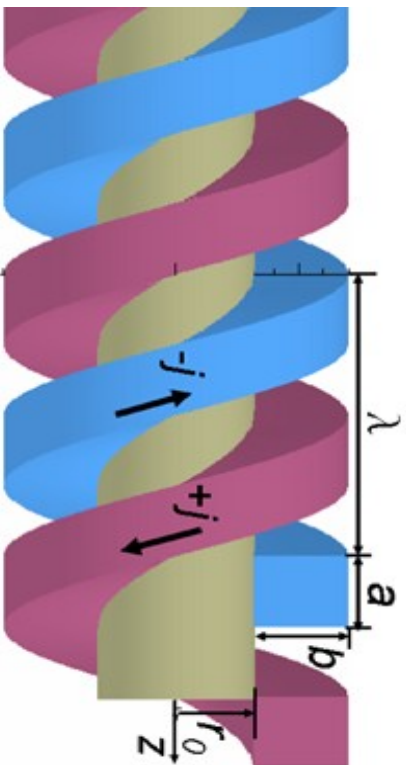


Helical Undulator Magnetic Field Optimization

Magnetic field vs conductor geometry



Previously was chosen

$a=5$ cm,

$b=5$ cm

and used corresponding current density to get 1.5 kG on-axis field.

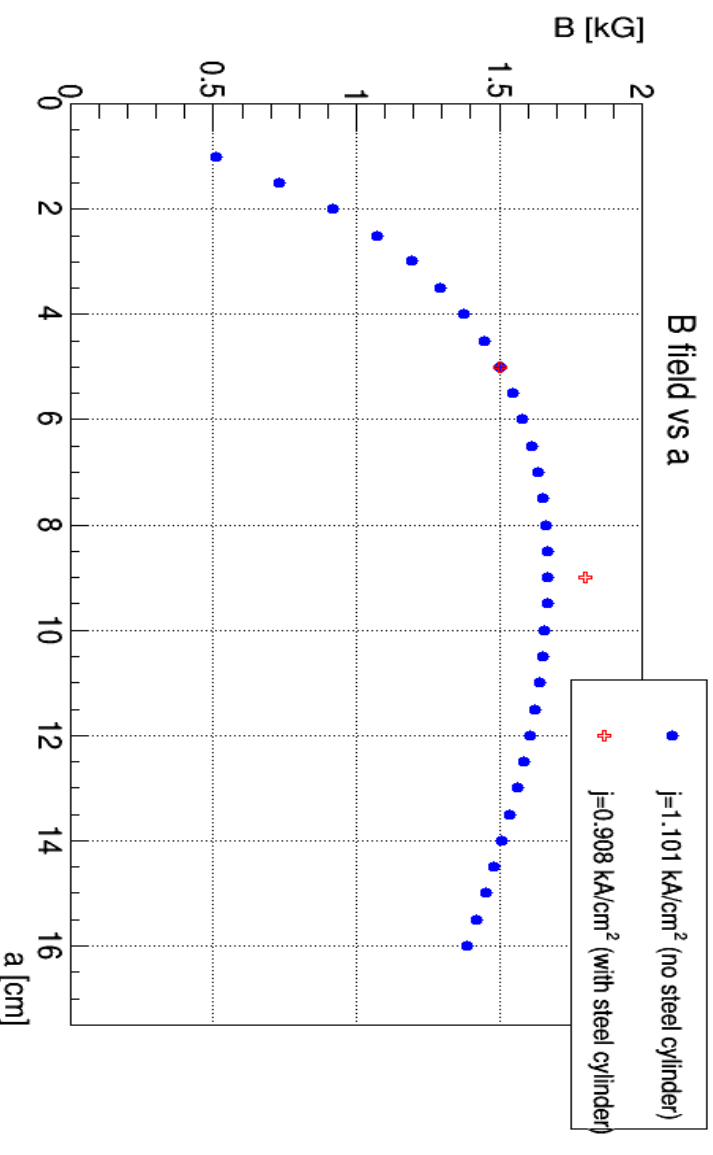
With

$a=9$ cm,

$b=2.8$ cm

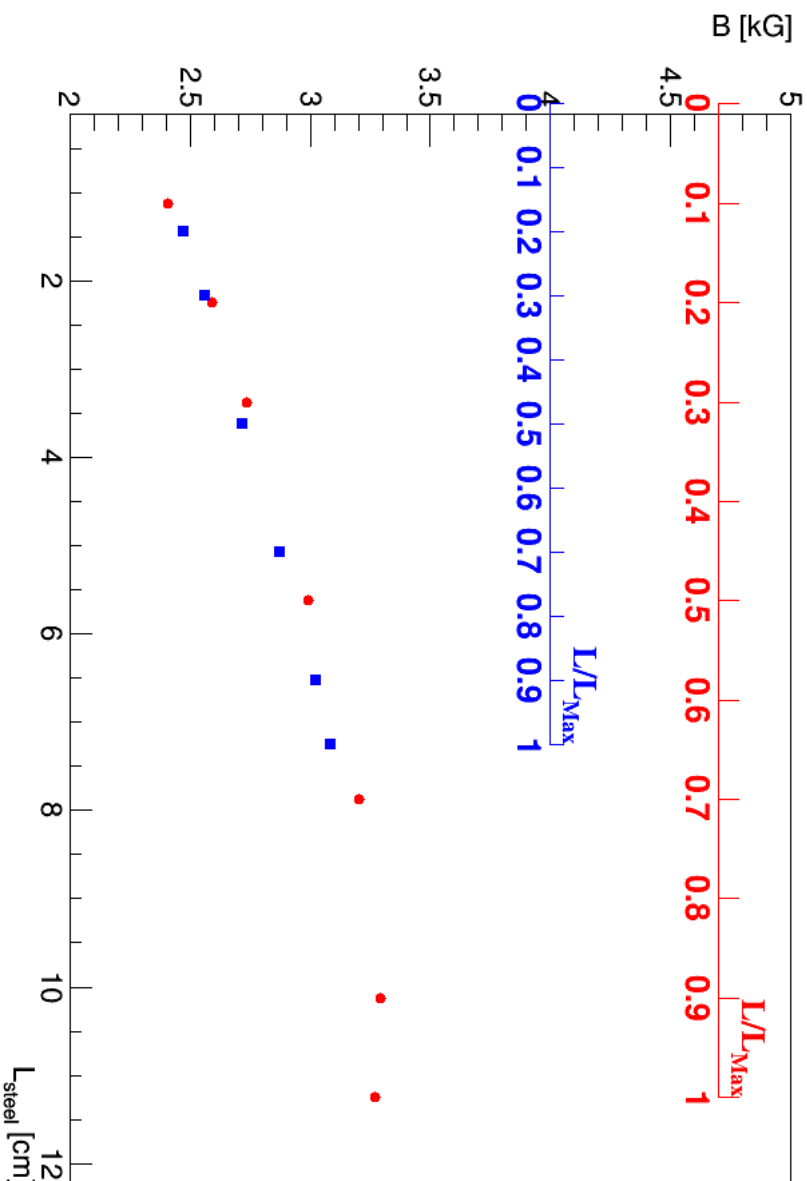
we get about 20% higher on-axis field

$b \times a = 25 \text{ cm}^2$, assuming the same number of conductors

