

PHYSICS WITH EXTRA DIMENSIONS

— Models and Collider Signatures

Tao Han, Univ. of Wisconsin-Madison

(ILC, Snowmass, Aug. 22, 2005)

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- ♠. Extra Dimensions: a fascinating thought
- ♠. Extra Dimensional Models
- ♠. Collider Signatures
- ♠. Summary

♠. Old Stories about Extra Dimensions

1914: G. Nordstrom considered

$$d = 5 :$$

$$A_{\hat{\mu}}(\hat{\mu} = 0, 1, 2, 3, 5) \Rightarrow A_{\mu}(\mu = 0, 1, 2, 3) + \phi$$

with scalar ϕ identified as gravitational field!

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1915: A. Einstein told us:

$$g_{\mu\nu} \rightarrow \eta_{\mu\nu} + \kappa h_{\mu\nu}$$

$$\text{metric } \text{dia}(\eta_{\mu\nu}) = (1, -1, -1, -1),$$

$h_{\mu\nu}$: the gravitational field.

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1921: Th. Kaluza; 1926: O. Klein

$$d = 5 :$$

$$\gamma_{\hat{\mu}\hat{\nu}}(\hat{\mu} = 0, 1, 2, 3, 5) \Rightarrow g_{\mu\nu}(\mu = 0, 1, 2, 3) + A_{\mu} + \phi$$

leads to gravity + $E\&M$ in 4D.

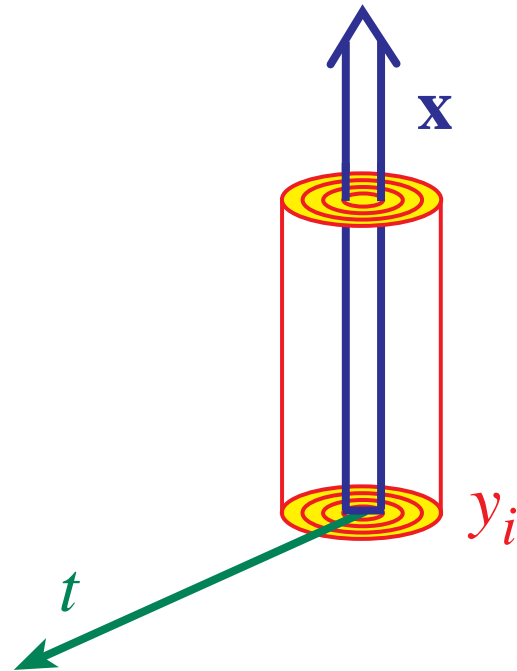
Wouldn't that be great !

(some quest with ϕ ...)

What happened to the extra dimension y ?

- Too small to see ?

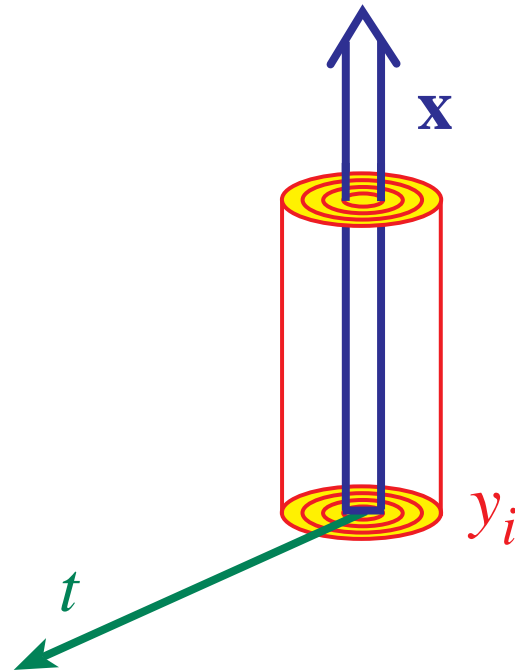
If our Universe (\vec{x}) is expanding as a function of t , why not some part (y) has shrunk or compactified ?



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If our Universe (\vec{x}) is expanding as a function of t , why not some part (y) has shrunk or compactified ?



- Too elusive to probe ?

Our $E\&M$ probes can't get there ?

Only gravity lives there (possibly large).

If the extra dimension becomes compact (a circle of radius R), then all fields (gravitational, electromagnetic etc.) in y -dimension are periodic functions :

$$F(x, y) = \sum_{n=-\infty}^{\infty} F^n(x) e^{in \cdot y/R}.$$

Equation of motion:

$$\begin{aligned} (\partial^\mu \partial_\mu - \partial^y \partial_y) F(x, y) &\Rightarrow (\partial^\mu \partial_\mu + \frac{n^2}{R^2}) F^n(x) \\ \Rightarrow m_n &\sim \frac{n}{R} \quad (\text{a set of tower!}) \end{aligned}$$

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$$\Delta M_{KK} = 1/R.$$

No γ_{KK} , e_{KK}^- , ... found $\Rightarrow R^{-1}$ large; or γ , e^- ... don't go there.

★ Extra Dimensions in String Theory:

80's: Green-Schwarz-Witten et al.

Bosonic String: 26-dim (anomaly-free)

Superstring: 10-dim

Supergravity: 11-dim

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String theory \Rightarrow extra dimensions!

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99–00's: Large extra dimensions ? ...

Arkani-Hamed, Antoniadis, Dimopoulos and Dvali: hierarchy

K. Dienes, E. Dudas, T. Gherghetta: coupling unification

Randall and Sundrum: hierarchy

Many more incarnations ...

♠ Low-Scale Extra Dimension Models (partial list)

General Consideration:

- In a factorizable flat metric:

$$ds^2 = \eta_{MN} dx^M dx^N, \quad M, N = (0, 1, \dots, 4 + n),$$

with Minkowski metric $\eta_{MM} = (1, -1, -1, \dots)$.

In general, a $4 + n$ -dimensional gravity action:

$$S = \frac{1}{2} M_D^{n+2} \int d^{4+n}x \sqrt{-g} \mathcal{R},$$

where M_D : the $4 + n$ -dim Planck scale.

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- The most general 4d Poincare invariant solution:

$$ds^2 = e^{2A(y)} \eta_{\mu\nu} dx^\mu dx^\nu - dy^i dy_i,$$

where $e^{2A(y)}$: a “warp” factor: the shape of space-time in y .

The 4-dim Planck scale is:

$$M_{pl}^2 = M_D^{n+2} \int d^n y e^{2A(y)} \equiv M_D^{n+2} V_n.$$

M_{pl} is made of M_D^{n+2} , V_n .

- Theory in 4d and KK decomposition:

$$\mathcal{L}^{(4)} = \int d^n y \mathcal{L}^{(4+n)}(\hat{F}_{MN}, \hat{\psi}, \hat{H}).$$

With y_i compactified,

$$\hat{F}(x, y_i) = \sum^k F_k(x) \left(a_k \sin \frac{ky}{R} + b_k \cos \frac{ky}{R} \right).$$

satisfying the boundary conditions in y_i .

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- Masses for KK modes: Stringy states: Winding modes:

$$M_{KK} \sim n/R, \quad \sqrt{n}M_S, \quad nRM_S^2.$$

- Graviton Interactions With Matter Fields:

$$S = \int d^4 x \sqrt{-\hat{g}} \mathcal{L}^{(4)} \approx -\frac{\kappa}{2} \int d^4 x (h_{\vec{n}}^{\mu\nu} + \phi_{\vec{n}} \eta^{\mu\nu}) T_{\mu\nu},$$

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The energy-momentum tensor, $T_{\mu\nu}$, includes all matter:

$$T_{\mu\nu}^{\text{fermions}}, T_{\mu\nu}^{\text{scalars}}, T_{\mu\nu}^{\text{EW}}, T_{\mu\nu}^{\text{QCD}} \dots$$

The rule: a graviton couples to EVERYTHING

Large Extra Dimensions (ADD) :

With n extra dimensions compactified on a torus of radius R ,

$$M_{pl}^2 \sim R^n M_D^{n+2}$$

Two fundamental scales: R and M_D (or M_S),*

* Arkani-Hamed, Antoniadis, Dimopoulos and Dvali.

