – computes resonant modes in cavities and cut-off frequencies of longitudinally homogeneous fields in waveguides.
- ABCI – solves Maxwell's equations directly in the time domain when a bunched beam passes through a structure.



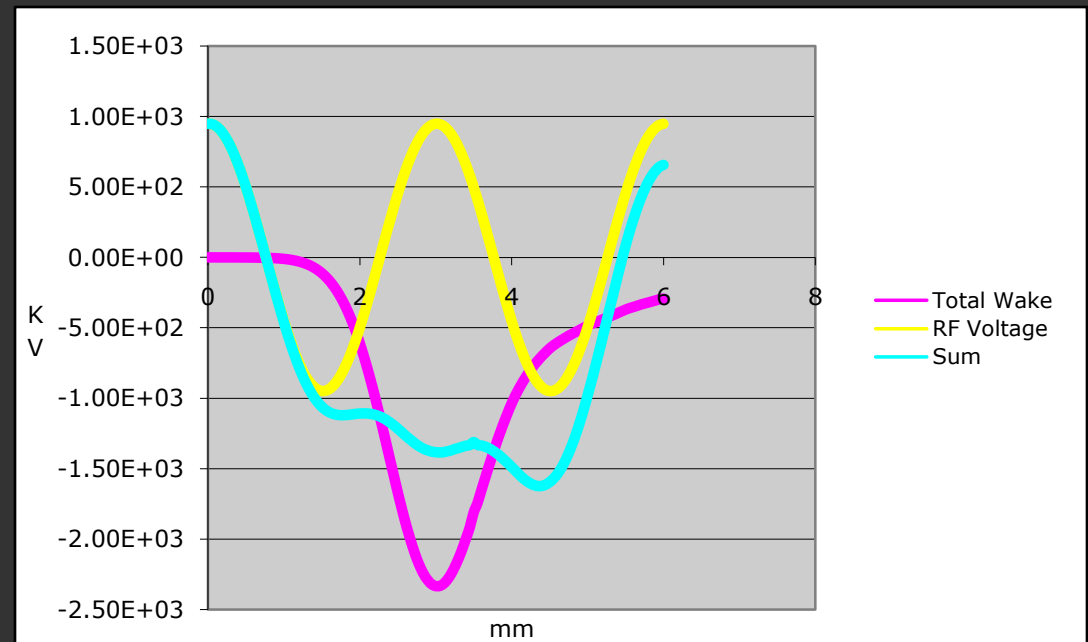
## Why care?

- N.B.: The longitudinal component of wake field is the more important component (cylindrically symmetry).
- Particles within a bunch experience Lorentz forces.
- Fields left behind = energy loss
- BUT: the energy loss can be recycled



# Recipe for a Possible Solution (in a nutshell)

1. Extract RF power from the wake of a short driving bunch (dielectric loading)
2. Inject RF power in a longer bunch (correctional superposition)
3. Apply sloping and DC corrections





## Pipe with Dielectric Layer (E-fields at $\Phi=0$ )

Calculated using URMEL-T (triangular mesh)

Partially trapped mode

Tapering models infinite length



## What I've been doing

- Extrapolating from data calculated for a 0.6 mm bunch (explained briefly in next couple of slides)
- Writing some convenience-motivated scripts to parse URMEL/ABCI output files
- Familiarizing myself with the literature and existing software
- Running simulations to gain intuition





## Rescaling wake data

$W(s) \equiv$  Wake of a 0.6 mm bunch

$W'(s) \equiv$  Wake of a bunch with variable length

$\rho \equiv$  Charge density (gaussian) of a 0.6 mm bunch

$\rho' \equiv$  Charge density (gaussian) of a variable length bunch

$$W(s) = \rho \otimes W_\delta$$

$$\mathcal{F}\{W(s)\} = \mathcal{F}\{\rho\} \mathcal{F}\{W_\delta\}$$

$$\mathcal{F}\{W'(s)\} = \mathcal{F}\{\rho'\} \mathcal{F}\{W_\delta\}$$

$$\mathcal{F}\{W'(s)\} = \frac{\mathcal{F}\{\rho'\}}{\mathcal{F}\{\rho\}} \cdot \mathcal{F}\{W(s)\}$$

$$W'(s) = W \otimes \mathcal{F}^{-1} \left\{ \frac{\mathcal{F}\{\rho'\}}{\mathcal{F}\{\rho\}} \right\}$$





## What's next

- Design: optimize dielectric resonator and coupler
- Verification: analyze existing wake data (which may need correction)
- More reading