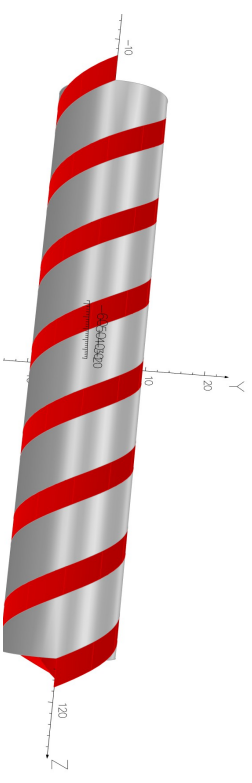
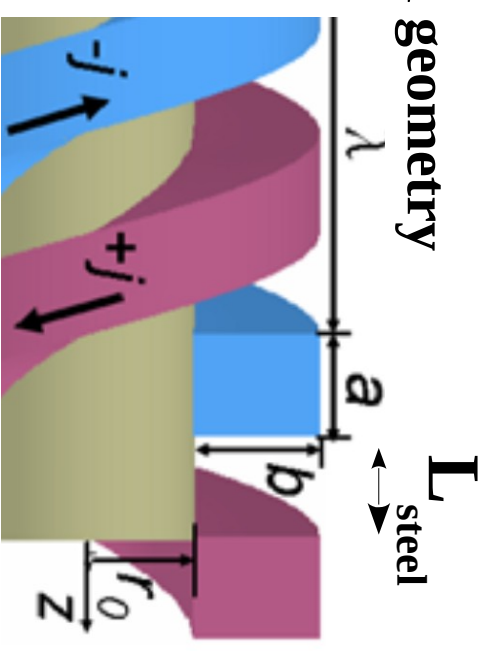


Magnetic field vs steel-spiral geometry

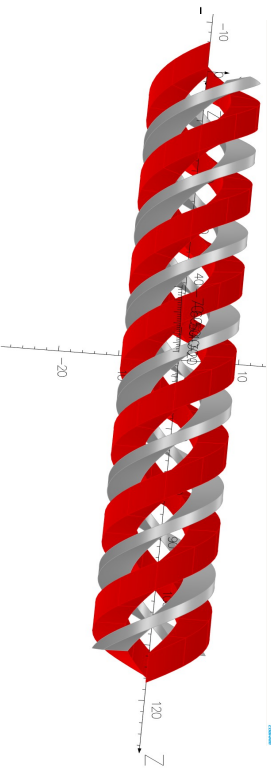
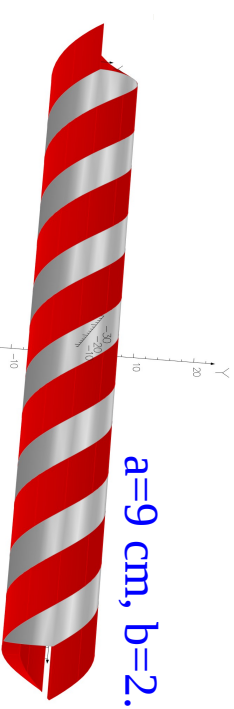
On-axis B field vs steel width (L)