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If $M_S \lesssim M_{pl}$, then $R \lesssim 1/M_S \sim 10^{-32}$ cm.

Too small to be appreciable !

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Low Scale Superstring: †

If $M_S \ll M_{pl}$ as low as $\mathcal{O}(1 \text{ TeV})$, (**Good!**) then

$$R \sim \frac{M_{pl}^{2/n}}{M_S^{2/n+1}} \approx \begin{cases} \mathcal{O}(0.1 \text{ mm}) & \text{for } n = 2 \\ \mathcal{O}(1.0 \text{ fm}) & \text{for } n = 7 \end{cases}$$

leads to “large” extra dimensions.

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- Table-top gravity experiments to reach $R \sim 0.1 \text{ mm}$,
- may search for light KK gravitons:
 $m = n/R \sim 10^{-3} \text{ eV} - 100 \text{ MeV}$.

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Although only gravitons in the extra dimensions,
it is more than just gravitational effects:

★ KK Graviton Density[‡]

If R is large, there will be a high degeneracy:

$$\begin{aligned}\Delta\vec{n}^2 &= \rho(m)dm^2, \\ \rho(m) &= \frac{\pi^{n/2}}{\Gamma(n/2)} R^n m^{n-2}.\end{aligned}$$

[‡]G. Giudice, R. Rattazzi and J. Wells;
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*Although each graviton couples gravitationally,
the high-degeneracy leads to*

$$\kappa^2 \rho(m) dm^2 \sim \kappa^2 R^n m^{n-2} dm^2 \sim E^n / M_S^{n+2}$$

Effective coupling $\kappa^2 \sim \frac{1}{M_{pl}^2} \rightarrow \frac{1}{M_S^2}$!

⇒ leads to possibly observable effects.

[‡]G. Giudice, R. Rattazzi and J. Wells;
T. Han, J. Lykken and R.-J. Zhang.

★ Bounds on the ADD model:

Table-Top Gravity Experiments:

A torsion pendulum/attractor experiment*
and a forced oscillator experiment†

New force with $r > 0.2$ mm excluded.

*E. Adelberger et al., Phys.Rev.Lett.86, 1418 (2001).

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Supernova bounds:

SN1987A energy-loss rate (mainly to ν 's), which leads to bounds§

$$n = 2 : \quad M_S > 30 - 130 \text{ TeV (!)}$$

$$n = 3 : \quad M_S > 2 - 9 \text{ TeV.}$$

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Neutron star heating:

Trapped KK gravitons in the SN core may overheat the NS.†

$$n = 2 : \quad M_S > 100 \text{ TeV}$$

$$n = 3 : \quad M_S > 10 \text{ TeV (!)}$$

These results have very little model-dependence.

$n < 3$ is strongly disfavored, if $M_S \sim \mathcal{O}(1 \text{ TeV})$.

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Universal Extra Dimensions (UED) :

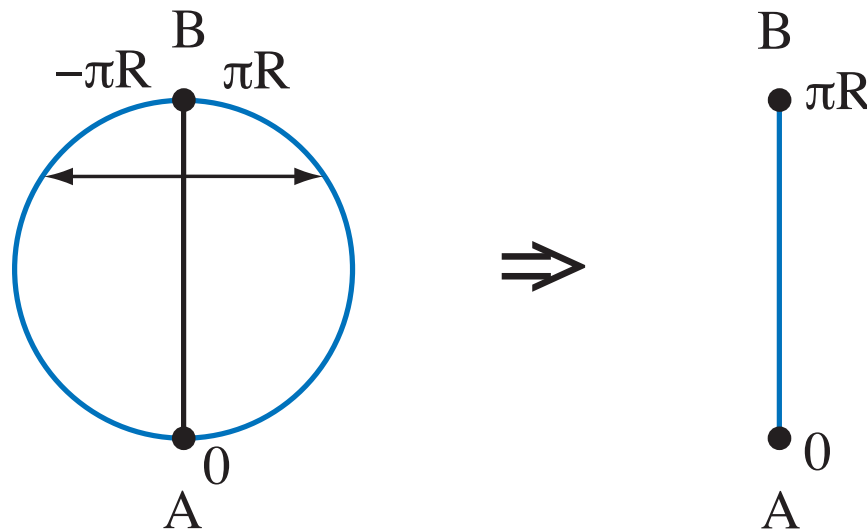
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★ “Orbifolding” S^1/Z_2 compactification:



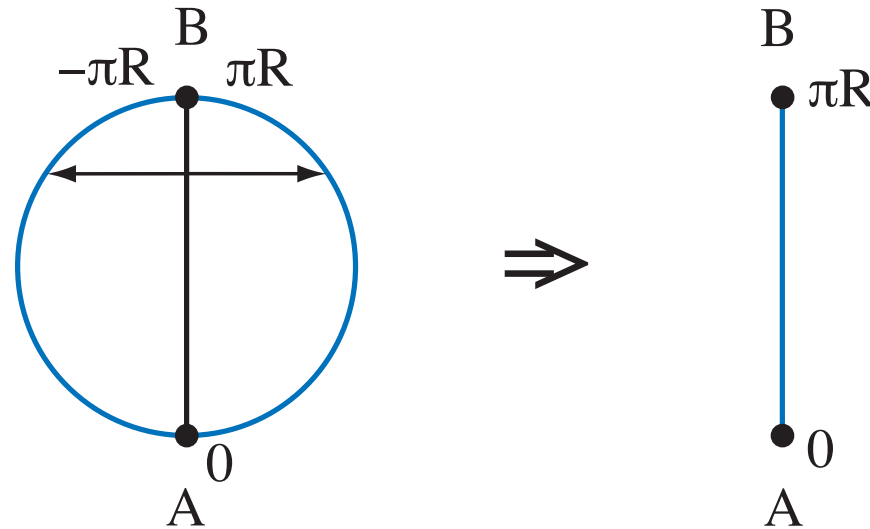
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★ “Orbifolding” S^1/Z_2 compactification:



- SM particles are the zero-modes;
- All particles have KK tower;
- KK-parity conserved.

★ Current bounds (both precision EW and Tevatron search)

$$M_{KK} \gtrsim 400 \text{ GeV} \quad \text{or} \quad R \lesssim \frac{1}{0.5 \text{ TeV}} \sim 10^{-15} \text{ mm.}$$

[¶]T. Appelquist, H.-C. Cheng, B.A. Dobrescu (2001).

The Randall-Sundrum Scenario:

In a 5-dim space, Randall and Sundrum found a static solution:*

$$ds^2 = e^{2A(y)} \eta_{\mu\nu} dx^\mu dx^\nu - dy^2,$$

where the “warp” factor $A(y) = -ky$,
with k the curvature scale in the 5th-dim.

*L. Randall, R. Sundrum, [hep-th/9905221](https://arxiv.org/abs/hep-th/9905221).

