

# Accelerator Physics - Homework 7

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### Exercise (Review)

Go through the notes that describe the simplified coordinate system for  $J$  and  $\varphi$  and lead to the single resonance Hamilton function. Write a successive list of the main steps and approximations taken to obtain at the single resonance approximation. When is this approximation a good model of a realistic accelerator?

### Exercise (Single resonance approximation)

An accelerator with linear optical elements, i.e. dipoles and quadrupoles. Use first order perturbation theory in nonlinear forces  $\Delta f$  to find which resonances can occur in the Hamilton function:

- (a) for a circular accelerator with one short sextupole that you approximate as a delta function.
- (b) for a circular accelerator with one continuous and constant sextupole strength all around the ring.

### Exercise(Review)

Go through the steps of finding a fixed point in the single resonance system. Start with the single resonance Hamiltonian and write a list of the main steps taken to obtain the fixed points and to determine their stability.

### Exercise (Amplitude dependent tune shift)

Compute the horizontal tune distribution  $\rho(\nu_x)$  for a Gaussian beam with an emittance of  $\epsilon = 180\text{nm}$  when the ring has the tune of  $\nu = 0.52$  and there is an octupole of strength  $2\text{m}^4$  with length  $1\text{m}$  at a place with  $\beta_x$  of  $40\text{m}$ .

### Exercise (Preparation for class)

Sleep well.