$a=5$ cm, $b=5$ cm
 $a=9$ cm, $b=2.8$ cm

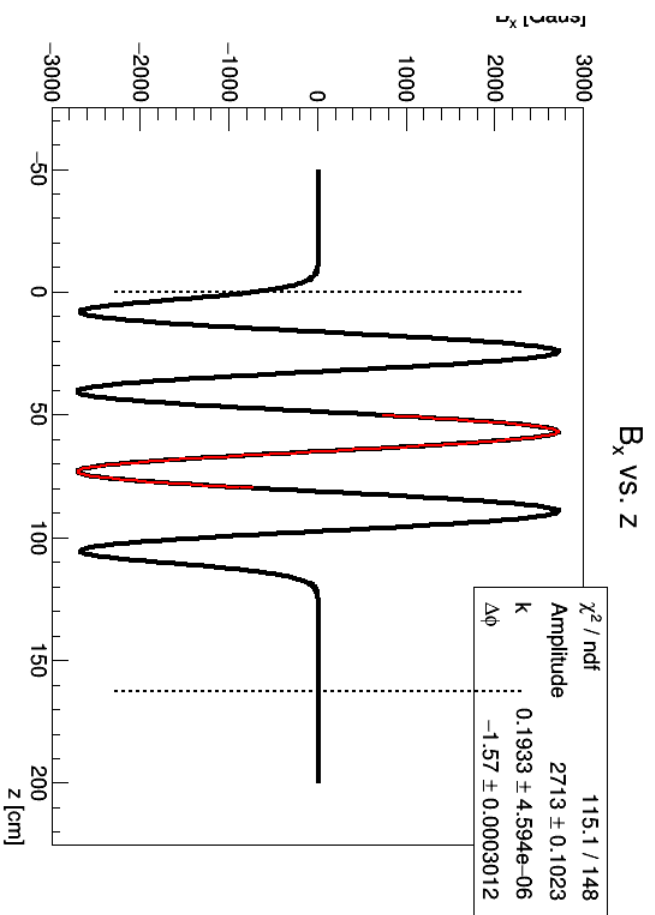


$a=9$ cm, $b=2.8$ cm

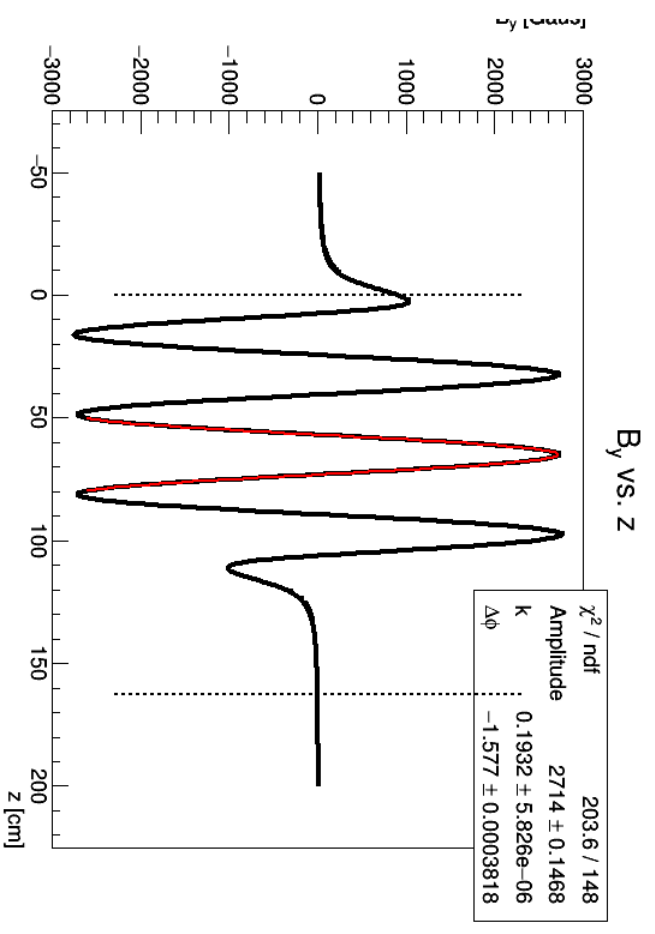


Magnetic field profile

$$B_x(z) = \text{Amp} * \sin(kz + \Delta\phi)$$

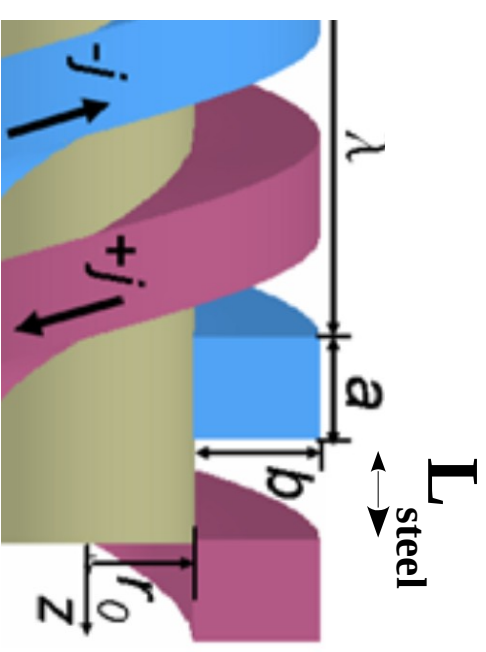
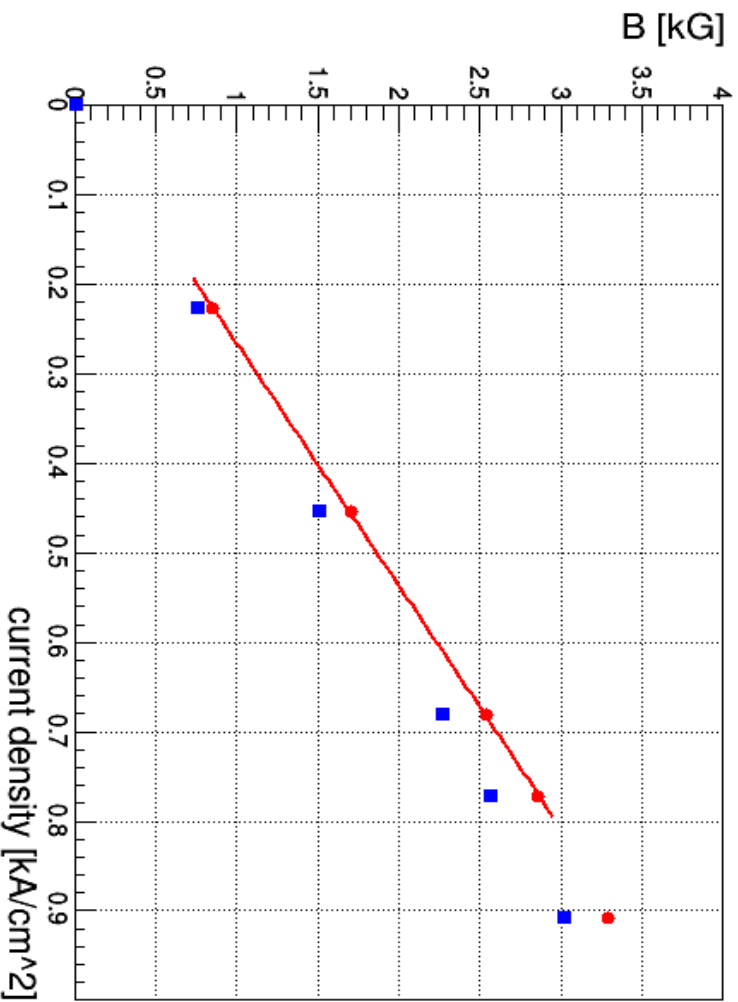


$$B_y(z) = \text{Amp} * \cos(kz + \Delta\phi)$$



Magnetic field vs current density

On-axis field vs current density

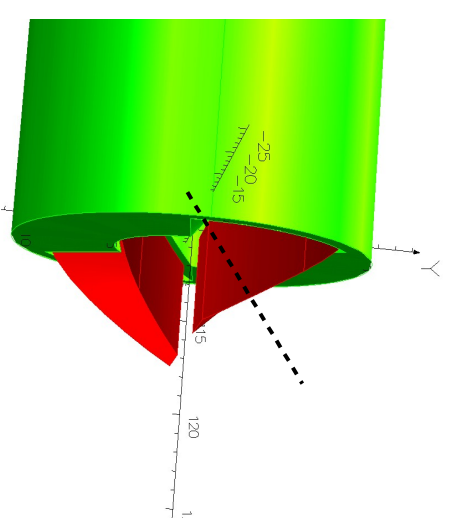


$a=5$ cm,
 $b=5$ cm,
 $L_{\text{steel}} = 10$ cm, steel (90% of available space)

$J_{\text{real}} = 1.24 * J_{\text{OPERA}}$ for $B_0 = 1.5$ kG $J = 0.508$ kA/cm²

$a=9$ cm,
 $b=2.8$ cm,
 $L_{\text{steel}} = 6.5$ cm, steel (90% of available space)

$J_{\text{real}} = 1.32 * J_{\text{OPERA}}$ for $B_0 = 1.5$ kG $J = 0.59$ kA/cm²



Summary

- **Adding spiral-steel material we can reduce the current density about twice**
- **On-axis transverse magnetic field still has Sin-Cos profile**