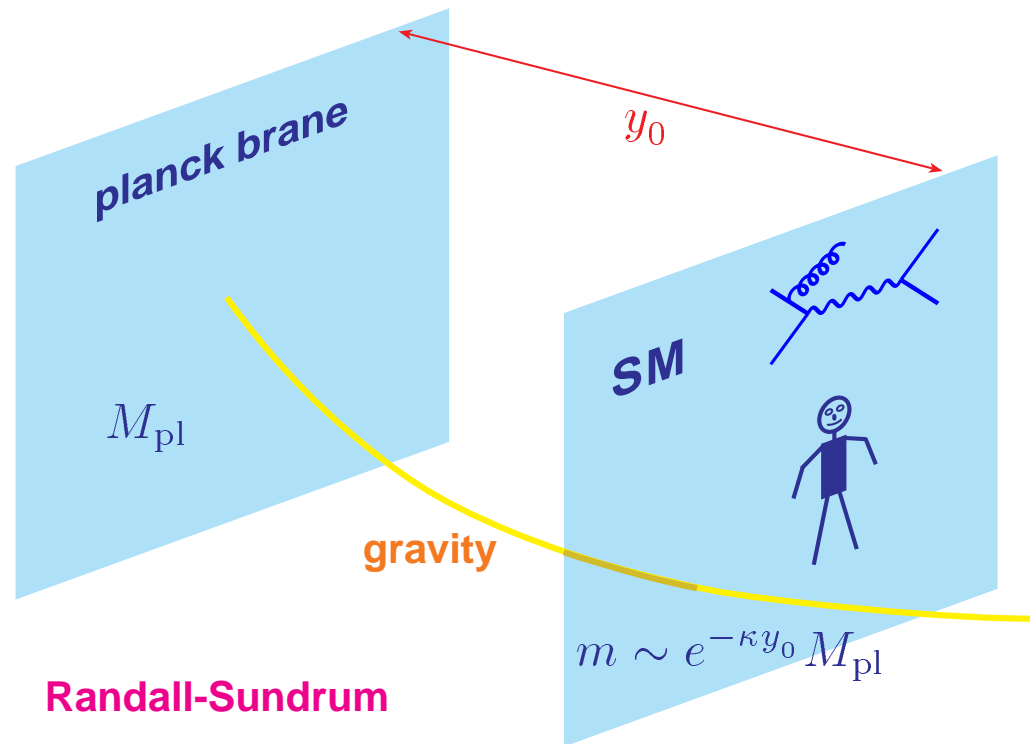
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The extra dimension y is “warped”.



*L. Randall, R. Sundrum, hep-th/9905221.

★ Mass hierarchy M_{pl}/M_{EW} generated on the two branes:

$$v = e^{-ky_0} M_{pl}.$$

To get $v \approx 246$ GeV, need $ky_0 \approx 40$.

The “size” of extra-dim: $y_0 \sim (10 - 100) l_{pl}$.

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★ KK decomposition:‡

Bulk fields:

$$\hat{F}_q(x, y_i) \sim \sum_k F_k(x) (a_k J_q + b_k Y_q),$$

where J_q, Y_q are Bessel functions of order $q=1,2$, half-integers for a gauge boson, graviton, fermion, respectively.

KK states $h_{KK}^{\mu\nu}, A_{KK}^\mu, f_{KK} \dots$ with masses $M_{KK} \sim e^{-ky_0} M_{pl}$, and with 1/TeV couplings.

Tension with EW data were studied and more involved configuration needed.||

‡Davoudiasl, Hewett, Rizzo, hep-ph/9909255.

||Gherhetta and Pomarol, hep-ph/0003129; Hewett, Petriello, Rizzo, hep-ph/0203091.

Variations of The RS Model:

★ Bulk Fields with Custodial Symmetry**

All fields in the bulk, with an enhanced gauge symmetry

$$SU_R(2) \times SU_L(2) \times U(1).$$

Electroweak symmetry broken by the Higgs field on the TeV brane.

Corrections to T (or ρ) small if $M_{KK} \sim$ a few TeV.

**Agashe, Delgado, May, and Sundrum, [hep-ph/0308036](#)

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★ Higgsless Model*

No Higgs fields at all;

Electroweak symmetry broken by the TeV brane boundary condition.

Tension between $W_L W_L$ scattering unitarity and the precision EW data severe †

** Agashe, Delgado, May, and Sundrum, [hep-ph/0308036](#)

* C.Csaki et al. [hep-ph/0305237](#), [hep-ph/0308038](#); Y.Nomura, [hep-ph/0309189](#).

† Hewett, Lillie, Rizzo, [hep-ph/0407059](#).

★ Orbifolding SUSY GUTS*

SUSY and GUTs breaking by orbifolding boundary conditions;
Electroweak scale generated by warping;

Distinctive feature: TeV scale GUT gauginos XY ;

However, the symmetry forbidding prompt proton decay
makes XY hard to observe:

stable charged hadrons $X, Y, (Xq\dots)$?

*Y.Nomura et al. [hep-ph/0209158](#); [hep-ph/0212134](#); [0305214](#).

Outcomes of Extra Dimensions Models:
an exciting frontier for explorers

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- Newton's law: modified at both short and long distances.*
- EWSB: gauge-boson masses and the Higgs[†], or “Higgsless”[‡]
- fermion masses: Yukawa couplings by displacement/overlapping^{††}
- ν masses/mixings: bulk neutrinos[¶]
- GUTs: gauge coupling power-law running* or log-running^{‡‡}
- SUSY GUTs: breaking by orbifolding[‡]
- new cosmology;[§] cosmological const.^{||}

*ADD; RS; Dvali et al.

†Cheng et al.; Luty et al.; Hall et al.; Ignatius et al.; Z. Chacko and A. Nelson

‡C. Csaki et al.

††Mirabelli and Schmaltz; Arkani-Hamed et al.

¶Mohapatra, Nandi, Perez-Lorenzana; Dienes et al.; Dimopoulos et al.

*Dienes, Dudas, Gherghetta; Dumitru and Nandi.

‡‡Agashe, Delgado and Sundrum, hep-ph/0212028.

‡Hall and Nomura; Hebecker and March-Russell et al.

§Binetruy et al.; Kaloper et al.; Csaki et al.; Flanagan et al.; Cline et al.; Kanti et al.; Mohapatra et al.

||Arkani-Hamed et al.; Silverstein et al.; Luty et al.

♠. Phenomenological Implications

▷ At “low” energies

- “very low”: $E \ll 1/R, M_S$:

4–dim effective theory: Standard Model + weak classical gravity.

(as our present experimental knowledge.)

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▷ At “low” energies

- “very low”: $E \ll 1/R, M_S$:

4–dim effective theory: Standard Model + weak classical gravity.

(as our present experimental knowledge.)

- march into the extra-dimensions: $1/R < E \ll M_S$,
(4 + n)–dim world directly probed, and gravity effects
observable:* mainly via light KK gravitons of mass

$$m_{KK} \sim 1/R,$$

or whatever propagate there \Rightarrow an effective theory (SM+KK).

*N. Arkani-Hamed, S. Dimopoulos, G. Dvali (1998);
G. Giudice, R. Rattazzi, J. Wells (1999);
T. Han, J. Lykken, R.J. Zhang. (1999);
Mirabelli, M. Peskin, M. Perelstein (1999);
J. Hewett (1999); T. Rizzo (1999); ...

▷ At intermediate energies $E \sim M_D, M_S$:
Stringy states significant* and resonances
at the s -channel poles dominant:†

$$\mathcal{M}(s, t) \sim \frac{t}{s - M_n^2}, \quad M_n = \sqrt{n}M_S.$$

*G. Shui and H. Tye (1998); K. Benakli (1999).

†Accomando, Antoniadis, Benakli (2000); Cullen, Perelstein, Peskin (2000).

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at the s -channel poles dominant:†

$$\mathcal{M}(s, t) \sim \frac{t}{s - M_n^2}, \quad M_n = \sqrt{n}M_S.$$

▷ At “trans Planckian” energies $E > M_D, M_S$:
 $(4 + n)$ -dim physics directly probed;
gravity dominant: black hole production*

$$M_{bh} = \sqrt{s} > M_D \text{ for } b < r_{bh}.$$

copiously produced at LHC or other TeV-scale experiments!

*G. Shui and H. Tye (1998); K. Benakli (1999).

†Accomando, Antoniadis, Benakli (2000); Cullen, Perelstein, Peskin (2000).

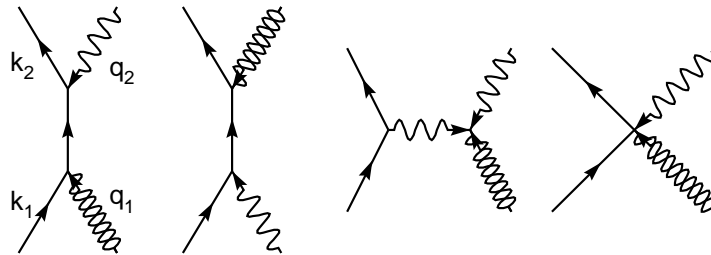
*T. Banks and W. Fischler (1999); E. Emparan et al. (2000);
S. Giddings and S. Thomas (2002);
S. Dimopoulos and G. Landsberg (2001).

★ Collider Searches for Extra Dimensions:

A. Collider Signals I (ADD)

Real KK Emission: Missing Energy Signature*

a. $e^+e^- \rightarrow \gamma + KK$ (γ +missing energy)



$n - \text{dim} :$	at LEP2	at LC(500)
$n = 4$	$M_S > 730$ (GeV)	4500
$n = 6$	$M_S > 520$ (GeV)	3100

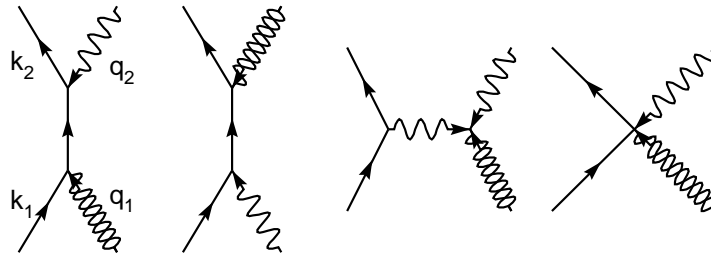
*Giudice, Rattazzi and Wells;
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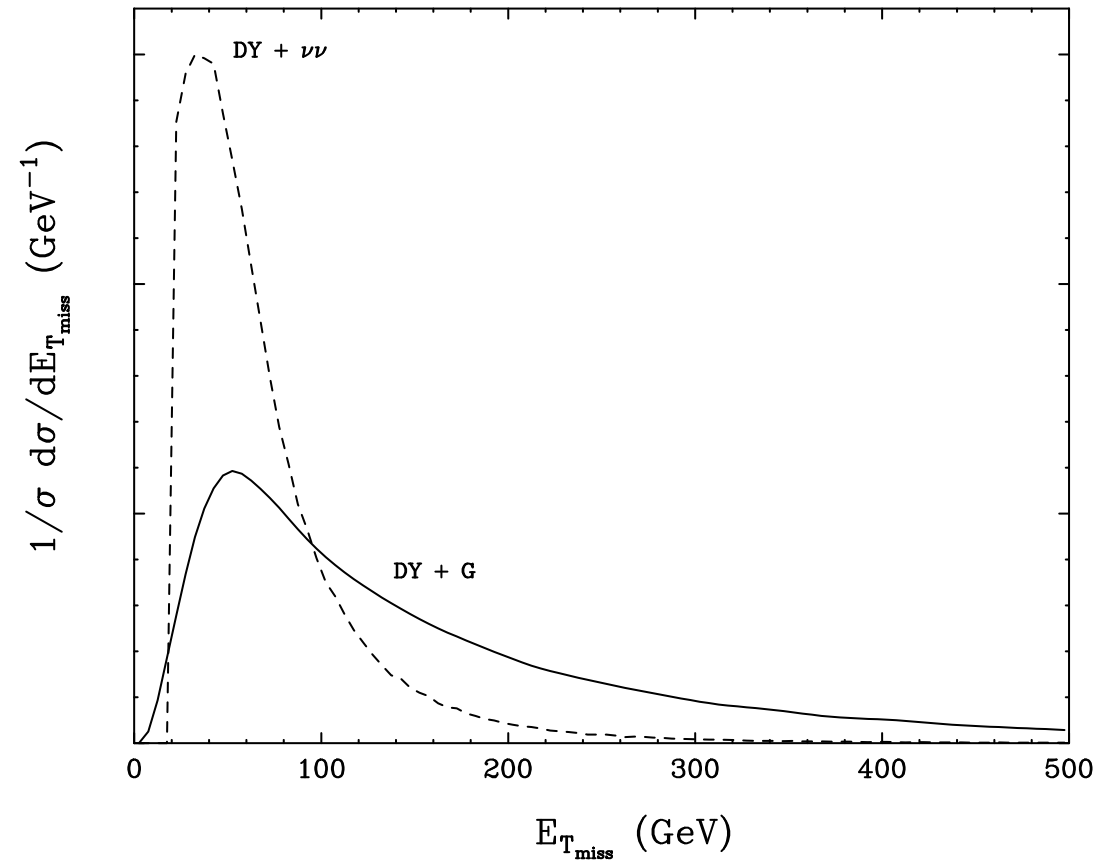
b. $p\bar{p} \rightarrow jet + KK$ (mono-jet+missing energy)

n – dim :	at Tevatron	at LHC
$n = 4$	$M_S > 900$ (GeV)	3400
$n = 6$	$M_S > 810$ (GeV)	3300

*Giudice, Rattazzi and Wells;
Mirabelli, Perelstein and Peskin;
Cheung and Keung

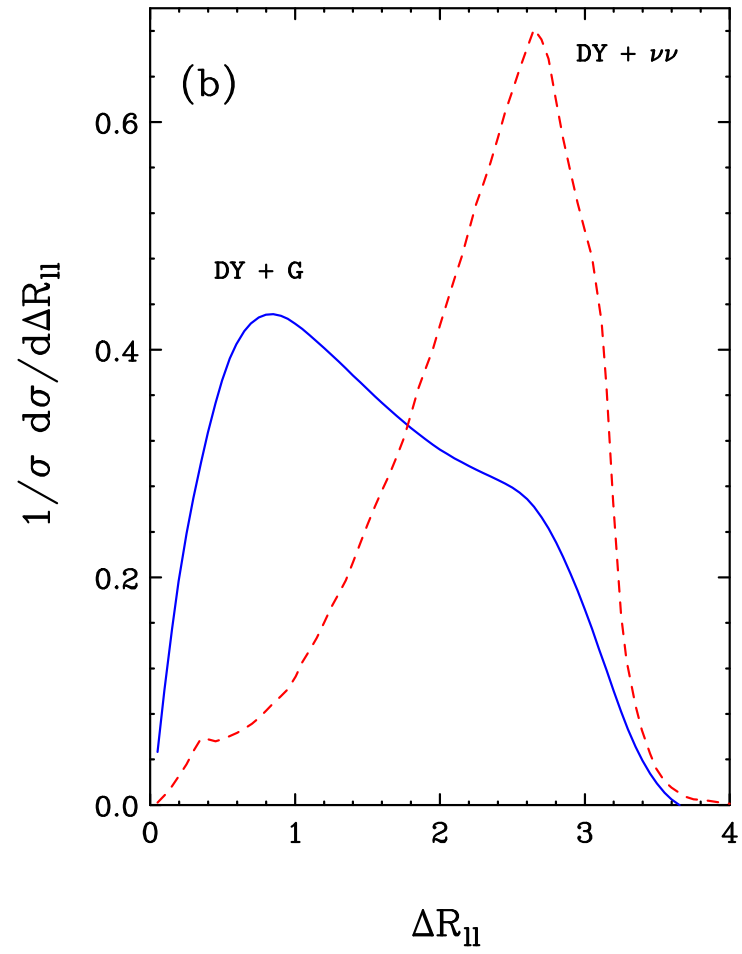
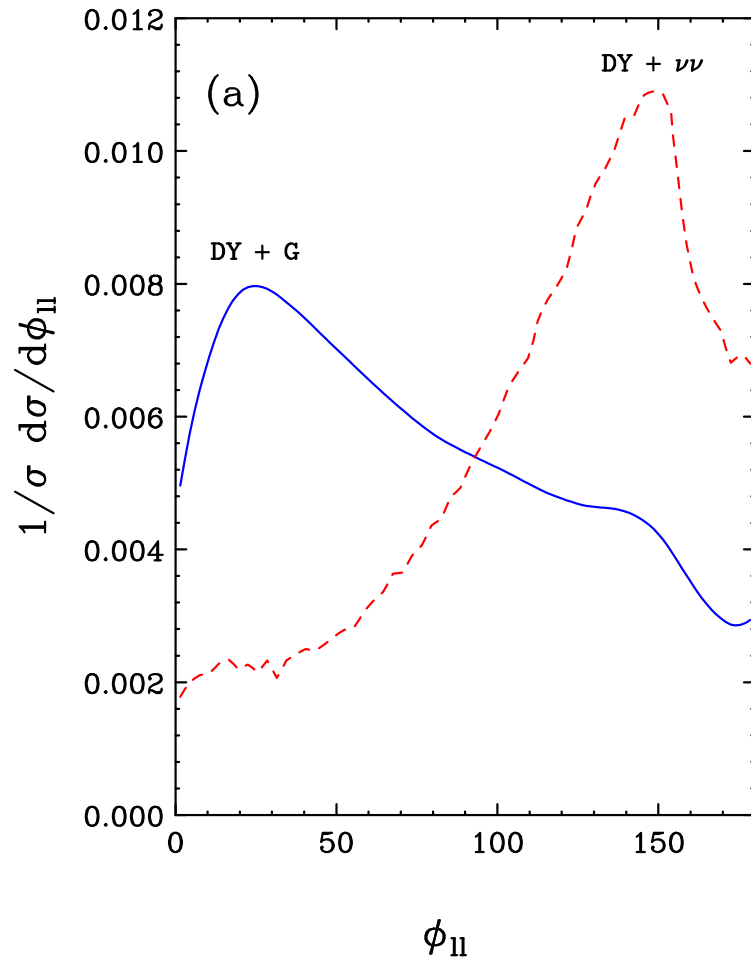
c. $p\bar{p} \rightarrow l^+l^- + KK$: Qualitative features? †

Larger/harder missing energies for the KK signal:



† Han, Rainwater and Zeppenfeld, [hep-ph/9905423](#), *Phys.Lett.* **B463**, 93(1999).

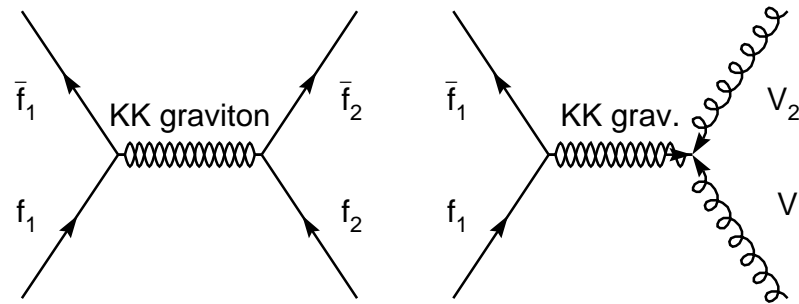
Consequently, the lepton opening angle is sensitive to it:



B. Collider Signals II (ADD)

Virtual KK Graviton Effects[‡]

On four-particle contact interactions:



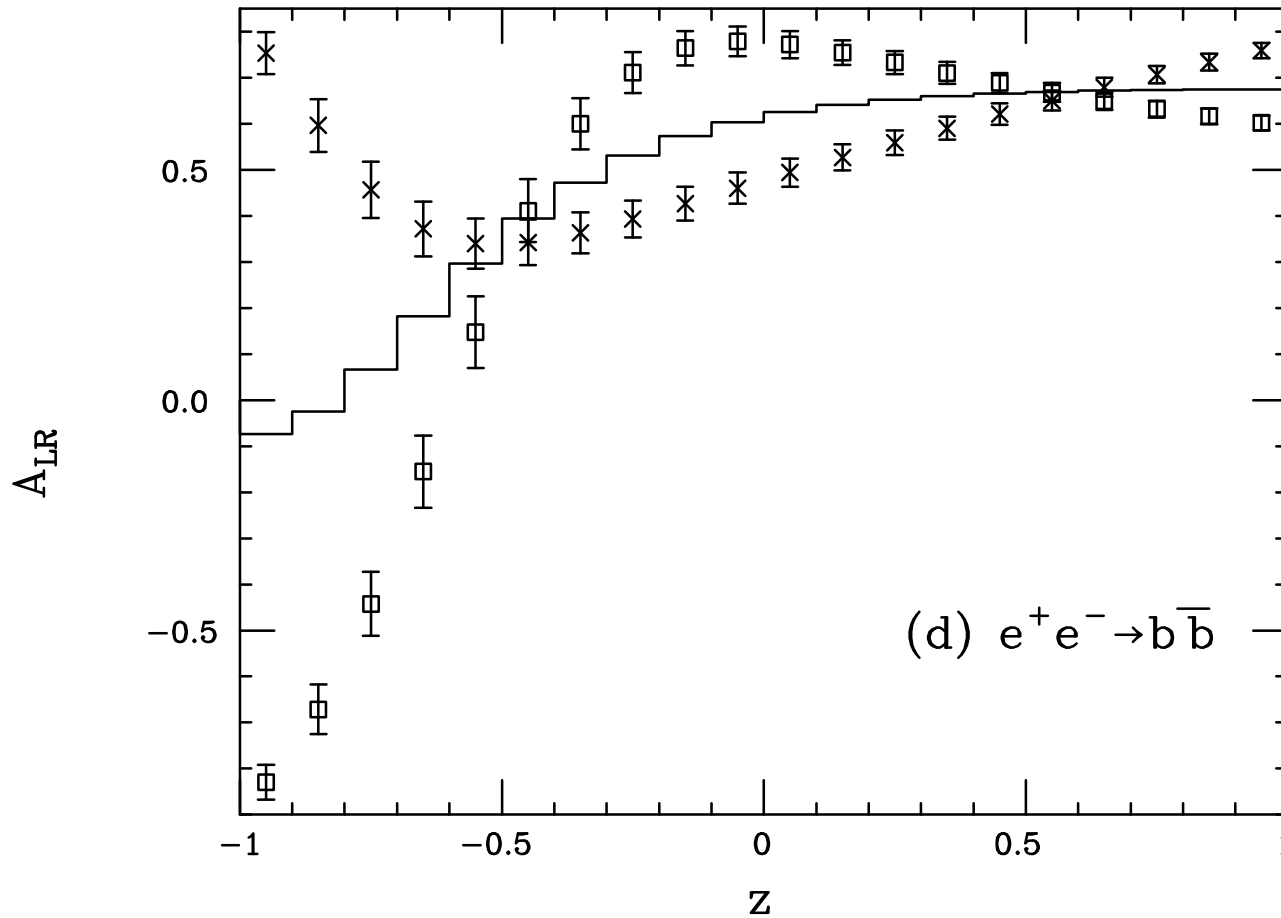
Sum over virtual KK exchanges:

$$\begin{aligned}
 i\mathcal{M} &\sim \bar{f}\mathcal{O}_if \bar{f}\mathcal{O}_jf \int_0^\infty \frac{dm_{\vec{n}}^2}{s - m_{\vec{n}}^2 + i\epsilon} \kappa^2 \rho(m_{\vec{n}}) \\
 &\sim \frac{s^2}{M_S^4} \bar{f}\mathcal{O}_if \bar{f}\mathcal{O}_jf.
 \end{aligned}$$

Again, effective coupling $\kappa^2 \sim \frac{1}{M_{pl}^2} \rightarrow \frac{1}{M_S^2}$!

[‡] Hewett; Han, Lykken and Zhang; Rizzo; Cheung; Agashe and Deshpande; Nussinov and Shrock; Shiu, Shrock and Tye; Atwood, Bar-Shalom and Soni; Mathews, Raychaudhuri and Sridhar;

Qualitative differences for signal/background distributions,
due to the **spin-2 exchange**:*



LR asymmetry for $e^+e^- \rightarrow b\bar{b}$ at $\sqrt{s} = 500$ GeV.
Solid: SM; “data” points for $\lambda = \pm 1$ with $75 fb^{-1}$.

*J.Hewett.

C. KK Resonant States at Colliders: (RS)

a. SM KK Particles:

If the SM fields (photons, electrons, Z , W , H^0 ...) also propagate in extra dimensions, then they have KK excitations.‡

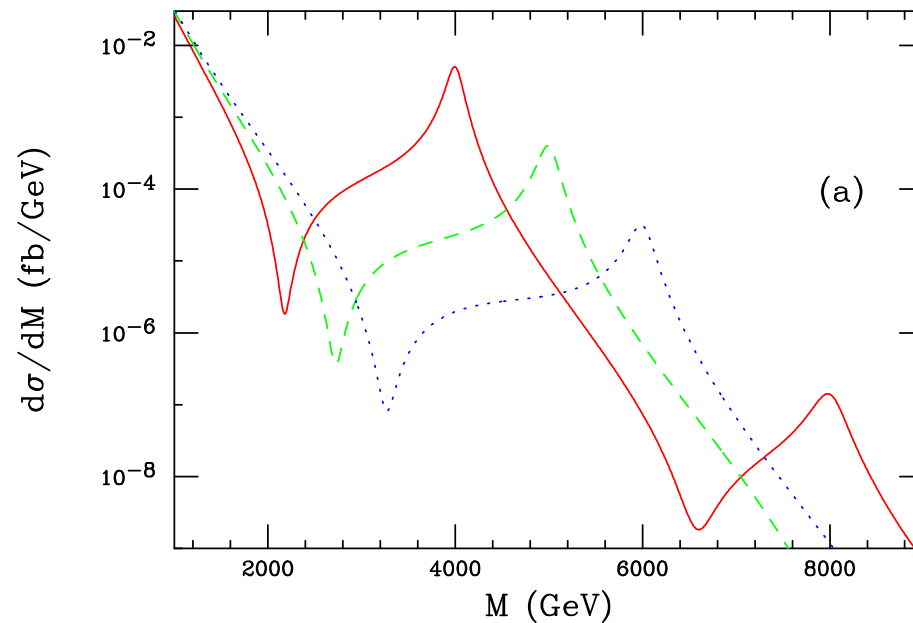
‡Davoudiasl, Hewett, Rizzo, [hep-ph/9911262](https://arxiv.org/abs/hep-ph/9911262).

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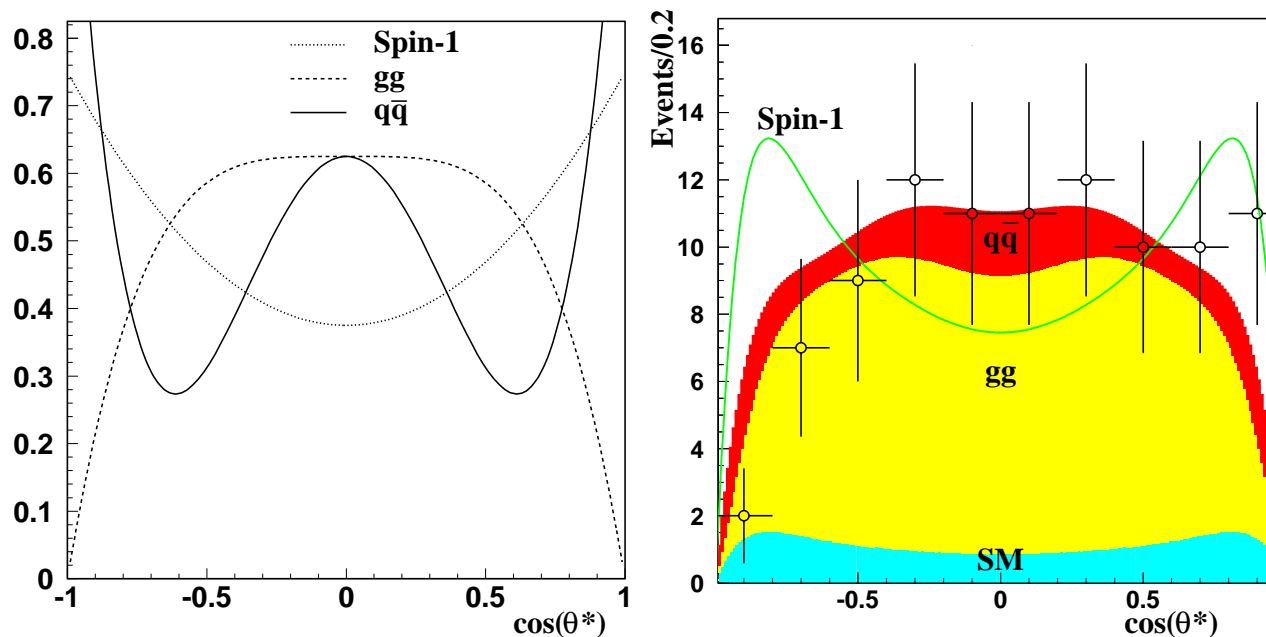
[‡]Davoudiasl, Hewett, Rizzo, [hep-ph/9911262](https://arxiv.org/abs/hep-ph/9911262).

b. Heavy KK gravitons

DY l^+l^- angular distributions:

$gg \rightarrow G \rightarrow e^+e^-$	$1 - \cos^4 \theta^*$
$q\bar{q} \rightarrow G \rightarrow e^+e^-$	$1 - 3 \cos^2 \theta^* + 4 \cos^4 \theta^*$
$q\bar{q}, gg \rightarrow V \rightarrow e^+e^-$	$1 + \alpha \cos^2 \theta^*$
$q\bar{q}, gg \rightarrow S \rightarrow e^+e^-$	1

At the LHC (ATLAS simulation*),



*Allanach et al., hep-ph/0006114

D. Stringy resonances at Colliders

Future colliders may reach the TeV string threshold thus directly produce the “stringy” resonant states.[†]
Amplitude factor near the resonance

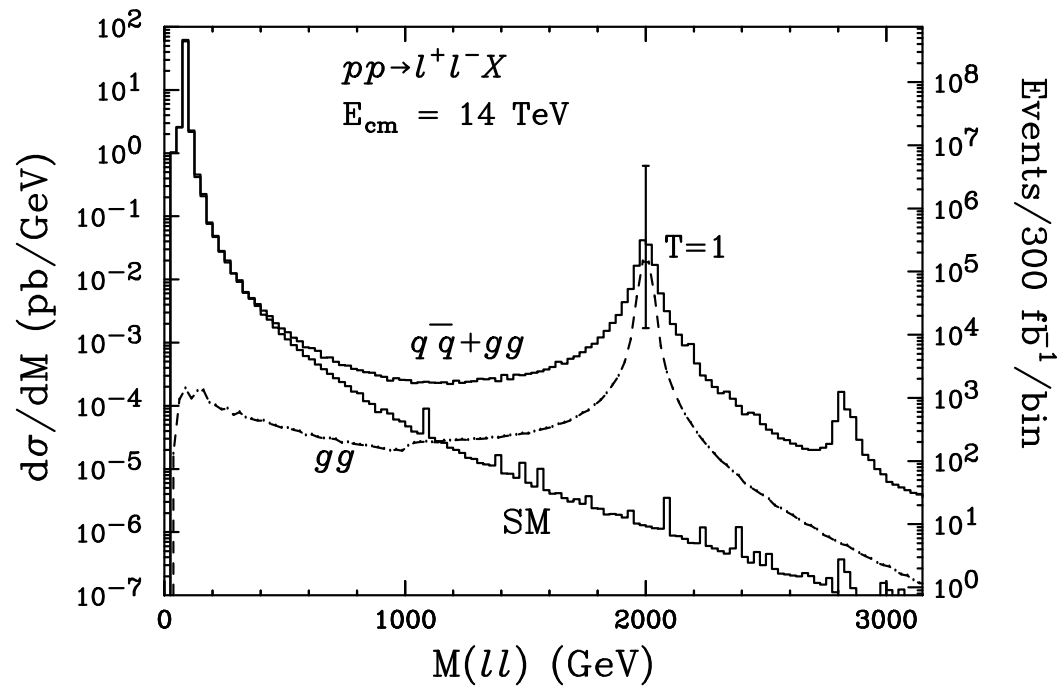
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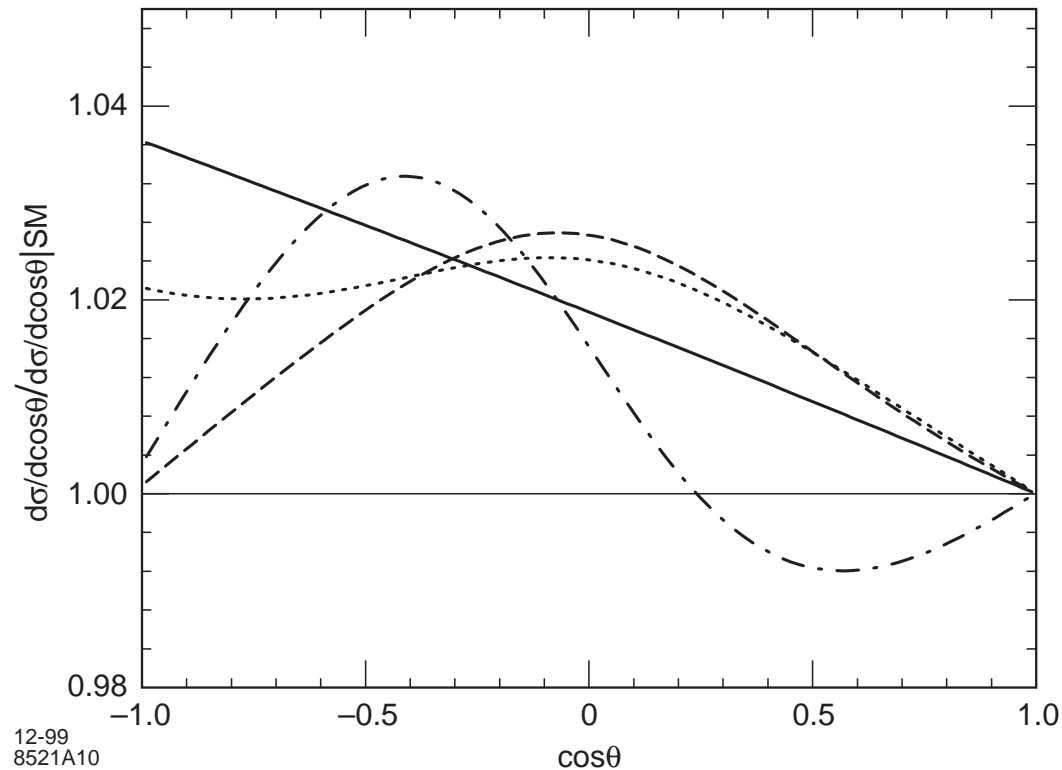
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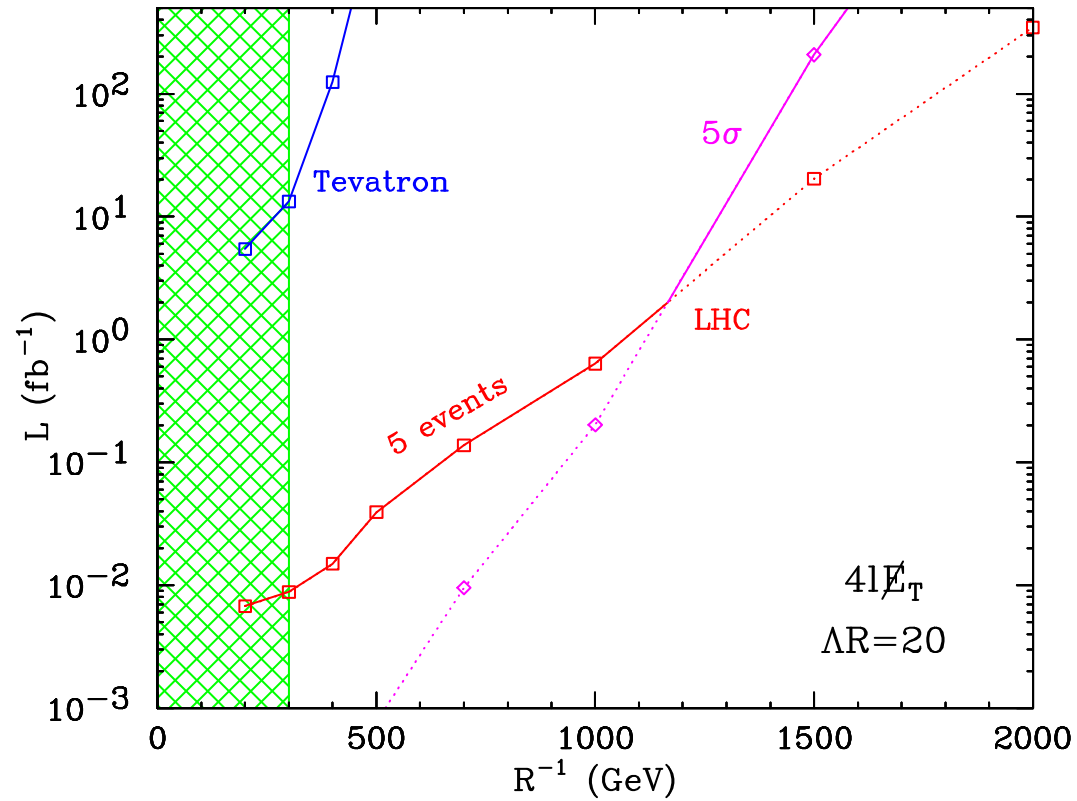
At the ILC:*



Comparison of deviations from the Standard Model prediction for Bhabha scattering at 1 TeV due to corrections from higher-dimension operators. The four curves represent: solid, string model with $M_S = 3.1$ TeV; dotted, KK exchange with $M_H = 6.2$ TeV; dashed, VV contact interactions with $\Lambda = 88$ TeV; dot-dash, AA contact interactions with $\Lambda = 62$ TeV.

*Cullen, Perelstein and Peskin hep-ph/0001166.

E. UED:*

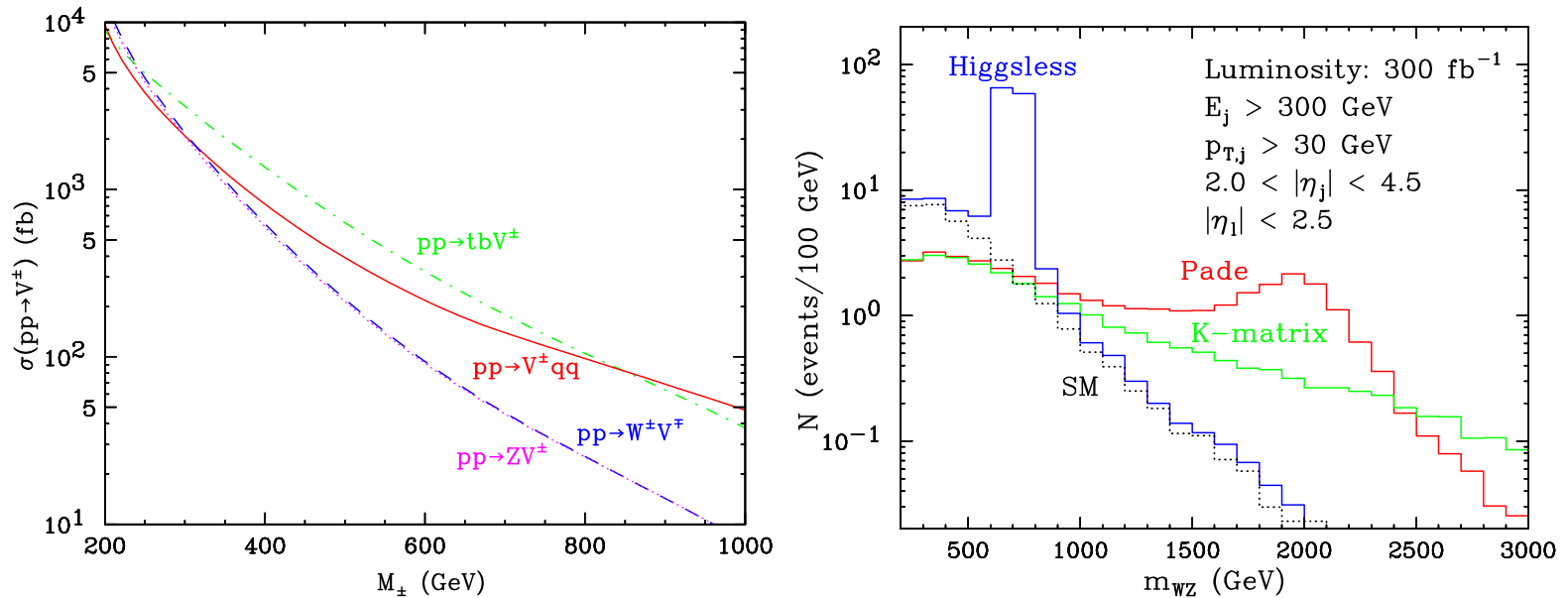


Discovery reach for MUEDs at the Tevatron (blue) and the LHC (red) in the $4l \cancel{E}_T$ channel. We require a 5σ excess or the observation of 5 signal events, and show the required total integrated luminosity per experiment (in fb^{-1}) as a function of R^{-1} , for $\Lambda R = 20$. (In either case we do not combine the two experiments).

*Cheng, Matchev, and Schmaltz, hep-ph/0205314.

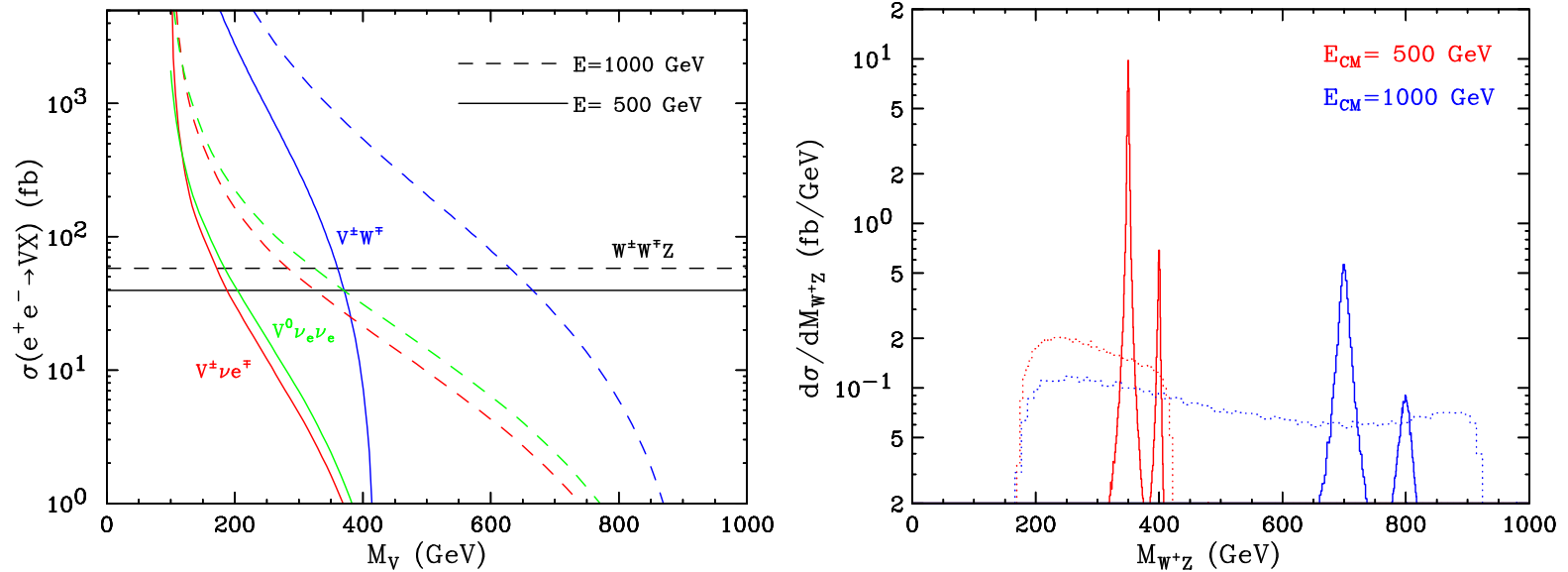
F. Higgsless:*

$$pp \rightarrow jj V_1^\pm \rightarrow jjWZ.$$



Left: Production cross-sections of V^\pm at the LHC. Here tbV^\pm production assumes SM-like couplings to third generation quarks. Right: The number of events per 100 GeV bin in the $2j + 3l + \nu$ channel at the LHC with an integrated luminosity of 300 fb^{-1} and cuts as indicated in the figure. Results are shown for the SM (dotted), the Higgsless model with $M_1^\pm = 700 \text{ GeV}$ (blue), and two "unitarization" models: Padé (red) and K-matrix (green).

*Birkedal, Matchev, and Perelstein, hep-ph/0508185.



Left: V_1 production cross-sections and the continuum SM background at an e^+e^- lepton collider of center of mass energy 500 GeV (solid) or 1 TeV (dashed). Right: WZ invariant mass distribution for Higgsless signals (solid) and SM background (dotted), at $E_{CM} = 500$ GeV (red, $M^\pm = 350, 400$ GeV) and $E_{CM} = 1$ TeV (blue, $M^\pm = 700, 800$ GeV).

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 - cosmic neutrinos: if $M_S \sim 1 - 3$ TeV; predate the LHC?
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Go Search for the Extra Dimensions !